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#### (54) Title: METER FOR **MEASURING AN** ELECTRICAL PARAMETER



**(57)** Abstract: In a meter for performing a measurement of an electrical para meter, an output **(6)** from a sensor **(5)** is sampled to produce at least one sam ple, and an iterative method is performed comprising: producing further sam-<sup>20</sup>ples; holding in memory a stored array **(15)** of samples comprising the at least Output indicating one sample and each of the further samples from each iteration; determining <sup>a</sup>state of the measurement a measure of statistical variability of a mean **(18)** for the respective iteration from a measure of statistical variability and from the number of samples used <sub>19</sub> to generate the measure of statistical variability; comparing the measure of <sup>19</sup><sup>19</sup> statistical variability of the mean with a pre-determined threshold (17); and **<sup>i</sup>**generating an electrical signal indicating a state of the measurement (20) if the Pre-determined threshold Measure of statistical measure of statistical variability of the mean of the samples taken during the measurement is less than or equal to the pre-determined threshold.



### Meter for Measuring an Electrical Parameter

#### Technical Field

The present invention relates generally to improved test apparatus for **5** measuring one or more electrical parameters, and more specifically, but not exclusively, to a hand-held digital meter capable of measuring resistance in an electrically noisy circuit.

#### **Background**

**10** Conventional meters for measuring an electrical parameter such as resistance may be used in an electrically noisy environment. Typically, an extended measurement period may be used to produce an averaged value of the electrical parameter, to reduce the effects of electrical noise. Typically, an operator may perform several measurements in order to gain confidence that a **15** measurement is reliable. However, this may be time-consuming and onerous on the user and the result may be uncertain.

### **Summary**

In accordance with a first aspect of the present invention, there is provided 20 a method of operation of a meter for performing a measurement of an electrical parameter, the method comprising, in the meter:

sampling an output from a sensor of the electrical parameter to produce at least one sample; and

iteratively performing steps of:

**25** sampling the output from the sensor to produce one or more further samples;

> holding in memory a stored array of samples comprising the at least one sample and each of the one or more further samples from each iteration;

**30** determining a measure of statistical variability from the stored array of samples for the respective iteration;

determining a measure of statistical variability of a mean for the respective iteration from the measure of statistical variability and from the number of samples used to generate the measure of statistical variability;

comparing the measure of statistical variability of the mean with a **5** pre-determined threshold; and

> generating an electrical signal indicating a state of the measurement if the measure of statistical variability of the mean of the samples taken during the measurement is less than or equal to the pre determined threshold.

**10** This allows a measurement to be made reliably and efficiently.

In an embodiment of the invention, the electrical signal indicating a state of the measurement indicates that the measurement has reached or exceeded a target confidence level.

In an embodiment of the invention, the electrical signal indicating a state **15** of the measurement indicates that the measurement is complete.

In an embodiment of the invention, measure of statistical variation is a standard deviation.

In an embodiment of the invention, the measure of statistical variation is a variance.

20 In an embodiment of the invention, the measure of statistical variability of the mean is a standard deviation divided **by** the square root of the number of samples used to generate the measure of statistical variability.

In an embodiment of the invention, determining the measure of statistical variability from the stored array of samples comprises, at each iteration:

**25** forming a second array of samples to be held for the iteration in addition to the stored array of samples **by** filtering the array of samples, and

> calculating the measure of statistical variability of the second array of samples.

This allows efficient operation in the presence of noise.

**30** In an embodiment of the invention, filtering the stored array of samples comprises applying a median filter.

This allows outlying samples to be discarded, reducing the effects of intermittent noise on measurement time.

In an embodiment of the invention, applying the median filter comprises:

arranging the samples in the stored array of samples in order of **5** magnitude;

forming the second array of samples from the stored array of samples **by**  discarding at least a sample with greatest magnitude.

This allows reliable operation in the presence of noise.

In an embodiment of the invention, forming the second array of samples **10** from the stored array of samples comprises discarding a sample with greatest magnitude and a sample with least magnitude.

