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DETECTION OF LOW SIGNAL-TO-NOISE RATIO SEISMIC SIGNALS

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OW SIGNAL-TO-NOISE RATIO SEISMIC SIGNALS

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 $BY$ 

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## 3,193,777<br>DETECTION OF LOW SIGNAL-TO-NOISE RATIO SEISMIC SIGNALS Joe P. Lindsey, Sheldon E. Elliett, and Ralph C. Loring, all of Bartlesville, Gsla., assignors to Phillips Petroieum

Company, a corporation of  $\mu$ eraware Filed Nov. 27, 1931, Ser. 199, 153,123<br>12 Claims. (Cl. 349—15.5)

This invention relates to a method and apparatus for 10 utilization in the identification of information in a plurality of signals. In one aspect the invention relates to reflection seismology, whereby seismograph records are produced and geophysical data interpreted therefrom. In another aspect the invention relates to the identification of 15 information contained in low signal-to-noise ratio signals.<br>In yet another aspect the invention relates to method and apparatus for improving the signal-to-noise ratio of

seismic signals.<br>The detection of systematic reflection events on sics- 20 mixing process.<br>mograph records by visual means is often extremely difficult, if not impossible, when the energy in the systematic reflection events is of the same order of or less than that in the unsystematic events appearing on the same recordings. As a practical manner visual identification of 25 common reflections in a plurality of records generally cannot be made unless the signal-to-noise ratio is greater than approximately 1.5. Unfortunately, records of this quality cannot always be obtained in many areas.

Many methods have been proposed and developed to  $30$ improve the seismic record to enable the operator to de tect reflection arrivals. These methods fall into the three broad categories of the application of some form of filtering, the addition of several traces containing systematic events, and the use of special methods of displaying the seismic data. events, and the use of special methods of displaying the 35

Conventional filtering has been pretty well exploited in years past. The need for a high pass, low pass, or band pass filter is usually obvious from the record appearance pass filter is usually obvious from the record appearance if some semblance of signal is present. However, con-<br>ventional filtering has severe limitations when special problems exist such as extremely low signal-to-noise ratios, periodic interferences caused by surface layer waveguide phenomena, ghost reflections, etc., or when the deeper reflection arrivals are severely scattered by an inhomogeneous surface layer. Solution of these problems<br>requires that the concept of filtering be considerably<br>broadened to include any black box that will improve<br>the signal-to-noise ratio and this is seldom just a high<br>

Three specific problems just mentioned—ghosts, wave-<br>guide phenomena, and scattering—can be handled by non-conventional filters of the proper design. In the case of scattering, it can be shown that given enough information about the signal and noise, a theoretically "optimum" filter can be designed to bring out a specific signal wavelet<br>and reject a specific noise with great success. To apply this technique to the seismograph problem requires more knowledge than is available, particularly about the noise  $\frac{30}{2}$ on each trace. In a pratcical sense, only statistical in formation is known concerning the noise, and the best estimate of the signal is that obtained from the sum of a certain number of traces. With these limitations, the effectiveness of a "static optimum" filter is considerably

reduced.<br>From the use of the "static optimum" filter it has been learned that an optimum filter must vary its tuning to match each reflection wave-shape on the record, thus requiring a dynamic filter characteristic, and that the statistical properties of the noise must he exploited to 2

eliminate as much of the noise as possible without risk

cf losing the signal. The attempt to fulfill these requirements has resulted in coherence multiplication, a process that can be viewed as a continuously optimum filtering of the seismic record. This process requires summing of all the traces and multiplying each trace by this sum. The multiplicaand the multiplication is carried out only for those intervals of time when the sum trace and the individual trace are of the same<br>polarity. The process yields a record with the same polarity, The process yields a record with the same noise ratio. On the average, the improvement in signal-<br>quality of the seismograph is proportional to the square<br>root of the number of traces in the composite.

However, the achievement of this improvement is critically dependent upon the time alignment of the sigrals; for only when the signal component is aligned is<br>the trace a measure of the quantity desired. This time alignment consideration cannot be overlooked in any

The times of arrival of the elastic waves from the shot point to the different seismometers vary with the horipoint to the different seismometers vary with the horizonzontal or surface distance between the shot point and scismometers. This variation or difference in time across the scismogram is referred to as normal moveout (sometimes as angularity of path) and is a dynamic error which tends to obscure alignments of corresponding signai portions along traces. The normal moveout time varies non-linearly in magnitude during the recording of these seismic signals. The magntiude is largest right after the detonation of the shot, when the differences in distances of the elastic wave travel paths are largest. The tances of the clastic wave travel paths are largest. The magnitude decreases as the differences in travel paths decrease for successively deeper reflecting horizons. The exact manner in which the normal moveout time varies as a function of time after the intial seismic disturbances will, of course, depend on the spacing of the different seismometers and the particular velocity function of the surveyed area.

A second time alignment correction which must be made is due to topographic effects such as variations in the elevation of the shot point and seisnometers and the existence of a weathered layer at the earth's surface. These effects introduce constant static errors in the time alignment of seismic cvents on the seismogram traces.

A number of procedures have been purposed or used<br>in the past for correcting time alignment errors due to normal moveout, elevational, and weathered layer effects. While some of these prior art procedures have<br>worked satisfactorily in some areas, others are not practical because they decrease the signal-to-noise ratios, or they require a number of very time-consuming corrective trace reproductions, while others are not able to cope with the non-linearity of the normal moveout. In addition the the linearity of the normal movement movement. In addition the prior art procedures have not been able to effectively counteract variations in dip, which is one of the most

