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(54) **MULTILOOP INTERFEROMETERS FOR QUANTUM INFORMATION PROCESSING**

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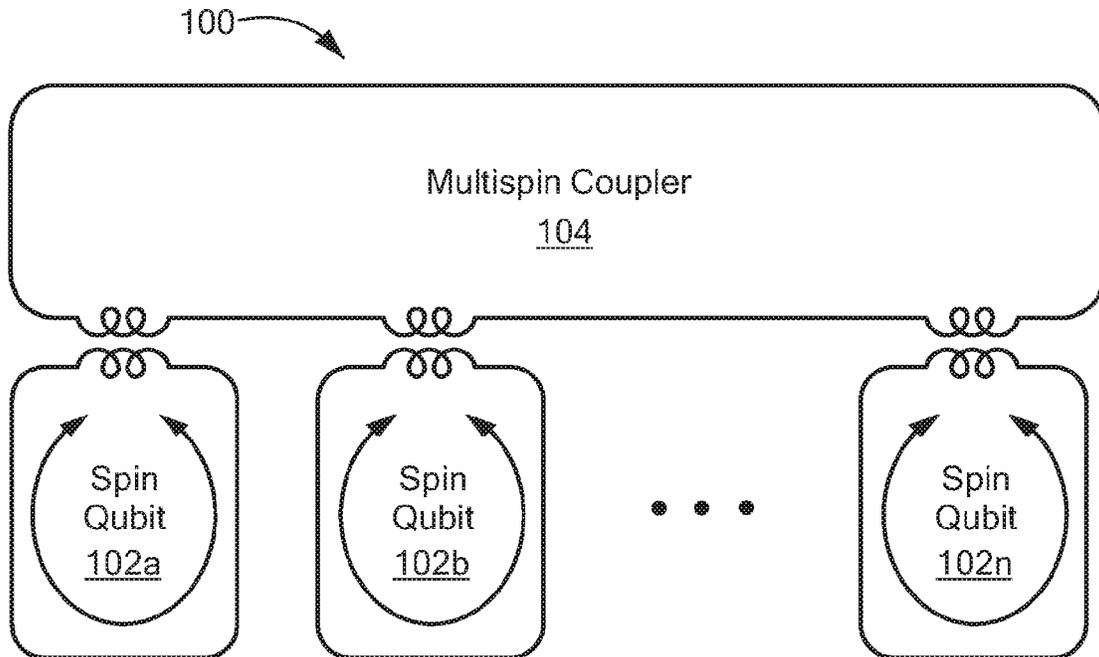
(57) **ABSTRACT**

(22) Filed: **Nov. 17, 2016**

Structures and techniques, using superconducting Josephson-junction based circuits, to directly engineer physical multiqubit (or “many-qubit”) interactions in a non-perturbative manner. In one embodiment, a system for multiqubit interaction includes: a multispin coupler including a plurality of loops, each loop having a pair of Josephson junctions; and a plurality of qubits each inductively coupled to the multispin coupler.

Related U.S. Application Data

(60) Provisional application No. 62/256,191, filed on Nov. 17, 2015.