This allows reliable operation in the presence of noise.

In an embodiment of the invention the method comprises:

calculating an average measurement of the electrical parameter at each

**15** iteration from the second array of samples; and

generating an output indicating the average measurement.

This allows a user-friendly interface to be provided.

In an embodiment of the invention, the method comprises:

generating an output indicating confidence of the measurement at each

20 iteration from the measure of statistical variability of the mean and a target measure of statistical variability of the mean.

This allows a user-friendly interface to be provided.

In an embodiment of the invention, the output indicating confidence of the measurement represents a percentage of a target confidence level.

**25** This provides a convenient indication of confidence level.

In an embodiment of the invention, the method comprises:

determining a time-to-finish estimate for the measurement from the measure of statistical variability; and

generating an output indicating the determined time-to-finish estimate.

**30** This provides an efficient user interface for the meter, allowing an efficient measurement to be performed.

In an embodiment of the invention, generating the output indicating the determined updated time-to-finish estimate comprises:

calculating an average of said determined time-to-finish estimate and at least some of previously determined time-to-finish estimates

**<sup>5</sup>**This allows a reliable estimate of confidence level to be provided.

In an embodiment of the invention, each said output is a digital control to a display.

In an embodiment of the invention, the method comprises stopping the measurement in response to the electrical signal indicating a state of the **10** measurement.

This allows efficient automatic operation of the meter.

According to a second aspect of the invention there is provided a meter for performing a measurement an electrical parameter, comprising:

a sensor configured to measure the electrical parameter;

**15** a processor configured to perform the method of the invention.

Further features and advantages of the invention will be apparent from the following description of exemplary embodiments of the invention, which are given **by** way of example only.

#### 20 Brief Description of the Drawings

Figure 1 is a schematic diagram illustrating test apparatus according to an embodiment of the invention, connected to an electrical component;

Figure 2 is a schematic diagram illustrating test apparatus according to an embodiment of the invention, illustrating generating an output indicating a state **25** of the measurement;

Figure **3** is a schematic diagram illustrating test apparatus according to an embodiment of the invention, illustrating generation of a time-to-finish estimate;

Figure 4 is a schematic diagram illustrating test apparatus according to an embodiment of the invention, illustrating generation of a second array of samples **30 by** filtering the stored array of samples;

Figure **5** is a schematic diagram illustrating test apparatus according to an embodiment of the invention, illustrating implementation of a median filter;

Figures 6a, **6b** and 6c illustrate examples of displays of the output;

Figure **7** is a flow diagram of operation of test apparatus according to an **<sup>5</sup>**embodiment of the invention;

Figure **8** is a flow diagram of operation of test apparatus according to an embodiment of the invention generating a time-to-finish estimate;

Figures 9a to 9e are graphs illustrating operation of the test apparatus in an electrically noisy environment;

**10** Figures 10a to **10d** are graphs illustrating operation of the test apparatus in the presence of impulsive noise;

Figures 1la and **1lb** show effect of smoothing of time-to-finish estimation;

Figure 12 is a flow diagram showing operation of the test apparatus in an **15** embodiment of the invention; and

Figure **13** is a flow diagram showing operation in an alternative arrangement.

#### Detailed Description

20 **By** way of example, embodiments of the invention will now be described in the context of a hand-held digital meter capable of measuring resistance of an electrical component or circuit, but it will be understood that embodiments of the invention may relate to other electrical test equipment and that embodiments of the invention are not restricted to use in a hand-held digital meter or to **25** measurement of resistance.