However, the requirement of accurate time alignment of low signal-to-noise ratio seismic signals for use in the ccherence multiplication process again leads to the difficulties of searching the record for reflection events where

the events are not visually evident.<br>In accordance with one aspect of this invention there is provided a process and apparatus for effecting the proper time alignment of scismic signals even in the presence of substantial amounts of noise wherein the seismic signals  $\ddotsc$ are time aligned at various dip angles through the utilization of an electromechanical analog of the time triangle, the time aligned signals for each dip angle are summed to form composite signals, the individual time aligned 70 to form composite signals, the individual time aligned<br>signals are compared with the respective composite sig3,193,797<br>and to form output signals whenever the individual signals are in phase with the composite signal, the output<br>signals are summed to obtain correlation signals repre-<br>sentative of the degree of correlation between the indi-<br>vidual signals and the composite signal, and the corr

there is provided a process and apparatus for improving the reflection seismology technique by increasing the readability of low signal-to-noise ratio seismic signals by effecting the proper time alignment of the low signal-to-<br>noise ratio signals through the process of time aligning<br>the signals at various dip angles by means of an electro-<br>mechanical analog of the time triangle, summing t time aligned signals for each dip angle to form composite<br>signals, comparing the individual time aligned signals<br>with the respective composite signal to form output sig-<br>nals, summing the output signals to obtain correlati signals representative of the degree of correlation be-<br>tween the individual signals and the composite signal, and the individual signals and the comparing the comparing the comparing the comparing propriate dip angle, and then increasing the signal-to-<br>noise ratio of the individual seismic traces which have<br>been time aligned with the all of such traces and multiplying each trace by the sum<br>during the intervals of time when the sum and the individual trace are of the same polarity. Accordingly, it is an object of the invention to provide

an improved process and apparatus for detecting actual  $z_0$  seismic signals in the presence of noise. Another object of the invention is to improve the reflection seismology<br>technique by increasing the readability of seismographic<br>records. Another object of the invention is to correct<br>seismographic records by an improved technique which rapid, accurate, and relatively simple. Another object of the invention is to provide improved method and apparatus for correcting the time alignment of scismic records.<br>Another object of the invention is to provide proper time Another object of the invention is to provide proper time<br>alignment of seismic signals by considering the effects of 40<br>various dip angles.

Other aspects, objects and advantages of the invention will be apparent from a study of the disclosure, the drawings and the appended claims.

In the drawings FIGURE 1 is a block diagram of the process in accordance with the invention;

FIGURE 2 is a schematic view of terrain in cross section showing the path geometry of elastic waves as they travel from shot point and are reflected back to seismom-<br>eters;<br>FIGURE 3 is a view showing the pictorial relationship 50

between the traces of a seismogram and the time triangle analog;

FIGURES 4 and 5 schematically illustrate mechanical analogs of the time triangle;

FIGURE 7 is a schematic circuit drawing of one em-<br>bodiment of the discrimination apparatus;<br>FIGURE 8 is a schematic representation of the operat-<br>ing features of FIGURE 7;

FIGURE 9 is a representation of seismic signals to be processed;<br>FIGURE 10 is representation of signals obtained by

the discrimination procedure in accordance with the invention;<br>FIGURE 11 is a schematic representation of the appa-<br> $65$ 

ratus for the coherence multiplication process; and

FIGURES 12, 13, 14 and 15 show the approximate wave forms produced in the apparatus of FIGURE 11.

Referring now to broad view of the overall process as 70 shown in FIGURE 1, the outputs from a plurality, commonly 24, of seismic detectors 1 are fed into storage zone 2, which can be a magnetic tape storage device. When it is desired to process the seismic signals, they are removed

zone  $3$  wherein the signals are time aligned at various dip angles. The time aligned signals corresponding to each dip angle are passed to discrimination zone 4 to produce a coherence signal for each dip angle. The coherence signals are compared to select the proper dip angle

5 in selection zone 5. The time aligned seismic signals corresponding to the proper dip angle are then passed to coherence multiplication zone 6 wherein the signal-to-noise here multiplication zone 6 wherein the signal-to-noise ratio is improved. The improved signals are then transmitted to interpretation zone 7 for interpretation of the 10 mitted to inter-

The basis for the reflection seismology technique is<br>shown in the space diagram of FIGURE 2. For purpose<br>of brevity, let it be assumed that the datum plane coin-<br>cides with the surface of the earth. The ray paths gener-<br>at  $15$ zons. Two such subsurface horizons are shown in FIG-URE 2, one of which is horizontal and the other at an angle or tilted with respect to the earth's surface.  $\overline{c_0}$  array of seismometers, such as  $S_1$ ,  $S_2$ ,  $S_3$ , and  $S_4$ , at the earth's surface and spaced in a predetermined manner from shot point E, detect the arrival of the reflected Waves and convert the same into electrical signals which are amplified and recorded on seismograms. The re-<br>flected sound waves appear to come from points  $I_1$  and  $I_2$ , known as image points. Each image point lies as far below the particular reflecting horizon as the shotpoint E is above the horizon and is located along a line normal<br>to the reflecting horizon and intersecting the shotpoint. Any ray path  $ER_nS_n$ , where  $S_n$  is the position of any seismometer and  $R_n$  any point of reflection, is equivalent to path  $I_nR_nS_n$ , where  $I_n$  is an image point for the horizon in which  $R_n$  lies. For example, ray path  $ER_3S_1$  is equivalent to path  $I_1R_1S_1$ , and ray path  $ER_3S_4$  is equivalent to  $35 \,$ evident that  $ER_2S_2$  (or  $I_1R_2S_2$ ) is greater than  $ER_1S_1$  (or  $I_1R_1S_1$ ) so that when reflected wave front from the hori $z$ ontal horizon reaches seismometer  $S_1$  the wave front will be short of seismometer  $S_2$ . In the case of the tilted or dipping horizon, it is evident that  $ER_8S_4$  (or  $I_2R_8S_4$ ) is greater than  $ER_6S_2$  (or  $I_2R_6S_2$ ) so that when reflected wave front from the tilted horizon reaches seismometer  $S_2$  on one side of the shotpoint E, the wave front is still short of the corresponding seismometer  $S_4$  on the other side of the shot point. The difference in reflection times is called normal moveout, and it increases both with the degree of tilt or dip and the distance between the end

FIGURE 6 is a schematic view of a multi-channel me- 55 the time triangle of FIGURE 3 with sides  $t_h$ ,  $t_r$ , and  $t_h$ <br>chanical analog corrector;<br>FIGURE 7 is a schematic circuit drawing of one em-<br>bodiment of the discrimina 60 reflector and back to shotpoint. degree of the seismometer array or spread.<br>The space diagram of FIGURE 2 can be converted into an analog diagram of time, as shown in FIGURE 3. Since the dimensions of the space of FIGURE 2 are distance, division of each of the triangle legs by a velocity parameter converts the triangle dimensions to time. The average velocity  $\nu$  over the ray path is used for the velocity parameter. This conversion to time units produces mometer station  $S_n$ ,  $t_r$  is the time from shotpoint E to reflector to seismometer  $S_n$  (or from image I to seismometer  $S_n$ ), and  $t_n$  is the normal time from shotpoint E to