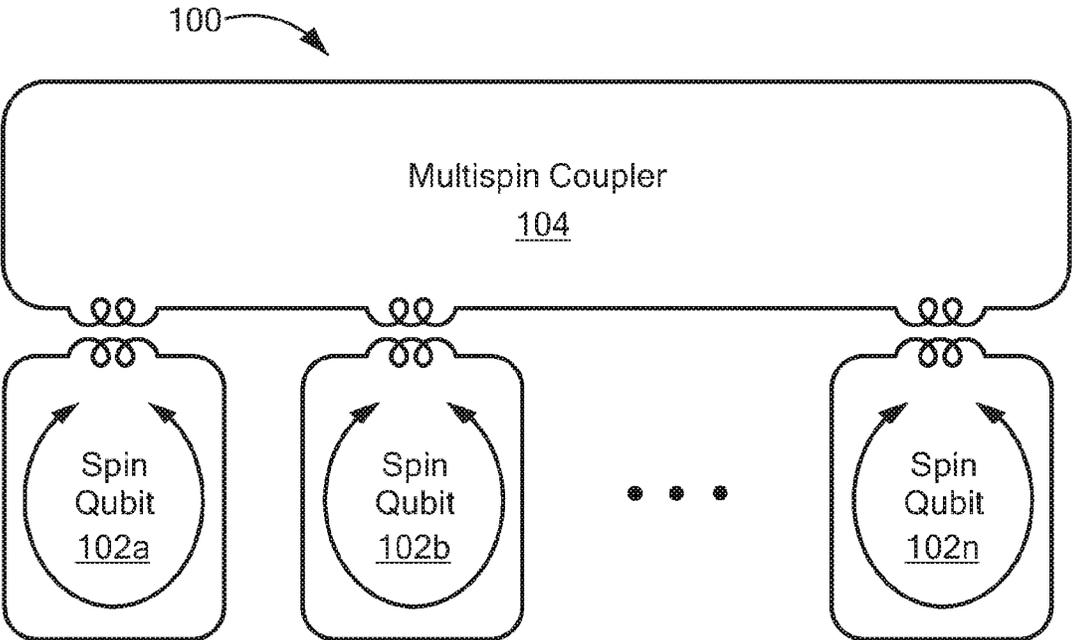


FIG. 1

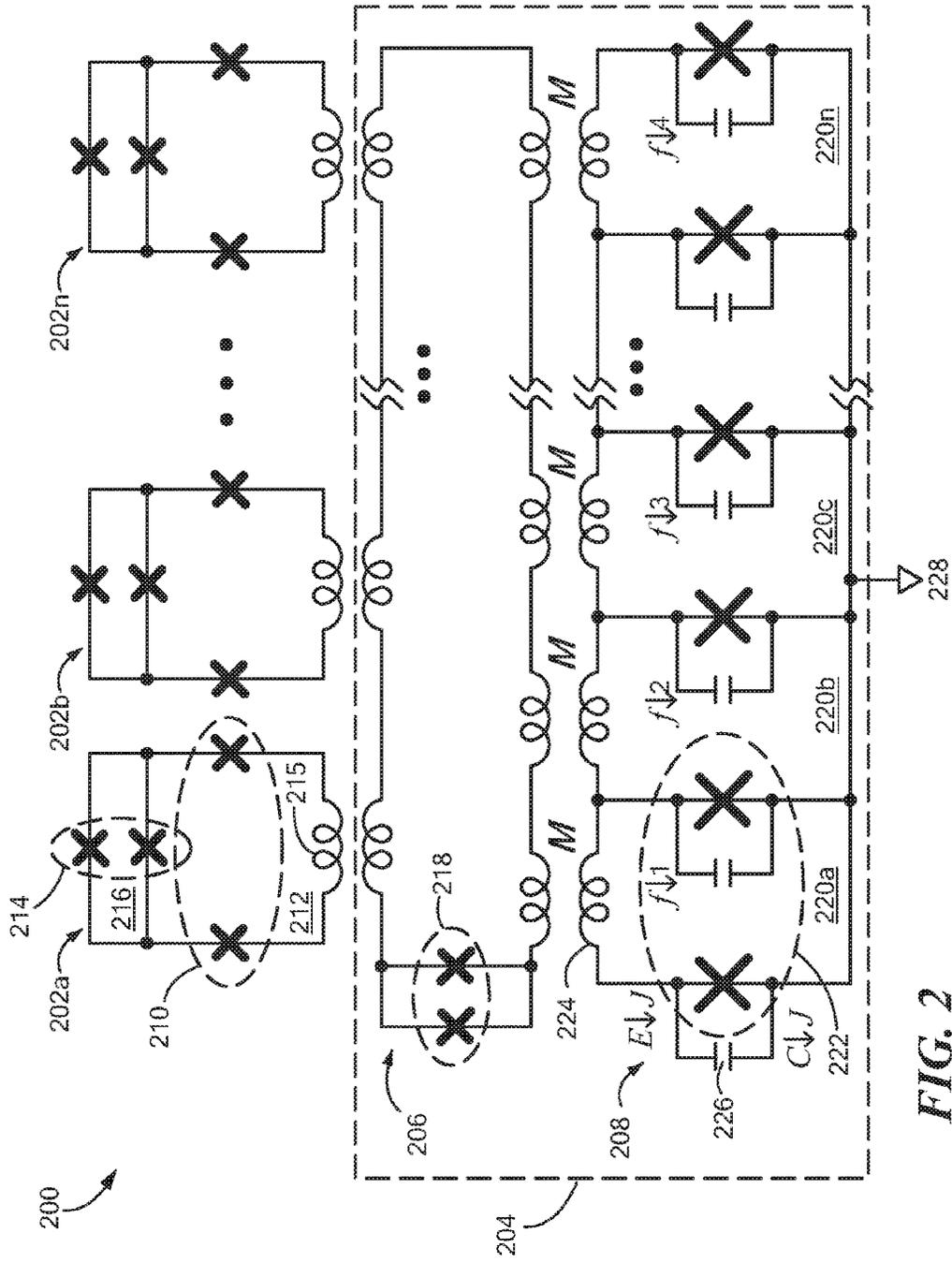


FIG. 2

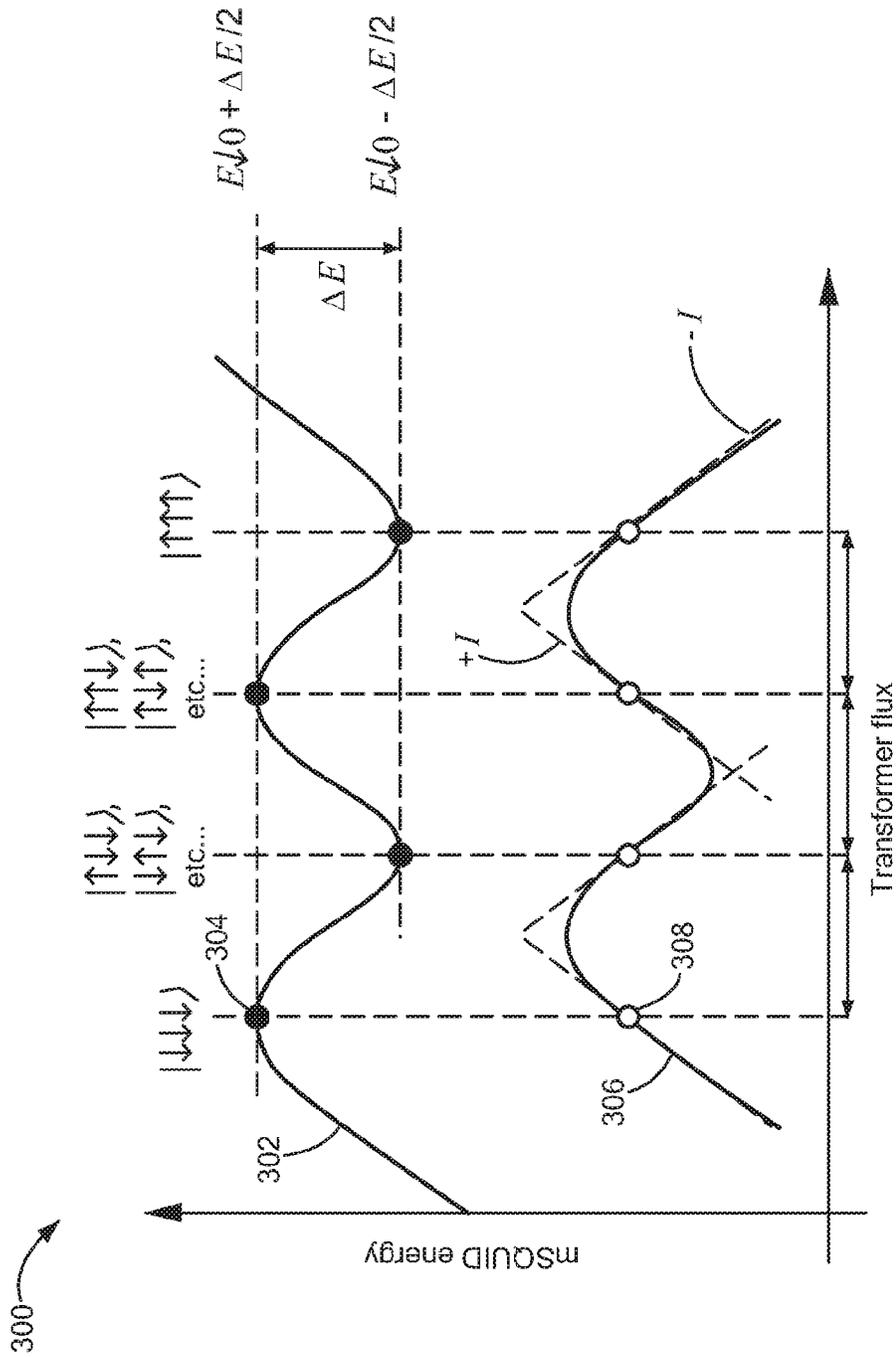


FIG. 3

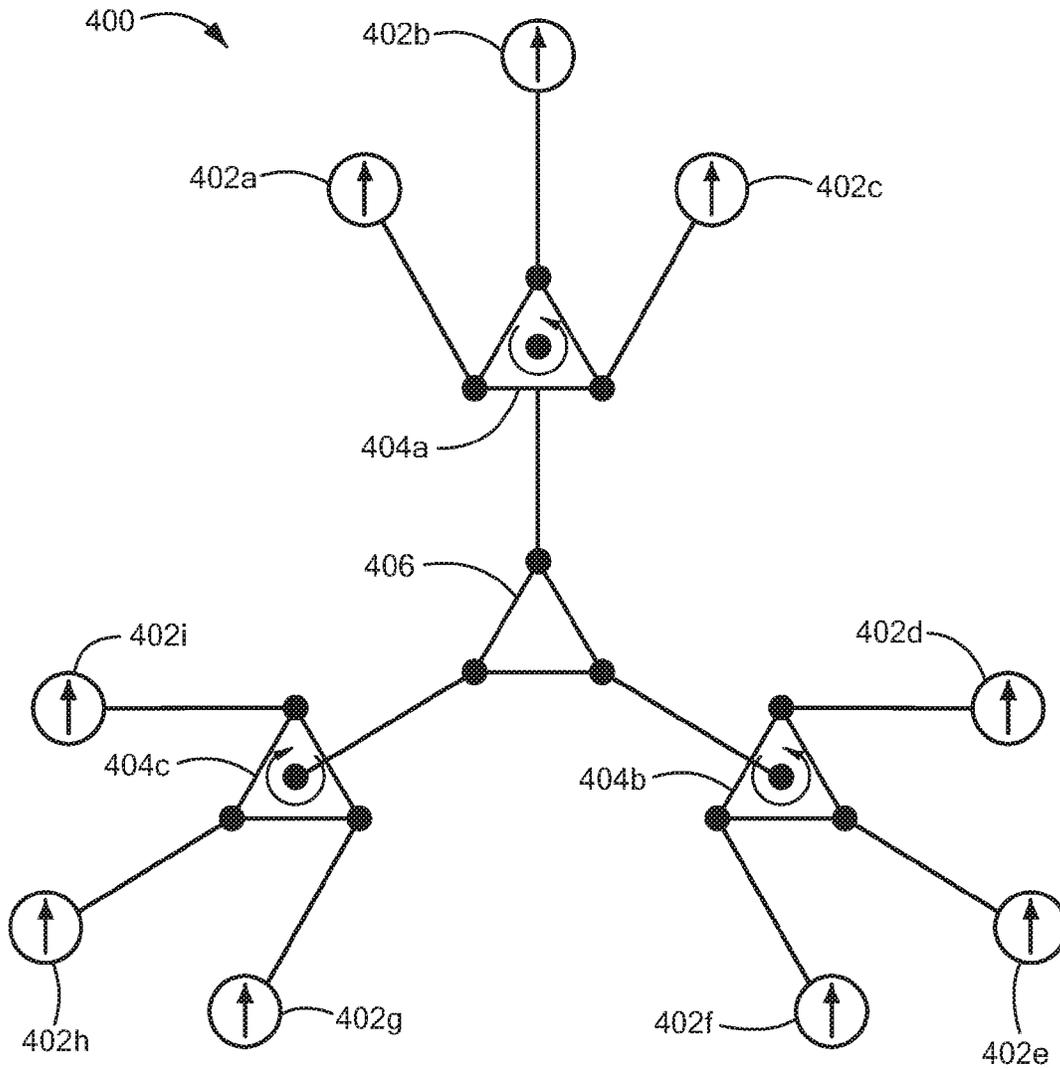


FIG. 4

MULTILOOP INTERFEROMETERS FOR QUANTUM INFORMATION PROCESSING

CROSS REFERENCE TO RELATED APPLICATION

[0001] This application claims the benefit under 35 U.S.C. §119(e) of U.S. Provisional Application No. 62/256,191 filed Nov. 17, 2015, which application is incorporated herein by reference in its entirety.

STATEMENT REGARDING FEDERALLY SPONSORED RESEARCH

[0002] This invention was made with government support under Contract No. FA8721-05-C-0002 awarded by the U.S. Air Force. The Government has certain rights in the invention.

BACKGROUND

[0003] Multiqubit quantum entanglement is a central physical resource on which the non-classical computational power of quantum information technology is based. As a result of this, known quantum information processing methods with the potential to achieve substantial performance improvement over classical techniques are built on methods for producing and exploiting large-scale quantum entanglement. The two most well-known quantum-processing paradigms are: digital quantum computing, which is expected to provide exponential performance enhancement most notably for problems in cryptography (Shor's algorithm) and quantum simulation of chemical and biological molecules (quantum phase estimation algorithm); and quantum annealing, where engineered quantum fluctuations may provide qualitative enhancement in the heuristic sampling of classical optimization problems.

[0004] In both of these quantum-processing paradigms, the machinery for construction and maintenance of large-scale quantum entanglement relies on pairwise interactions between qubits. Larger-scale entanglement is then built up by combining many of these pairwise interactions, either by applying them successively in time in a pulsed manner, or by engineering many static pairwise interactions simultaneously to obtain an effective higher-order interaction perturbatively. This is largely limited by physical hardware constraints: two-qubit interactions are the only physical-level entangling operations that have yet been demonstrated in any qubit modality.