Figure 1 shows test apparatus 1 according to an embodiment of the invention, in this example a hand-held digital meter, connected to an electrical device 2, for testing of the resistance of the electrical device 2. The meter has a first terminal **3** and a second terminal 4 for connection to the electrical device **30** under test. The meter also has a sensor **5,** operating as a measurement circuit, connected to the first **3** and second 4 terminals. The measurement circuit may not

necessarily be directly connected to the first and second terminals, but may be connected via other components, for example an input protection circuit, which may comprise, for example, a series arrangement of one or more positive temperature coefficient resistors and/or high current resistors and/or fuses. The

- **5** measurement circuit typically has a high input impedance so as not to disturb the circuit under test when it is connected. The measurement circuit, when measuring resistance, may operate as a high input impedance voltmeter connected across the first and second terminals, with a current source arranged to drive a known current through the electrical component under test. The sensor may be controlled **by** a **10** control circuit or controller **9.** The control circuit may comprise, for example, a microcontroller having program memory containing program code, or the controller may be part of another processor or may be implemented **by** digital logic or **by** a programmable gate array. The functions of the control circuit and a processor **13** for performing signal processing may be combined as one or more
- **15** controller or processor circuits, and may be performed **by** software or firmware configured to run on a programmable device.

As shown in Figure **1,** on output of the sensor is sampled **by** a sampler **7**  to produce samples. **A** signal processor circuit or signal processing operation of a processor **13** determines a measure of statistical variability **10** of the samples, 20 and a further signal processor circuit or signal processing operation determines a a measure of the statistical variability of the mean from the measure of statistical variability and from the number of samples used to generate the measure of statistical variability. The measure of statistical variability of the mean is compared with a pre-determined threshold, and, if the measure of statistical **25** variability of the mean is less than or equal to the pre-determined threshold, an electrical signal is generated indicating a state of the measurement, such as an indication that the measurement complete. The electrical signal may be an analogue or digital signal causing a display 14, for example a liquid crystal display of the meter, to display an indication of the status of the measurement, for example **30** an indication that the measurement is complete, and/or an indication that the measurement has reached or exceeded a pre-determined confidence level. This

allows an improved user interface for a meter, allowing a more efficient measurement operation to be performed.

The measure of statistical variability may be, for example, a standard deviation, and the measure of statistical variability of the mean may be the **<sup>5</sup>**standard deviation divided **by** the square root of the number of samples used to generate the measure of statistical variability. In an alternative embodiment, the measure of statistical variability may be a variance.

The state of the measurement indicated **by** the electrical signal may be completion of the measurement, and may be readiness of the measurement, for **10** example within a pre-determined tolerance.

As shown in figure 2, the following steps may be iteratively performed: sampling the output from the sensor to produce one or more further samples, holding in memory a stored array of samples **15** comprising the previous samples **16** and each of the one or more further samples from each iteration, determining

- **<sup>15</sup>**a measure of statistical variability of the mean from the stored array of samples, and comparing a measure of statistical variability of a mean **18** determined from the stored array of samples in a comparison circuit or programme step **19** with a pre-determined threshold **17.** The comparison may generate an output 20 in the form of an electrical signal indicating a state of the measurement, which may be 20 an indication that the measurement is complete, if the measure of statistical
- variability of the mean of the samples taken during the measurement is less than or equal to the pre-determined threshold. The output may cause the display to show an indication that the measurement is complete, and the measurement process may be stopped.

**25** Figure **3** shows determining a time-to-finish estimate for the measurement from the measure of statistical variability and generating an output to indicate the determined updated time-to-finish estimate. This allows a continually updated estimate of time-to-finish to be provided. The time to finish estimate may be derived from the estimated number of samples to finish, which may be derived **30** from the measure of statistical variability and a target confidence level. As described in more detail in connection with Figure **8,** the estimated number of

samples to finish may be given **by** the square of the result of the division of the measure of statistical variability, in the form of standard deviation, **by** a target confidence level.

As shown in Figure 4, an updated measure of statistical variability may be **<sup>5</sup>**generated from the stored array of samples **by,** at each iteration, forming a second array of samples 22 to be held for the iteration in addition to the stored array of samples **by** filtering the array of samples in a filter 21, and calculating **23** a standard deviation of the second array of samples, allowing reliable operation of the meter in the presence of noise in the circuit being measured in the device under **10** test.