FIGURE 3 also shows the pictorial relationship be-<br>tween the time of arrival and the traces of a seismogram recorded by a seismometer  $S_0$  at a shotpoint E and seismometer  $S_n$  located at a known distance from the shotpoint. The difference in arrival times of a seismic event at a seismometer  $S_0$  and at seismometer  $S_n$  is equal to  $\Delta t$ , the extra time required for the wave to travel from shotpoint E to reflector to seismometer  $S_n$ . This extra time is the normal moveout time correction neces-

From storage zone 2 and introduced into time alignment  $75$  eter distance) does not vary with time, however, the leg Sary to convert reflection time  $t_r$  to normal time  $t_n$ .<br>There is an important difference in the dynamic time dependent properties of the space triangle of FIGURE 2 and the time triangle of FIGURE 3. In the space triangle of  $FIGURE 2$ , the leg  $ES<sub>n</sub>$  (shotpoint to seismom-

 $ET_n$  (shotpoint to image distance) and  $T_n$ s (in  $T_{n-1}$  from the seismometer distance) both increase in senger firmulation shot instant in a manner determined by the change in average velocity  $v$ . This increase is uniform with time average velocity  $v$ . This increase is uniform where  $\frac{1}{2}$  if the average velocity is constant. The legs of the time triangle of FIGURE 3 behave somewhat different-<br>ly. Since average velocity is a determining factor in<br>the length of each leg of the time triangle, all three legs change with record time. The  $\log t_{\rm h}$  usually decreases with record time since the special dimension  $\mathbb{E}_{\text{on}}$  is constant and v usually increases. The leg in regresents elapsed time from the shot instant and increases uniformly. The leg t<sub>r</sub> must increase in such a way as to maintain the time triangle closed.

In accordance with the invention, the normal move-15 out is corrected by the electromechanical analog of the out is corrected by the electromechanical analog is shown<br>time triangle of FIGURE 3. Such an analog is shown schematically in FIGURE 4. A magnetic tape 11 containing the trace of one seismometer  $S_n$  is attached at  $S_n$  is adapted 20 initial time end to a tape carriage 12 which is adapted 20 to move at a constant speed in one direction. The other end of the tape 11 is attached to a tape takeup drum<br>13. Since the tape 11 has a dimension in time units, it can represent the leg  $t_r$  of the time triangle. As the can represent the leg  $t_r$  of the time triangle. As the carrier tapes, the tape carriage 12 is returned to its<br>tape carriage 12 starts at the indicated initial position 25 magnetic tapes, the tape carriage 12 is swung out and travels uniformly downward, the tape will move across the magnetic playback head 14 allowing the seismic<br>date to be reproduced. The resulting non-uniform tape denoted to be represented. The residence of the residence velocity across the playback head 14 will cause the time of playout of reflection events to be equivalent to nor mal time  $t_n$  rather than reflection time  $t_r$  since the location of the playback head  $14$  and tape  $11$  are such that reproduced events are advanced by an amount equal to  $\Delta t$ . Consequently, the normal moveout time correction  $\Delta t$  is accomplished directly in playback operation.  $35$ 

Since not all reflection events require the same value of  $t<sub>h</sub>$ , this side of the time triangle must vary in length as the  $t<sub>n</sub>$  side increases uniformly. The quantity  $t<sub>h</sub>$  must be maintained proportional to the inverse of average 46) velocity  $v$ , the constant of proportionality being the shot-<br>point-to-seismometer distance. The average velocity as a function of normal time must be known or assurned. In most situations the average velocity increases with the record time and the parameter  $t_h$  decreases with the increase in normal time  $t_h$ . 45

when the reflecting horizon is tilted or dipped, an appropriate change in the time triangle must be made<br>to maintain the mechanical analog. This is accomplished by changing the angle between the  $t<sub>h</sub>$  and  $t<sub>n</sub>$  legs of the triangle from 90°. The amount of change is equal to the dip angle  $\alpha$ . FIGURE 5 illustrates the incompanion analog configuration required for a dip angle  $\alpha$ . 50

The analogs discussed to this point have been limited to a single recorded seismic trace. A multi-channel analog with the same accuracy of the single channel analog can be accomplished by instrumenting a multi plicity of mechanical analogs using a common  $t_n$  dimension and a multiplicity of  $t_n$  dimensions. Since the same average velocity function holds approximately for same average velocity function holds approximately for every trace, the  $t<sub>h</sub>$  function associated with the farthest 60 seismometer station can be scaled downward for each of the other seismometer stations thereby simplifying the problem of generating the  $t<sub>h</sub>$  motions required for the multiplicity of time triangles. FIGURE 6 illustrates a six channel time corrector developed as an extension of 65<br>the single channel corrector of FIGURE 4. Six tapes 11 are attached to a common carriage 12 which is adapted to move along guide rods 17. In FIGURE 6, the cor-<br>ners of the six time triangles represented by the tape inners of the six time triangles represented by the tape in dex pins 16 are the only corners that are not common. 70 However, these corners are related positionally in the same way that the seismometers stations are related. So, if the index pins 16 are coupled in such a way that movement of the pin for the farthest seismometer station also move the other pins in proportion, all the  $t<sub>h</sub>$  75 55

dimensions of each time triangle are maintenance proper proportion, and thus all of the six time triangles are generated simultaneously with a downward motion of<br>the tape carriage 12.