SUMMARY

[0005] It is appreciated herein that multiqubit interactions have engineering potential for improving the performance and scalability of quantum information processing systems. For example, in the case of digital quantum computing using topological encoding for fault-tolerance, the fundamental interactions that are required involve four qubits. Realizing this with two-qubit interactions requires four individual two-qubit gates, and introduces an entirely new class of error processes relative to the idealized case. Block encoding in these schemes, which promises even higher performance, requires even higher-order interactions (e.g., involving more than four qubits). For quantum annealing, the realization of large-scale entanglement using two-spin interactions only (as in some existing commercial quantum information processing systems) is exponentially inefficient in the number

of spins involved, and this is an important reason that no evidence for quantum-enhanced performance has yet been observed in these machines.

[0006] Described herein are structures and techniques, using superconducting Josephson-junction based circuits, to directly engineer physical multiqubit (or "many-qubit") interactions in a non-perturbative manner.

[0007] According to one aspect of the disclosure, a system for multiqubit interaction includes: a multispin coupler including a plurality of loops, each loop having a pair of Josephson junctions; and a plurality of qubits each inductively coupled to the multispin coupler. In some embodiments, each loop of the multispin coupler includes an inductive element coupled between the pair of Josephson junctions and an energy storage element arranged in parallel with a first one of the pair of Josephson junctions. In certain embodiments, the multispin coupler further includes a transformer inductively coupled to each of the plurality of qubits and to each loop of the multispin coupler. In many embodiments, each of the plurality of qubits includes a first loop and a second loop, the first and second loop each including a pair of Josephson junctions, the first loop further including an inductive element coupled between the pair of Josephson junctions. In some embodiments, the plurality of qubits includes three or more qubits. In particular embodiments, the multispin coupler can be configured to operate in either an energy mode or a current mode, wherein in energy mode a total potential energy within the multispin coupler is proportional to a parity operator over each of the plurality of qubits, wherein current mode a total current circulating within the multispin coupler is proportional to the parity operator over each of the plurality of qubits. In many embodiments, the multispin coupler can be configured to operate in either an energy mode or a current mode by adjusting a magnetic flux through one or more of the loops of the multispin coupler.

[0008] According to another aspect of the disclosure, a system for multiqubit interaction includes: a first multispin coupler; a plurality of second multispin couplers each inductively coupled to the first multispin coupler, wherein the first multispin coupler and each of the plurality of second multispin couplers include a plurality of loops, each loop having a pair of Josephson junctions; and a plurality of qubits coupled to each of the second multispin couplers.

[0009] In some embodiments, each of the plurality of second multispin couplers is configured to operate in an energy mode whereby a total potential energy within each of the plurality of second multispin couplers is proportional to a parity operator over each of the plurality of qubits coupled thereto, wherein the first multispin coupler is configured to operate in a current mode whereby a total current circulating within the first multispin coupler is proportional to a parity operator over each of the plurality of qubits coupled to each of the plurality of second multispin couplers.

[0010] In various embodiments, each of the plurality of second multispin couplers is configured to operate in a current mode whereby a total current circulating within each of the plurality of second multispin couplers is proportional to a parity operator over each of the plurality of qubits coupled thereto, and wherein the first multispin coupler is configured to operate in an energy mode whereby the total potential energy within the first multispin coupler is propor-

tional to a parity operator over each of the plurality of qubits coupled to each of the plurality of second multispin couplers.

BRIEF DESCRIPTION OF THE DRAWINGS

[0011] The foregoing features may be more fully understood from the following description of the drawings in which:

[0012] FIG. 1 is a block diagram of a system to provide multiqubit interactions using a multispin coupler, according to an embodiment of the disclosure;

[0013] FIG. 2 is a diagram of a circuit to provide multiqubit interactions using a multiloop superconducting quantum interference device (mSQUID), according to another embodiment of the disclosure;

[0014] FIG. 3 is a graph illustrating different modes of mSQUID operation, according to embodiments of the disclosure; and

[0015] FIG. 4 is a diagram of an inverse paramagnetic tree structure to provide multiqubit interactions.

[0016] The drawings are not necessarily to scale, or inclusive of all elements of a system, emphasis instead generally being placed upon illustrating the concepts, structures, and techniques sought to be protected herein.

DETAILED DESCRIPTION

[0017] Referring to FIG. 1, according to an embodiment of the disclosure, a system **100** includes a plurality of qubits **102a-102n** (generally denoted **102**) and a multispin coupler **104**.