As shown in Figure **5,** in an embodiment of the invention, filtering the stored array of samples may comprise applying a median filter, allowing a reliable time to finish estimate to be generated. Applying the median filter comprises arranging the samples in the stored array of samples in order of magnitude 24, **15** forming the second array of samples from the stored array of samples **by**  discarding at least a sample with greatest magnitude, and typically also at least a sample with the least magnitude **25.** 

In addition, a display may be generated showing the running average of the measurements of the electrical parameter, for example resistance. This may 20 be useful to a user of the meter. To do this, an average measurement of the electrical parameter may be calculated at each iteration from the second array of samples, and the output indicating the average measurement may be generated from this. Alternatively or in addition, an output indicating confidence of the measurement may be generated at each iteration from the updated measure of **25** statistical variability and a target measure of statistical variability. The output indicating confidence of the measurement may represent a percentage of a target confidence level, providing a user-friendly interface providing a convenient indication of confidence level.

Updating the output to indicate the determined updated time-to-finish **30** estimate may comprise filtering, for example, calculating an average of the updated time-to-finish estimate and at least some of previously determined time-

to-finish estimates. The filtering of the previously determined time to finish estimates may be **by** a digital filter, such as a median filter. The output is typically a digital control to a display.

In addition to applying to measurements of resistance, embodiments of the **<sup>5</sup>**invention can apply to other systems performing measurements of a given quantity.

In prior art systems, in order to increase accuracy of a measurement, the data is usually acquired many times and an average value is reported as a final value. However, despite filtering in hardware using, for example, analogue **10** electronic filters and/or software, using for example averaging and/or digital filters, the output value can still fluctuate, due to the amount of noise present in the input data. For many devices such as multimeters or other specialised testers the measurement time may be pre-set, for example to **0.5** sec per screen update and each new value overwrites the previous value, so that historical data is not **15** displayed. In the case of a large amount of noise, insufficient information may be

gathered to make an accurate measurement. As a consequence the displayed result can vary wildly, which can be confusing to the operator, and may call into doubt the validity of the results.

**A** typical prior art approach used in practice is for an operator to take 20 several readings and to find average of them, for example with a calculator or spreadsheet, or for example just recording the highest and the lowest reading and take average of the two. Either method requires writing down results, performing mental arithmetic, or using devices to perform the averaging. This is difficult to do in practice, as both hands can be required to hold the instrument so writing **25** down requires a second person, time consuming and prone to mistakes. When the averaging is carried out manually it is typically unknown how many measurements should be taken to provide a reliable average, so that enough points are recorded.

Embodiments of the invention perform averaging automatically, with the **30** number of measurements adjusted adaptively on-the-fly. The ongoing measured value is processed **by** statistical methods, so that the confidence in the

measurement stability can be estimated. The measurement time may be extended for as long as required in order to measure the quantity with a specified confidence level. Additionally, for a given level of noise, and for a noise level which changes with time, the processing circuit can predict how many iterations it will take for

- **5** the measurement to complete, so that the time-to-finish value can be predicted. This gives assurance to the operator because not only the final value will be given with high confidence, but it will also give information about the time it is required to achieve good confidence, for example 1 second or **10** minutes.
- In embodiments of the invention, the averaging operation is carried out **10** automatically, for potentially large number of measurements within the capabilities of on-board computer memory and processing power. The live averaged value may be displayed, and/or a live estimation of the confidence level. The final measured value may be displayed after the calculated confidence indicates that the measurement is within a technical specification of the
- **15** instrument. The confidence level can be displayed in terms of a percentage value of the technical specification of the instrument. An indication that the measurement is complete may be displayed, for example, **by** displaying **"100%"**  as a confidence level, or any other indication that the measurement is complete. In addition, live estimation or prediction of time-to-finish may be displayed. The
- 20 measurement may be aborted **by** the operator if the predicted time-to-finish is too long, but the current average value and the estimated confidence may be given, even if they are outside of the specification level.