 $\mathbf{0}$ There are two basic phases of operation of the multichannel device such as schematically illustrated in FIG-URE 6. First, the seismic field data displayed are re produced in such a manner that each trace of the seismogram is transcribed onto an individual magnetic tape of the analog corrector of this invention. Then, the data on the individual magnetic tapes are played off in such a way that the required time corrections are accoma way that the required time corrections are accomplished. To transcribe the field data onto the individual magnetic tapes of the analog device, all of the index pins 16 (which are attached to magnetic heads 14) are positioned at the initial carriage position. This means that the  $t_h$  arm 18 coupled indirectly to the index pins 16 is positioned so that the  $t_h$  dimension is zero. In this condition, the tape carriage is started and moves uniformly downward as each channel of seismic data is recorded on its respective tape. No change in the time alignment of reflection events is produced by the recording of the tapes in this phase.

formly downward, the  $t_n$  arm 18 is moved in such a way<br>30 that the proper value of  $t_n$  is maintained at all times for<br>all channels. When the playout made in this phase is To play back the data thus recorded on the individual to a position corresponding to the  $t<sub>h</sub>$  value desired at time zero. As the tape carriage 12 is started and moved unithat the proper value of  $t<sub>h</sub>$  is maintained at all times for examined, all reflection events will be time-aligned if the proper  $t_n$  occurred at the reflection normal time  $t_n$ . the proper  $t<sub>h</sub>$  occurred at the reflection normal time  $t<sub>h</sub>$ It is also necessary that the plane containing the  $\frac{1}{4}$ dimensions be set at the correct angle. If the reflections are from a subsurface horizon that has zero dip, the  $t<sub>h</sub>$  plane must be at exactly  $90^\circ$  with respect to the plane of travel of the tape carriage. For other than zero dip angle of the reflecting bed, the  $t<sub>h</sub>$  plane must be accordingly tilted and then the data played out to

achieve the time alignment of the reflection events. analog corrector are disclosed in copending application<br>Serial No. 123,231, filed July 11, 1961, by R. G. Piety<br>and R. A. Doubt, which is assigned to the assignee of<br>the present application and the description of which is

Referring now to FIGURE 7, the first of a plurality<br>of signals to be studied for time alignment with proper<br>dip angle is applied between input terminals  $2\theta a$  and  $2Ia$ ,<br>the latter being grounded. Terminal  $2\theta a$  is conn minal  $22a$  is connected by means of an input resistor  $23a$  to the first input terminal of a summing amplifier  $24$ . Amplifier  $24$ , which can be a conventional high gain operational amplifier, is provided with a feedbac of amplification such that the output signal is in phase<br>with the input signal. This output signal is applied<br>through resistors 26 and 27 to the input of a second<br>amplifier 28. Amplifier 28 is provided with a feedback resistor 29. Amplifier 28 is also provided with a suitable number of stages such that the output signal at terminal 30 is  $180°$  out of phase with the input signal to amplifier 28. A rectifier 31 is connected between ground and the junction between resistors 26 and 27.<br>Rectifier 31 serves to remove the negative half cycles of

the input signal applied to amplifier 28. Thus, the signal at terminal 30 comprises a series of negative pulses.<br>The output signal of amplifier 24 is also transmitted through a second network similar to the one previously described and wherein corresponding elements are designated by like primed reference numerals. The only difference between these two circuits is the polarity of rec

the  $\overline{31}$ , which results in a series of positive pulses appearing at output terminal  $30'$ .

 $\frac{1}{22}$  commun 20a is also connected through a capaci $t^2$  and a resistor 33a to the control grid of a triode 34a. The control grid of triode 34a is connected through a rectifier 35a and a resistor 36a to a terminal 37a that is maintained at a positive potential. A terminal 38a, which is maintained at a negative potential, is connected through a resistor  $39a$  and a rectifier  $40a$  to the control grid of triode 34a. The first end terminal of a potentiometer 42a in<br>
is connected to the innetion between restifies  $37 \text{ m}$  and is connected to the junction between rectifier  $35a$  and resistor  $36a$ , and the second end terminal of potentiometer 42a is connected to the junction between resistor  $39a$ and rectifier  $40a$ . The contactor of potentiometer  $42a$ is connected to ground. Potentiometer  $42a$  and resistors 15<br>36a and 39a thus form a voltage dividing network such that positive and negative bias potentials are applied to rectifier 35a and 40a, respectively. These rectifiers there by provide a bipolar clipper such that signals having substantially a square wave shape are applied to triode  $34a_{20}$ <br>from input terminals  $20a$ .<br>The cathode of triode  $34a$  is connected to ground

through a resistor  $44a$ . The anode of triode  $34a$  is connected through a resistor 45a to a terminal 46a which is maintained at a positive potential. The anode of triode 34a is also connected through a capacitor 47a, a resistor  $48a$  and a resistor  $49a$  to a terminal  $50a$ . A pair of diodes 53a, connected in back-to-back relationship, is connected between ground and the junction between resistors  $48a$ <br>and  $49a$ . These rectifiers function as an additional clipping network so that signals having substantially a square wave configuration appear at terminal 50a. A rectifier 51a is connected between terminal 30 and terminal 50 $a$ . A rectifier 52a is connected between terminal 50a and<br>terminal 30<sup>'</sup>. Terminal 50a is also connected to the first<br>is  $\frac{m_{\text{part}}}{m_{\text{max}}}$  terminal 55*a* of a second summing circuit.

The apparatus of FIGURE 7 is provided with as many individual clipping circuits as there are signals to be compared. Thus, the summing circuit previously described is provided with additional input termnals  $22b$ ,  $22c$ , **22***n*. The clipping circuit associated with terminal 22*n* is illustrated in the lower part of FIGURE 7. This clipping circuit is identical to the one previously described and corresponding elements are designated by similar *n* reference charcters. Input terminals  $55a, 55b, 55c...$  55*n* are connected  $45\,$ 

Input terminals 55cm, 55cm, 55cm, 55cm, 55cm, 56cm, 56cm, 56m to the first input of a summing amplifier 57. Amplifier 57 is provided with two feedback resistors 58 and 59 in series, the latter being adjustable. The output of am-<br>plifier 57 is connected the unit. The output of amplifier 57 is connected through a pair of back-to-back rectifiers 60 and a resistor 61 to ground. Output terminals 62 and 63 are connected to the respective end terminals of resistor 61.<br>As previously mentioned, the signal at terminal 30