[0018] In many embodiments, the qubits **102** are provided as flux qubits. As is known, flux qubits (also known as persistent current qubits) are micrometer-sized loops of superconducting metal interrupted by a number of Josephson junctions. The Josephson junction parameters may be fabricated such that a persistent current will flow continuously when an external flux is applied. The computational basis states of the qubit are defined by the circulating currents, which can flow either clockwise or counter-clockwise.

[0019] The multispin coupler **104** provides multiqubit (i.e., two or more) interactions in a non-perturbative manner. In some embodiments, the multispin coupler **104** may be provided as a multi-loop circuit.

[0020] Referring to the embodiment of FIG. 2, a circuit **200** can provide multiqubit interactions using a multispin coupler. The circuit **200** includes a plurality of qubits **202a-202n** (**202** generally) and a multispin coupler **204** provided as a multiloop DC interferometer (referred to herein as an “mSQUID”). The mSQUID **204** includes a transformer **206** to which each of the qubits **202** may be inductively coupled.

[0021] In the embodiment of FIG. 2, the qubits **202** are provided as flux qubits each having two pairs of Josephson junctions (in FIG. 2, individual Josephson junctions are denoted “X”). For example, qubit **202a** is denoted as having a first pair of Josephson junctions **210** arranged about a first loop **212**, and a second pair of Josephson junctions **214** arranged about a second loop **216**.

[0022] Each qubit **202** further includes an inductive element **215** to provide inductive coupling with the mSQUID transformer **206**. As used herein, the term “inductive element” refers to any circuit element that stores energy in a

magnetic field, including linear and nonlinear inductors. In the embodiment of FIG. 2, the qubit inductive element is coupled between the pair of Josephson junctions **210** within the first loop **212**.

[0023] In other embodiments, the qubit inductive element **215** could be placed within the second loop **216** (e.g., between Josephson junctions **214**). In certain embodiments, a qubit may include multiple inductive elements (e.g. one in each of its two loops). Those skilled in the art will understand that each loop of a qubit has a finite self-inductance to which other loops can couple via a mutual inductance. By coupling to a loop with the larger junctions (e.g., loop **212** in FIG. 2), this is effectively coupling to an operator, while the loop with the smaller junctions (e.g., loop **216** in FIG. 2) is effectively coupling to an X operator.

[0024] It should be understood that the concepts and structures sought to be protected herein are not limited to the qubit structure shown in FIG. 2. For example, in some embodiments, any qubit which has a state-dependent magnetic moment can be used. The illustrative mSQUID **204** includes the transformer **206**, a multiloop circuit **208** inductively coupled thereto, and an output **228**. The transformer **206** may include a Josephson junction pair **218**, as shown. Including Josephson junctions in the transformer can allow flux to enter and leave the transformer loop when it is cooling (so that flux is not trapped, as would happen in a closed superconducting loop). Josephson junction pair **218** may also allow the transformer **206** to be tunable.

[0025] The multiloop circuit **208** includes a plurality of loops **220a-220n** (**220** generally), each having a Josephson junction pair **222**, an inductive element (e.g., a linear or non linear inductive element) **224** to provide inductive coupling to the transformer **206**, and an energy storage element **226** (e.g., a capacitor) arranged in parallel with one of the loop Josephson junctions. To promote clarity in the figure, the Josephson junction pair, inductive element, and energy storage element are labeled only for a first loop **220a**.

[0026] It should be understood that the number of loops **220** within the circuit **208** may be selected based on requirements for a given application. In particular, the number of loops **220** determines the number of free parameters that can be used to define the shape of mSQUID’s nonlinear energy vs. flux characteristic. Thus, increasing the number of loops **200** may provide additional control required for a given application. However, it will be appreciated that increasing the number of loops **200** may require more flux from the transformer **206** for the mSQUID to function.

[0027] It will be appreciated that the design of each mSQUID loop **220** is based on that of a conventional DC SQUID, hence the name mSQUID (or multiloop SQUID). As is known, the effective Josephson potential energy of a DC SQUID can be modulated by changing the relative gauge-invariant phase between the two Josephson junctions, adjusted via the magnetic flux through the respective loop. In the case of a multiloop SQUID **204**, an arbitrary potential energy function vs. uniform flux can be realized by adjusting the individual flux bias through the multispin coupler loops **220**. In particular, the constant phase offset between each Josephson junction can be controlled to realize arbitrary potential energy function vs. uniform flux. The result is that for flux Φ coupled to a common transformer and applied equally to all loops **220** of the mSQUID **204**, an arbitrary

potential energy function $U(\Phi)$ can be engineered by appropriately tuning the offset fluxes applied to the individual loops **222**.