Embodiments of the invention may use a target value for the required level of confidence to estimate the required number of data points. Since the **25** measurement time for each data point is typically known, which may be a fixed value in a given instrument, for example **0.5** sec, the time required to reach the required level of confidence may be estimated. The final value and/or the running average may be displayed with the estimated level of confidence.

**If** the target value of the confidence is reached then the measurement can **30** be terminated automatically and the final value frozen on screen, indicating that the measurement is complete or at least ready to a predetermined tolerance. **If**

not, the time-to-finish may be estimated and the next iteration is initiated and added to the population for statistical re-analysis. The cycle may repeat until the target value of confidence is reached, or the user aborts the test because the waiting time is unacceptably long due to the noise content. With each iteration

**<sup>5</sup>**more data is gathered and the quality of the average value improves approximately **by** the reciprocal of square root of **N,** where **N** is the number of points. Therefore, with a sufficient number of acquired values the target value will be reached, because **N** increases with each iteration, so the reciprocal of square root **N**  typically decreases exponentially.

**10** Figure 6a, **6b** and 6c illustrate examples of displays of the output generated in embodiments of the invention at three stages of operation. Two typical examples are shown: a rectangular display with a digital scale showing confidence level, as a measure of dispersion, and/or time to finish, and a circular display with an arc showing confidence level. Colour coding may be used to indicate progress. **15 Of** course may other types of display may be implemented.

Figure 6a shows an illustrative example of a first stage, at the start of a noisy measurement. **A** low confidence level 26a, 27a is shown **(5%),** a long predicted time **(27** minutes) and the displayed average value of the measured electrical parameter is truncated, because the dispersion is greater than **+/- 0.5.** 

20 Figure **6b** shows a mid point of a long measurement, with **50%** confidence level **26b, 27b,** 2 minutes waiting time, and the displayed value showing one digit after the decimal point.

Figure **6b** shows a finished measurement with **100%** confidence level 26c, 27c and full resolution of the displayed value, indicating that the measurement is **25** complete.

The display may indicate the state of the measurement, for example that the measurement is complete, **by,** for example, a change of colour, display of a message, or **by** other suitable means. An audio signal may be generated on the basis of the electrical signal to indicate the state of the measurement, such as to **30** indicate that the measurement is ready and/or complete.

the average value.

12

The measurement time may be adjusted on-the-fly in an adaptive way. **If**  the measurement starts with lower noise, and then larger noise appears, or even a single glitch, then the confidence level is automatically reduced on the basis of statistical analysis, which automatically increases the time required to complete

**<sup>5</sup>**the measurement. **If** initially the noise is high and reduces during measurement, then the confidence level will be improved much more quickly, thus reaching the target value in a shorter time. This happens automatically, without any user intervention.

Figure **7** is a flow diagram of operation of test apparatus according to an **10** embodiment of the invention in steps **S7.1** to **S7.12.** Three main values can be produced: the current average value, which may be a running or moving average, estimated iteratively at **S7.5,** a value corresponding to the current uncertainty of the measurement, estimated at **S7.7,** and a target value corresponding to technical specification of the measurement of the instrument. The actual values used for **15** calculating the target specification can be different from those specified for the instrument. For example, a safety margin could be provided, for example 2x, so that the produced average result is sufficiently stable, so that other measurement errors due to offsets, temperature, etc., would not take the value outside of the full specification. As shown in Figure 7, the quantity sdomreal is calculated at step 20 **S7.7,** which is the standard deviation of the mean, which indicates the quality of

As shown in the embodiment of Figure **7,** a target confidence level sdomideal is specified or estimated. This can be achieved **by** giving a fixed value, or a value related to the measured number, for example not greater then **+/- 5%** of **25** the measured value. The target value is the threshold which dictates when the algorithm will stop. **A** running average xaverage is estimated at step **S7.5,** and this value may be indicated **by** the display to the operator. The last value of the measurement may be indicated to the user, or stored in the memory. The standard deviation of the population, sreal, is estimated at step **S7.6,** which allows **30** measuring the quality of the average value, also referred to as a measure of the statistical variation of the mean or sdom real. The comparison between the target confidence value and the real confidence value may determine when the algorithm will stop. The number of iterations to finish or the time-to-finish may be estimated, as shown in Figure **8.** This provides a helpful indication to the operator.