55 comprises a series of negative pulses which represent the negative half cycles of the sum of the signals to be compared. The signal at terminal 30' represents the corresponding positive pulses of this sum. Rectifiers  $51a$  and  $51n$  operate to transmit the output signal from the upper 511 operate to transmit the upper clipping circuit to the first input of summing amplifier 57 when this clipped signal is in phase with the summed<br>output signal from amplifier 24. The operation of rectifiers  $51a$  and  $51n$  in this manner can readily be seen from an examination of the curves in FIGURE 8. It will be assumed that the output signal which appears at  $65$ terminal 50 $a$  from triode 34 $a$  is of a square wave configuration as shown by curve  $65$ . It will first be assumed that this signal is in phase with the sum of the individual signals being compared. Under these circumstances, the output signals at terminals  $30$  and  $30'$  are of the form<br>shown by respective curves 66 and 67 of FIGURE 8. During the first half cycle, terminal  $50a$  is positive and terminal 30 is zero so that rectifier  $51a$  does not conduct. Terminal 30' is positive at this same time so that rectifier 75

 $\frac{1}{2}$  does not conduct. Thus, the positive half cycle of the output signal from triode  $34a$  is transmitted as an input to summing amplifier 57. During the second half cycle, the signal at terminal 50a is negative. The signal at ter-Inimal 30 is also negative, whereas the signal at terminal  $30'$  is zero. Again, neither of the rectifiers  $51a$  or  $52a$ conducts so that a negative signal is transmitted from tri-<br>ode 34a to summing amplifier 57.

If the signal transmitted through triode  $34a$  should be  $180^\circ$  out of phase with the sum of the initial input signals, as shown by curve 68, there is no output signal transmitted to summing amplifier 57. During the first half cycle of such a signal, terminal  $50a$  is negative. However, the potential at terminal 30 is zero so that rectifier 51*a* conducts to prevent the signal at terminal 50*a* from being transmitted to amplifier 57. During the second half cycle, the signal at terminal  $50a$  is positive whereas the signal at terminal  $30'$  is zero, so that rectifier  $52a$  conducts. Thus, the output signal from triode  $34a$  is shorted at all times so that there is no output

signal transmitted to summing amplifier 57.

25 are applied to summing amplifier 57 through respective sum of the input signals. Variable resistor  $59$  permits the<br>30 gain of summing appliface  $57$  to resistor  $59$  permits the The clipped signals from the remainder of the individual networks are also compared with summed signals vidual networks are also compared with summer signals at terminals 30 and 30'. The resulting transmitted signals resistors  $56b$ ,  $56c$ ...  $56n$ . The magnitude of the output signal from amplifier 57 is thus representative of the number of input signals which are in phase with the sum of the input signals. Variable resistor 57 permits the gain of summing amplifier 57 to be adjusted so that an output signal is transmitted only when a preselected num ber of individual signals are in phase with the sum.<br>The effectiveness of this procedure for identifying com-

The effectiveness of this procedure for identifying common reflections in a plurality of seismic records is illus-<br>trated in FIGURES 9 and 10. The curves of FIGURE 9 are seismic records prior to being processed by the apparatus of this invention. Electrical signals representative of the curves of FIGURE 9 are then applied as inputs to the apparatus of FIGURE 6. The procedure is repeated a number of times with the curves of FIGURE 9 being displaced from one another by amounts varying from  $+33^{\circ}$  to  $-36^{\circ}$ , as noted in FIGURE 10. These<br>displacements are arbitrary assumptions to compensate<br>for "angularity of path" corrections of the seismic signals.<br>The output signals of the apparatus of FIGURE 6 then applied as inputs to the apparatus of FIGURE 7. As noted in FIGURE 10, there is a decided correlation near the center of the resulting records, with respect to time. This indicates that common reflection appear in the records at this time.

60 form the control trace (FIGURE 13). Referring now to FIGURE 11, there is shown a stor age means 110 wherein there is disposed a plurality of individual seismic signals which have been corrected for angularities-of-path in time alignment zone 3 (see FIG-URE 1) in accordance with the proper dip angle as de termined in discrimination zone 4 and selection zone 5. Storage means 110 can comprise a magnetic tape. All of the corrected signals are removed from storage means 110 and applied to a means for summing 112 to thereby

The control trace that appears at the output of 112 is next applied to each of two channels in such manner that<br>the control trace is divided into  $(+)$  and  $(-)$  polarity components. Where reference is made hereinafter to a plus or minus polarity signal that is derived from this seismic data, the reference is to the polarity of the signal<br>as it appears when drawn from the storage means 110, regardless of its actual polarity in subsequent apparatus<br>and operation. This is because the means for summing<br>112 and other apparatus each causes a phase inversion.<br>Therefore, for clarity, a plus  $(+)$  signal or channel ( the opposite polarity. The ultimate output signal of the coherence multiplication system is phase inverted from

the input signal of the coherence multiplication system. It is not essential to correct this condition, but correction can be achieved by connecting an inverting amplifier to the output terminals. The polarity of the components of the control trace is determined in accordance with an  $5$ arbitrarily selected zero. The same operations are per formed on this control trace in each channel. Therefore, for the sake of brevity, only one channel-that operating on the positive polarity signal-will be described hereinafter. The negative polarity signals are operated on in 10 that portion of the apparatus denoted by prime numbers in FIGURE 11. For the sake of providing uniform chan nel construction, the signal into the  $(-)$  channel is subjected to phase inversion in inverter 55.

signals to a mixer  $114$ , which is really another means for summing and which also receives a negative-going second input (sawtooth) signal 115 (FIGURE 12) and produces the waveform 116 (FIGURE 14) as an output signal. A sawtooth generator provides the signal  $\overline{115}$  20 lower quality seismic data trace is removed from storage which is combined with the control trace in the mixer 114 to thereby produce the waveform 116. A negative-going sawtooth 115 is applied to both the plus and minus polarity channels because (a) mixers 114 and 114 in clude a phase-inverting amplifier and (b) inverter 115 25 provides a control trace of correct phase for mixing with the sawtooth in the negative channel.