[0028] In operation, each qubit **202** nominally produces a state-dependent flux $\pm\Phi_q$ through the transformer **206**. For N qubits **202** coupled to transformer **206**, the total qubit-state-dependent flux (i.e., the total state-dependent flux from all qubits, which is the input to the mSQUID) then takes one of the $N+1$ different values: $\Phi_k \in \Phi_q \{-N, -N+2 \dots 0 \dots N-2, N\}$.

[0029] It is appreciated herein the mSQUID **204** can be dynamically adjusted such that it behaves like a current source: $(\Phi)=I\Phi$, an inductor: $U(\Phi)=\Phi^2/2L$, or any more complicated nonlinear magnetic element whose behavior can be expressed as a potential energy $U(\Phi)$ (the classical parameters I , L , etc. are related to the Taylor expansion coefficients of the energy vs. flux characteristic about a chosen bias point). Furthermore, since the internal Josephson frequencies of the multispin coupler **204** can be kept relatively large (>100 GHz), this electrical behavior can be preserved over an extremely wide frequency range. As a result, the mSQUID **204** may be used in parametric nonlinear quantum devices—such as amplifiers and frequency converters—that conventionally rely on the “bare” Josephson nonlinearity, which is relatively weak by comparison.

[0030] Referring to FIG. 3, in various embodiments, an mSQUID (e.g., mSQUID **204** in FIG. 2) can be operated in two different modes: energy mode and current mode. In energy mode, the potential energy within the mSQUID’s multiloop circuit is proportional to the N -qubit parity operator $\hat{P}_N = \prod_{i=1}^N \hat{\sigma}_i^z$ such that: $\hat{U}(\Phi_k) = \Delta E \cdot \hat{P}_N$, where $\hat{\sigma}_i^z$ is the Z operator for the i th qubit. In current mode, the total current circulating within the mSQUID’s multiloop circuit is proportional to the N -qubit parity operator $\hat{P}_N = \prod_{i=1}^N \hat{\sigma}_i^z$ such that $\hat{I}(\Phi_k) = I_m \cdot \hat{P}_N$. In some embodiments, the mSQUID **204** can be configured to operate in a given mode by adjusting the magnetic flux through the mSQUID loops **220**, as discussed above.

[0031] The graph **300** in FIG. 3 illustrates these two modes of mSQUID operation. The top curve **302** illustrates energy mode, wherein the total potential energy as a function of possible qubit flux values (denoted by circles along the curve **302**, e.g., circle **304**) is effectively proportional to a multispin (in this case, three-spin) operator: $\hat{U} = \Delta E \hat{\sigma}_1^z \hat{\sigma}_2^z \hat{\sigma}_3^z$. In energy mode, the potential energy vs. input flux can be tailored such that at the flux points accessible via the qubits’ input to the transformer, the mSQUID energy takes on one of two values, according to the total parity of the qubit state. This results in an effective interaction between the qubits.

[0032] The bottom curve **306** illustrates the current mode of operation, in which the potential energy is the same at all of the possible qubit flux values (denoted by circles along the curve **306**, e.g., circle **308**), but the mSQUID circulating current (proportional to the slope of the energy vs. flux) is proportional to a multiqubit operator: $\hat{I} = I_m \hat{\sigma}_1^z \hat{\sigma}_2^z \hat{\sigma}_3^z$. In current mode, the potential energy is kept constant and independent of the qubits’ input state, while the effective mSQUID circulating current (which is given by the derivative of the energy with respect to the flux) assumes only two values, and is proportional to the total qubit state parity.

[0033] It should be understood that although FIG. 3 illustrates mSQUID operation for the case of three (3) qubits, the concepts, structures, and techniques sought to be protected

herein be used to effect interactions between arbitrary numbers of qubits (e.g., between N qubits, where $N>1$).

[0034] FIG. 4 illustrates how the different modes of mSQUID operation can be combined using a so-called “inverse paramagnetic tree” structure to provide higher-order multiqubit interactions. An inverse paramagnetic tree structure **400** may include a root mSQUID **406**, a plurality of intermediate mSQUIDs (e.g., intermediate mSQUIDs **404a**) coupled thereto, and a plurality of qubits (e.g., qubit **402a**) coupled to each of the intermediate mSQUIDs. In the embodiment of FIG. 4, the structure **400** includes three (3) intermediate mSQUIDs **404a-404c**, each having a group of three (3) qubits (or “spins”) **402** coupled thereto. In particular, qubits **402a-402c** are coupled to a first intermediate mSQUID **404a**, qubits **402d-402f** are coupled to a second intermediate mSQUID **404b**, and qubits **402g-402i** are coupled to a third intermediate mSQUID **404c**.