The following equations may be used for the features of Figures **7** and **8:** 

**5 (1)** xaverage (also called mean) value of the **N** population of xi

$$
\overline{x} = \frac{1}{N} \sum_{i=1}^{N} x_i
$$

(2) variance  $(s^2)$  is dispersion of population around its mean

$$
s^{2} = \frac{1}{N-1} \sum_{i=1}^{N} (\overline{x} - x_{i})^{2}
$$

**(3)** s real, standard deviation (s, sd, stdev), is a square root of variance

10 
$$
s = \sqrt{s^2} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (x - x_i)^2}
$$

(4) standard deviation of the mean (sdomreal) gives information about likelihood that the mean value is close to the "true" value represented **by** the population of all measurements

Both variance and standard deviation measure dispersion of the population **15** around the mean value. The value of sdomreal in Figure **7** may be equal to sdom given **by** the following equation.

$$
sdom = \frac{s}{\sqrt{N}}
$$

It can be seen that equations (2) and **(3)** are directly related to each other and all calculations can be carried out either in terms of standard deviation or 20 variance. Standard deviation is typically used, because it is easier to understand, because the results can be expressed in the same units as the measured results. For example if measurement is in  $\Omega$  then also the dispersion measured by standard deviation can be expressed in  $\Omega$ . However, it can be also expressed in relative units, for example **%.** 

**25** Figure **8** is a flow diagram showing an embodiment of the invention in which an output indicating time to finish is generated. As shown in Figure **8,** this may be in addition to the features of Figure **7.**

As shown in Figure **8,** number of total points to finish may be given **by** 

$$
N_x = \left(\frac{s_{\text{real}}}{sdom_{\text{ideal}}}\right)^2
$$

Estimated total time to finish is number of point to finish scaled **by** the time of one point

$$
5 \qquad \qquad time\_tot = const \cdot N_x
$$

Time-to-finish is calculated **by** subtracting the elapsed time from the total time

 $time$   $to$   $finish = time$   $tot - time$   $elapsed$ 

The equation for standard deviation could be replaced **by** one with **10** unbiased statistical variance.

Figures 9a to 9e show an example of the performance of the system shown in Figure **7** and Figure **8** with a real measurement with fairly constant noise. Figure 9a shows noisy readings **28** and their running average **29.** Figure **9b** shows exponentially decaying values of *sdomreal* **30.** Figure 9c shows estimated total

**15** time **31** for the whole measurement. Figure **9d** shows estimated time-to-finish **32**  as the measurement progresses. Figure 9e is an interpretation of the curve shown in Figure **9d.** The dashed rectangle 34 shows an initial interval in which not enough points are gathered to give reliable information about dispersion of values. After about 20 readings the statistics is robust enough and the predicted time-to 20 finish **33** begins to linearly decrease to zero, at which point the measurement stops

because the target value was reached.

Figures 10a to **10d** show an example of adaptive performance. **A** fairly long measurement is shown in order to better illustrate the concept. The noise level is fairly constant, but at some point there is a large glitch which disturbs the **25** value of the running average.

Figure 10a shows raw input data **36,** Figure **l0b** shows standard deviation ofmean(sdom real) **37** detects that the mean was disturbed with the glitch shown in Figure 10a. Figure 10c shows the estimated total time **38** is extended accordingly and Figure **10d** shows the time-to-finish/points-to-finish **39** are

adjusted automatically. Because all the data is used then this glitch is also included in the statistical evaluation and it is automatically taken into account in the estimation of confidence and time-to-finish. However, it can be clearly seen from Figure **1Od** that if the glitch had not happened then the measurement would **<sup>5</sup>**automatically terminate at much shorter time (probably around 120 readings,

instead of **225).** 

Nevertheless, regardless the number of actual readings taken in the whole measurement the final value of the measurement has similar level of confidence within the technical specification.