The waveforms 116 thus produced are next applied to first and second width modulators 117 and 117' wherein there is formed a time-series of pulses 118 (FIGURE 15), the spacings of which are a function of, and may be said to be representative of, the successively occurring amplitudes of the respective poiarity component of the control trace. The spikes of the waveform shown in FIGURE 14 are necessary to switch the width modulator 35 117 from one state to another. The width modulator 117 (also 117') is essentially a flip-flop which is adjusted to change state upon the application to the input terminal thereof of a voltage equal to E (as shown in FIGURE 14) and to subsequently change efter that that such 40 14) and to subsequently change state after that event only upon the input signal going to zero. Changes in the region from zero to E volts produce no change of state.<br>The switching function upon the application of voltage E occurs whether the voltage is equal or greater than E. The spikes of FIGURE  $14$  consume a time interval of  $45$  about 1 percent of the total duration of 1 sawtooth cycle (1000 microscconds). The output signal of the width modulator has the waveform 113 as shown in FIGURE 15. It should be apparent from comparing FIGURE 14 with FIGURE 15 that the width modulator also performs 50 a polarity separating function because no width modula tor signals are produced by the negative portion of the portion of FIGURE 14) by reason of the inability of the mixed signal to achieve a voltage amplitude equal to or greater than E. It should be understood that the summing circuit 112 and mixer 114 both include an inverting amplifier and therefore the inversion that takes place in the mixer 114 merely returns the control trace component to its original polarity as derived from the original signals<br>drawn from 10.<br>The sawtooth signal thus serves to "sample" the ampli-

tudes of the control trace. As is evident from FIGURE 14, there is some non-symmetry in the sampling, by reason of the shape of the sawtooth frequency. Hereinafter,  $65$ when the term "sample" or "sampling" is used, reference is made to the technique of causing a circuit to change state by applying thereto a compound waveform made up of plural waveforms neither one of which is capable up of plural waveforms neither one of which is capable cf producing a stable change of state by itself.

Each respective series of pulses (waveform 118) is then applied to a power state 120, hereinafter termed a driver. One of the principal reasons for supplying the drivers wave trains 121 and 121', respectively, formed therein can be applied to a plurality of individual channels, thereby to be compared, i.e., multiplied by the individual seismic traces operated on in each individual channel. Moreover, it is to be noted that the output signals 121, 121' from the driver (and width modulator too) have various spacings W, each of which are representative of an amplitude of the control trace produced in the means for summing 112. The reason that two channels are provided for producing these time spaced pulses is so that

signals of different polarities can be multiplied by them.<br>This common equipment of the coherence multiplication system provides a control trace which is compared by multiplication with each individual seismic data trace The control trace is next applied as one of the input  $15$  in an individual subsequent circuit. One of these subsequent circuits is next described. It is understood that a plurality of these individual circuits is provided and that. preferably they are all constructed in like manner.

Still referring to FIGURE 11, a signal representing a 110 and applied to a means, 122, for separating such trace into its positive and negative polarity components. From this point cn there is a separate channel provided for the con ponents of each polarity. These components are next applied to an inverting amplifier and a clamp circuit in combination 124 and 124' (representing each channel respectively). The clamp circuits operate to pass only those signals having a certain amplitude or greater. Such signals as are passed are applied to multiplying circuits  $126$  and  $126'$  where they are multiplied by the time spaced signals  $121$  or  $121'$ , as the case may be. The output signals from the multipliers are then applied to a fourth means for summing,  $128$ .

The output signal from the means for summing has the general appearance of signal 129. As noted on the drawing, it is of broken line form and the positive and negative components have discontinuities  $130$  where they come together. In some instances (e.g. where  $130$  is small) the signal. However, it is generally desired to form a continuous signal having discontinuities  $130$  removed, if possible. To this end, a filter  $132$  is provided. The output<br>signal from the filter  $132$  is of the general form  $133$  hav-<br>ing seismic events  $134$  clearly shown thereon and segments<br> $135$  which represent those areas where filter or a LRC passive filter of a general type well-known to those in the electronic art.<br>The details of a preferred embodiment of the coherence

multiplication system are disclosed in copending application Serial No. 811,367, filed May 6, 1959, by J. P. Greening, now U.S. Patent 3,032,743, the description of which is incorporated herein by reference.

5 5 that there is provided in accordance with this invention 60 scribed in conjunction with a presently preferred embodi-From the foregoing description it can readily be seen a novel procedure and apparatus for identifying information in a plurality of signals and which are particularly adapted for increasing the value of low signal-to-noise ratio seismic signals. While the invention has been d ment, it is obvious that it is not limited thereto.

We claim:

120 and 120' is to provide sufficient power so that the  $75$  said one element corresponding to said leg  $t_r$  of said 1. An apparatus for correcting the normal moveout of a plurality of seismic traces, produced by a plurality of seismometers, comprising means for generating a me-<br>chanical analog of the seismic time triangle for each of<br>said traces, said triangle comprising legs  $t_h$ ,  $t_r$ ,  $t_n$ , where<br>leg  $t_h$  is the horizontal time from shotp eter, leg  $t_r$  is the time from shot image to seismometer<br>and leg  $t_n$  is the normal time from shotpoint to shot image, a plurality of transcribing stations, one element<br>of said analog being a stored record of the respective one of said traces capable of being dynamically transcribed by<br>a respective one of said plurality of transcribing stations,

seismic time triangle, means for manipulating the analogs so that the length of the leg  $t_n$  of each of said analogs increases uniformly with time, this time starting from a time corresponding to shot instant when the legs  $t_r$  and  $t_h$ of said analog are coincident, the length of the leg  $t<sub>h</sub>$  of each of said analogs is proportional to the shot point to seismometer distance and inversely proportional to the average velocity between shot image and seismometer, the angle between the leg  $t<sub>h</sub>$  and leg  $t<sub>n</sub>$  for each of said analogs is 90° plus the angle of dip of the horizon, and so that the length of the leg  $t_r$  of each of said analogs is such as to maintain each of said analog triangles closed, said transcribing stations during said manipulating being located on said stored records external to the analog tri angles, so that the resulting non-uniform motion of said stored records across said transcribing stations will cause the time of transcription of seismic events to be equiva lent to the normal time rather than the reflection time, means for summing the transcribed signals of said tran scribing stations, means for comparing the resulting sum  $_{20}$ with each of said transcribed signals, means for establishing an output signal for each of said transcribed signals that is in phase with said resulting sum, means for sum-<br>ming the output signals to produce a coherence signal,<br>the magnitude of the coherence signal being representa- $_{25}$ tive of the common information present in said transcribed signals, means for varying the value of said angle of dip, and means for comparing the coherence signals corresponding to a plurality of values of said angle of dip to determine the proper value of said angle of dip for 30 accurate time alignment of said plurality of seismic traces.  $\overline{10}$ 