[0035] The root mSQUID **406** may be operated in a different mode than the intermediate mSQUIDs **404**. For example, each group of M (e.g., $M=3$) qubits **402** may be coupled to a respective intermediate mSQUID **404** operating in current mode, such that the total circulating current in each intermediate mSQUID **404** is proportion to a M -qubit operator product, with $M=3$ in FIG. 4. In turn, each intermediate mSQUID **404** may be coupled to a root mSQUID **406** operating in energy mode, such that the total energy in the root mSQUID **406** is proportional to an N -qubit operator product, with $N=9$ in FIG. 4. Thus, it will be appreciated that the parities of multiple groups of M qubits **402** can be combined, resulting in an effective interaction between all N qubits.

[0036] It should be understood that the tree structure **400** shown in FIG. 4 is merely one example and that an inverse paramagnetic tree structure **400** could include additional levels (i.e., more than one level of intermediate mSQUIDs **404**) and could have more than three (3) connections at each level of the tree. Moreover, the number of connections at each level may vary in some embodiments. For example, the root mSQUID could be coupled to a certain number of intermediate mSQUIDs, each of which could be coupled to a different number of qubits. Further, the structure **400** can be used to realize either X or Z operators by connecting to either the Z or X loops of the qubits **402**.

[0037] It is appreciated that the concepts, structures, and techniques described herein may be used to provide high-order qubit interactions and, as such, could have transformational importance in both quantum annealing and in digital quantum information processing.

[0038] All references cited herein are hereby incorporated herein by reference in their entirety.

[0039] Having described certain embodiments, which serve to illustrate various concepts, structures, and techniques sought to be protected herein, it will be apparent to those of ordinary skill in the art that other embodiments incorporating these concepts, structures, and techniques may be used. Elements of different embodiments described hereinabove may be combined to form other embodiments not specifically set forth above and, further, elements described in the context of a single embodiment may be provided separately or in any suitable sub-combination. Accordingly, it is submitted that the scope of protection sought herein should not be limited to the described embodiments but rather should be limited only by the spirit and scope of the following claims.

What is claimed is:

1. A system for multiqubit interaction comprising:
 - a multispin coupler including a plurality of loops, each loop having a pair of Josephson junctions; and
 - a plurality of qubits each inductively coupled to the multispin coupler.
2. The system of claim 1 wherein each loop of the multispin coupler includes an inductive element coupled between the pair of Josephson junctions and an energy storage element arranged in parallel with a first one of the pair of Josephson junctions.
3. The system of claim 1 wherein the multispin coupler further includes a transformer inductively coupled to each of the plurality of qubits and to each loop of the multispin coupler.
4. The system of claim 1 wherein each of the plurality of qubits includes a first loop and a second loop, the first and second loop each including a pair of Josephson junctions, the first loop further including an inductive element coupled between the pair of Josephson junctions.
5. The system of claim 1 wherein the plurality of qubits includes three or more qubits.
6. The system of claim 1 wherein the multispin coupler can be configured to operate in either an energy mode or a current mode, wherein in energy mode a total potential energy within the multispin coupler is proportional to a parity operator over each of the plurality of qubits, wherein current mode a total current circulating within the multispin coupler is proportional to the parity operator over each of the plurality of qubits.
7. The system of claim 6 wherein the multispin coupler can be configured to operate in either an energy mode or a current mode by adjusting a magnetic flux through one or more of the loops of the multispin coupler.

8. A system for multiqubit interaction comprising:
 - a first multispin coupler;
 - a plurality of second multispin couplers each inductively coupled to the first multispin coupler, wherein the first multispin coupler and each of the plurality of second multispin couplers include a plurality of loops, each loop having a pair of Josephson junctions; and
 - a plurality of qubits coupled to each of the second multispin couplers.
9. The system of claim 8
 - wherein each of the plurality of second multispin couplers is configured to operate in an energy mode whereby a total potential energy within each of the plurality of second multispin couplers is proportional to a parity operator over each of the plurality of qubits coupled thereto; and
 - wherein the first multispin coupler is configured to operate in a current mode whereby a total current circulating within the first multispin coupler is proportional to a parity operator over each of the plurality of qubits coupled to each of the plurality of second multispin couplers.
10. The system of claim 8
 - wherein each of the plurality of second multispin couplers is configured to operate in a current mode whereby a total current circulating within each of the plurality of second multispin couplers is proportional to a parity operator over each of the plurality of qubits coupled thereto; and
 - wherein the first multispin coupler is configured to operate in an energy mode whereby the total potential energy within the first multispin coupler is proportional to a parity operator over each of the plurality of qubits coupled to each of the plurality of second multispin couplers.

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