**10** The confidence of measurement can be also estimated not in terms of dispersion but as a percentage value, with the value of **100%** meaning that the target value was reached. For example, assuming that the target value (target **= C.CC)** should be 0.12 (which is **100%** confidence). One method of converting **C.CC** into **%** value could be as follows, **by** way of example:

**15** 

**1.** assume or calculate target value, e.g. Cideal **= 0.12** 

2. calculate real confidence level Creal from statistical data, e.g. **0.39** 

**3.** re-map the real value to **0-100%** scale Cpercent **= 100 \*** Cideal/  $C$ real =  $31\%$ 

20 Other ways of re-mapping to **0-100%** scale are possible.

The algorithm does not have to be used for a single-value measurement. The same can be applied to measuring waveforms, or other signals. The waveform data can be compared to the average value and the dispersion from the average can be measured in a similar way as it is done for standard deviation of a single **25** value variable. Thus, some pre-processing may be done before the data is fed into the algorithm, but the key nodes of the algorithm would still be used. The algorithm may be used if a trend of changing underlying values of the parameter to be measured is known. For example, for linearly changing values they could be pre-processed **by** linear regression so that the confidence indicator could work **30** on the coefficients of slope and intercept of a given curve.

**If** the problem is approached as statistical noise suppression then the displayed value will change from **100%** (infinitely high noise) to **0%** (no noise) then the equation would be:

Noisepercent **= 100 - 100 \*** Cideal **/** Creal **= 100 \*** (1 **-** Cideal **/** Creal)

**5** As can be seen from Figures 10a and 10c, a single large glitch in a fairly large population of other data points is capable of doubling the time-to-finish value, which may be undesirable from the user viewpoint. **If** such a glitch, or a few such glitches are excluded from the whole population of data then the remaining noise in the data is significantly smaller and the time-to-finish is **10** significantly shorter. This is because a value of standard deviation (s real) is affected **by** the noise and the glitch. **If** the glitch is excluded then the value of s real is significantly reduced and the algorithm converges more quickly In an embodiment of the invention, a median filter may be utilized as shown in Figure **5.** 

**15** Typically, in a median filter, the old data is discarded and only the new data is retained for further processing. **By** contrast, in embodiments of the invention, the old data is retained, and the truncated mean filtering is re-applied to the full set of data on each step, because the input array will continue to grow with each iteration.

20 Figures 11a and **1lb** show the effect of smoothing of the time-to-finish estimation. The estimated time-to-finish value 43 can fluctuate sharply due to noise in the input data. The elapsed time is shown as straight line 42. Fluctuation may be frustrating for the operator relying on the time-to-finish value. In order to reduce such fluctuations a running average can be employed to reduce **25** variations, as shown in curve 44.

This would require storing the previous values of time-to-finish at each iteration, and calculating an average of such whole set, or an average of its subset, e.g. the last **50%** items in it, before the time-to-finish value is displayed.

Figure 12 is a flow diagram showing operation of the test apparatus in an **30** embodiment of the invention in steps **S** 12.1 to **S12.7.**

Figure **13** is a flow diagram showing operation of the test apparatus in an alternative arrangement in steps **S13.1** to S13.4.

In some arrangements, some or all of the signal processing functions may be performed in a processor in an external network, for example being performed **5** in the cloud. In this case the controller and/or processor would be in communication with the external network to send the data, for example the samples, for signal processing and to receive the results of the signal processing.