2. Apparauts for increasing the information available from a plurality of low signal-to-noise ratio seismic signals comprising, in combination; a plurality of magnetic tapes; means for storing each of said plurality of low 3.5 signal-to-noise ratio seismic signals on a respective one of said magnetic tapes; means to produce a plurality of being responsive to the signal stored on a respective one<br>of said magnetic tapes and to the rate of movement of  $\alpha$ of said magnetic tapes and to the rate of movement of such respective magnetic tape past said means to produce; means for varying the rate of movement of each of said magnetic tapes past said means to produce as a function of time, a predetermined dip angle, and the ratio of the distance between the shotpoint and the seismometer  $45\frac{45}{10}$ station at which the respective seismic signal was de tected to the average velocity of the seismic wave, where-<br>by said transcribed signals are representative of said plurality of low signal-to-noise ratio seismic signals in a time-<br>aligned relationship for said predetermined dip angle;<br>first and second summing means; means for applying to  $50$ <br>said first summing means as inputs thereto s of transcribed signals from said means to produce; a plurality of signal comparing means, each having a first is adapted to transmit a signal when input signals thereto are in phase; means connecting the output of said first rality of signal comparing means; means connecting each of said plurality of transcribed signals from said means to produce to a respective one of the second inputs of said plurality of signal comparing means; means connect ing the outputs of said comparing means to the inputs of said second summing means, and means for varying the value of said predetermined dip angle, whereby a comparison of the outputs of said second summing means corresponding to each value of said predetermined dip angle is indicative of the proper value of dip angle to be utilized for accurate time alignment of said plurality of low signal-to-noise ratio seismic signals.

3. Apparatus for increasing the information available from a plurality of low signal-to-noise ratio seismic signals comprising, in combination; a plurality of magnetic tapes; means for storing each of said plurality of low signal-to-noise ratio seismic signals on a respective one  $75$  tion at which the respective seismic signal was detected

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of said magnetic tapes; means to produce a plurality of transcribed signals with each of said transcribed signals being responsive to the signal stored on a respective one of said magnetic tapes and the rate of movement of such respective magnetic tape past said means to produce; s means for varying the rate of movement of each of said magnetic tapes past said means to produce as a function cf time, a predetermined dip angle, and the ratio of the distance between the shotpoint and the seismometer sta tion at which the respective seismic signal was detected to the average velocity of the seismic wave, whereby said transcribed signals are representative of said plurality of low signal-to-noise ratio seismic signals in a time-aligned relationship for said predetermined dip angle; first and<br>second summing means; means for applying to said first  $15$ summing means as inputs thereto said plurality of transcribed signals from said means to produce; a plurality of signal comparing means, each having a first input and a Second input and an output and each of which is adapted to transmit a signal when input signals thereto are in phase; means connecting the output of said first rality of signal comparing means; means connecting each of Said plurality of transcribed signals from said means to produce to a respective one of the second inputs of said plurality of signal comparing means; means connecting the outputs of said comparing means to the inputs of said second summing means, means for varying the value of said predetermined dip angle, whereby a comparison of the outputs of said second summing means corresponding to each value of said predetermined dip angle is indicative of the proper value of dip angle to be utilized for accurate time alignment of said plurality of low signalto-noise ratio seismic signals; a third summing means to sum a plurality of seismic signals to establish a first signal; means to apply to said third summing means as inputs thereto the transcribed signals from said means to produce which were provided as a function of said proper value of dip angle; fourth and fifth summing means; a sawtooth generator; means connecting the output of said generator to an input of said fourth summing means; means connecting the output of said third summing means to an input of said fourth summing means; a signal in verter; means connecting the output of said third sum ning means to an input of said fifth summing means through said signal inverter; means connecting the out put of said generator to an input of said fifth summing means; first and second pulse width modulators; means connecting the outputs of said fourth and fifth summing means to the inputs of said first and second modulators, respectively; first and second signal multiplying means; means to divide a seismic signal into positive and negative components; means connecting the positive components output of said means to divide and the output of said first modulator to the respective inputs of said 55 first multiplying means; means connecting the negative components output of said means to divide and the out put of said second modulator to the respective inputs of said second multiplying means; and means to sum the outputs of said first and second multiplying means. 60

4. Apparatus for increasing the information available from a plurality of low signal-to-noise ratio seismic signals comprising, in combination; a plurality of magnetic tapes; means for storing each of said plurality of low signal-to-noise ratio seismic signals on a respective one of said magnetic tapes; means to produce a plurality of transcribed signals, with each of said transcribed signals being responsive to the signal stored on a respective one of said magnetic tapes and the rate of movement of such respective magnetic tape past said means to produce; 70 means for varying the rate of movement of each of said magnetic tapes past said means to produce as a function of time, a predetermined dip angle, and the ratio of the distance between the shotpoint and the seismometer sta

13<br>to the average velocity of the seismic wave, whereby said transcribed signals are representative of said plurality<br>of low signal-to-noise ratio seismic signals in a time-<br>aligned relationship for said predetermined dip angle;<br>first and second summing means; means for applying to<br>  $\mathcal{G}$ are in phase; means connecting the output of said first summing means to each of the first inputs of said plurality of signal comparing means; means connecting each of said plurality of transcribed signals from said means plurality of signal comparing means; means connecting the outputs of said comparing means to the inputs of said second summing means; means for varying the value of said predetermined dip angle whereby a comparison of  $20$ the outputs of said second summing means corresponding to each value of said predetermined dip angle is indica tive of the proper value of dip angle to be utilized for accurate time alignment of said plurality of low signalto-noise ratio seismic signals; means for summing the transcribed signals from said means to produce corre sponding to said proper value of said dip angle to form a first signal; means for generating a sawtooth signal; means for summing said first signal and said sawtooth signal to form a second signal; means for summing said sawtooth signal and the inverse of said first signal to form a third signal; means for generating a pulse of uniform determined value to form a fourth signal; means for generating a pulse of uniform amplitude when said third 5 signal exceeds a second predetermined value to form a fifth signal; means for dividing an individual one of said transcribed signals from said means to produce corre-<br>sponding to said proper value of said dip angle into positive and negative components, means for multiplying said  $\partial \Omega$ fourth signal by said positive components to form a sixth signal, means for multiplying said fifth signal by said negative components to form a seventh signal, and means for summing said sixth and seventh signals.