The above embodiments are to be understood as illustrative examples of the invention. It is to be understood that any feature described in relation to any **10** one embodiment may be used alone, or in combination with other features described, and may also be used in combination with one or more features of any other of the embodiments, or any combination of any other of the embodiments. Furthermore, equivalents and modifications not described above may also be employed without departing from the scope of the invention, which is defined in

**15** the accompanying claims.

#### Claims

**1. A** method of operation of a meter for performing a measurement of an electrical parameter, the method comprising, in the meter:

**<sup>5</sup>**sampling an output from a sensor of the electrical parameter to produce at least one sample; and

iteratively performing steps of.

sampling the output from the sensor to produce one or more further samples;

**10** holding in memory a stored array of samples comprising the at least one sample and each of the one or more further samples from each iteration;

> determining a measure of statistical variability from the stored array of samples for the respective iteration;

**15** determining a measure of statistical variability of a mean for the respective iteration from the measure of statistical variability and from the number of samples used to generate the measure of statistical variability;

> comparing the measure of statistical variability of the mean with a pre-determined threshold; and

20 generating an electrical signal indicating a state of the measurement if the measure of statistical variability of the mean of the samples taken during the measurement is less than or equal to the pre determined threshold.

**25** 2. **A** method according to claim **1,** wherein the electrical signal indicating a state of the measurement indicates that the measurement has reached or exceeded a target confidence level.

**3. A** method according to claim 1 or claim 2, wherein the electrical **30** signal indicating a state of the measurement indicates that the measurement is complete.

4. **A** method according to any preceding claim, wherein the measure of statistical variability is a standard deviation.

**5 5. A** method according to any one claims **I** to **3,** wherein the measure of statistical variability is a variance.

**6. A** method according to any preceding claim, wherein the measure of statistical variability of the mean is a standard deviation divided **by** the square **10** root of the number of samples used to generate the measure of statistical variability.

**7. A** method according to any preceding claim, wherein determining the measure of statistical variability from the stored array of samples comprises, **15** at each iteration:

forming a second array of samples to be held for the iteration in addition to the stored array of samples **by** filtering the array of samples, and

calculating the measure of statistical variability of the second array of samples.

20

**8. A** method according to claim **7,** wherein filtering the stored array of samples comprises applying a median filter.

**9. A** method according to claim **8,** wherein applying the median filter **25** comprises:

arranging the samples in the stored array of samples in order of magnitude;

forming the second array of samples from the stored array of samples **by**  discarding at least a sample with greatest magnitude.

**30**

**10. A** method according to claim **9,** wherein forming the second array of samples from the stored array of samples comprises discarding a sample with greatest magnitude and a sample with least magnitude.

**5 11. A** method according to any one of claim **7** to claim **10** comprising: calculating an average measurement of the electrical parameter at each iteration from the second array of samples; and

generating an output indicating the average measurement.

- **10** 12. **A** method according to any preceding claim comprising: generating an output indicating confidence of the measurement at each iteration from the measure of statistical variability of the mean and a target measure of statistical variability of the mean.
- **15 13. A** method according to claim 12, wherein the output indicating confidence of the measurement represents a percentage of a target confidence level.

14. **A** method according to any preceding claim, comprising:

20 determining a time-to-finish estimate for the measurement from the measure of statistical variability; and

generating an output indicating the determined time-to-finish estimate.

**15. A** method according to claim 14, wherein generating the output **25** indicating the determined updated time-to-finish estimate comprises: calculating an average of said determined time-to-finish estimate and at least some of previously determined time-to-finish estimates.

**16. A** method according to any one of claims **10** to claim **15,** wherein **30** each said output is a digital control to a display.

**17. A** method according to any preceding claim, comprising stopping the measurement in response to the electrical signal indicating a state of the measurement.

**5 18. A** meter for performing a measurement of an electrical parameter, comprising:

a sensor configured to measure the electrical parameter;

a processor configured to perform the method of any one of claims 1 to

**17.** 

**10**





Figure 2



Figure 3



Figure 4



Figure 5



Figure 6b



Figure 6c



Figure 7



Figure 8



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Figure 12



Figure 13