**5.** Apparatus for increasing the information available om a plurality of low signal-to-noise ratio seismic traces  $45$ from a plurality of low signal-to-noise ratio seismic traces comprising, in combination, means for generating a mechanical analog of the seismic time triangle for each of said traces, said triangle comprising legs  $t<sub>h</sub>$ ,  $t<sub>r</sub>$ , and  $t<sub>n</sub>$ , where leg  $t<sub>h</sub>$  is the horizontal time from shotpoint to seismometer, leg  $t_r$  is the time from shot image to seis- 50 mometer, and leg  $t_n$  is the normal time from shotpoint to shot image, a plurality of transcribing stations, one element of said analog being a stored record of the respective one of said traces capable of being dynamically transcribed by a respective one of said plurality of tran-55 scribing stations, said one element corresponding to said leg  $t_r$  of said seismic time triangle; means for manipulating the analogs so that the length of the leg  $t_n$  of each of said analogs increases uniformly with time, this time 60 starting from a time corresponding to shot instant when the legs  $t_r$  and  $t_h$  of said analog are coincident, the length of the leg  $t<sub>h</sub>$  of each of said analogs is proportional to the shotpoint to seismometer distance and inversely proportional to the average velocity between shot image and 65 seismometer, the angle between the leg  $t<sub>h</sub>$  and leg  $t<sub>n</sub>$  for each of said analogs is 90° plus the angle of dip of the horizon, and so that the length of the leg  $t_r$  of each of said analogs is such as to maintain each of said analog triangles closed; said transcribing stations during said manipulating being located on said stored records ex ternal to the analog triangles, so that the resulting non uniform motion of said stored records across said tran scribing stations will cause the time of transcription of scribing stations will cause the time of transcription of of the common information present in said transcribed<br>seismic events to be equivalent to the normal time rather 75 signals; means for varying the value of said angl

adapted to transmit a signal when input signals thereto  $10$  means for varying the value of said angle of dip; and of said plurality of transcribed signals from said means all algundated of said plurality of sealine traces, include for<br>to produce to a respective one of the second inputs of said  $\frac{15}{2}$  summing the transcribed signal 5 said third signal exceeds a second predetermined value than the reflection time; first summing means for summing the transcribed signals of said transcribing stations: means for comparing the resulting sum with each of said transcribed signals; means for establishing an output signal<br>for each of said transcribed signals that is in phase with<br>said resulting sum; second summing means for summing the output signals to produce a coherence signal, the magnitude of the coherence signal being representative of the common information present in said transcribed signals; means for comparing the coherence signals corresponding to a plurality of values of said angle of dip to determine the proper value of said angle of dip for accurate time alignment of said plurality of seismic traces; means for produce corresponding to said proper value of said angle of dip to form a first signal; means for generating a sawtooth signal; means for summing said first signal and said sawtooth signal to form a second signal; means for sun ming said sawtooth signal and the inverse of said first signal to form a third signal; means for generating a pulse of uniform amplitude when said second signal ex ceeds a first predetermined value to form a fourth signal; means for generating a pulse of uniform amplitude when to form a fifth signal; means for dividing an individual corresponding to said proper value of said angle of dip into positive and negative components; means for mul-30 tiplying said fourth signal by said positive components to form a sixth signal; means for multiplying said fifth signal by said negative components to form a seventh signal; and means for summing said sixth and seventh signals.

 $\mathbf{U}$ 6. Apparatus for increasing the information available from a plurality of low signal-to-noise ratio seismic traces comprising, in combination, means for generating a me chanical analog of the seismic time triangle for each of said traces, said triangle comprising legs  $t<sub>h</sub>$ ,  $t<sub>r</sub>$ , and  $t<sub>n</sub>$ , where leg  $t<sub>h</sub>$  is the horizontal time from shotpoint to seismometer, leg  $t_r$  is the time from shot image to seismometer, and leg  $t_n$  is the normal time from shotpoint to shot image, a plurality of transcribing stations, one element of said analog being a stored record of the respective one of the said traces capable of being dynamically transcribed by a respective one of said plurality of transcribing stations, said one element corresponding to said leg  $t_r$  of said seismic time triangle; means for manipulating the analogs so that the length of the leg  $t_n$  of each of said analogs increases uniformly with time, this time starting from a time corresponding to shot instant when the legs  $t_r$  and  $t_h$  of said analog are coincident, the length of the leg  $t<sub>h</sub>$  of each of said analogs is proportional<br>to the shotpoint to seismometer distance and inversely proportional to the average velocity between shot image and seismometer, the angle between the leg  $t<sub>n</sub>$  and leg  $t<sub>n</sub>$ for each of said analogs is  $90^\circ$  plus the angle of dip of the horizon, and so that the length of the leg  $t_r$  of each of said analogs is such as to maintain each of said analog triangles closed; said transcribing stations during said manipulating being located on said stored records exter nal to the analog triangles, so that the resulting non-uni form motion of said stored records across said transcrib ing stations will cause the time of transcription of seismic events to be equivalent to the normal time rather than the reflection time; first summing means for summing the transcribed signals of said transcribing stations; means for comparing the resulting sum with each of said transcribed signals; means for establishing an output signal Scribed signals; means for establishing an output signal for each of said transcribed signals that is in phase with said resulting sum; second summing means for summing the output signals to produce a coherence signal, the magnitude of the coherence signal being representative

and means for comparing the coherence signals corre sponding to a plurality of values of said angle of dip to determine the proper value of said angle of dip for ac curate time alignment of said plurality of seismic traces; third summing means to sum a plurality of seismic signals to establish a first signal; means to apply to said third sum ming means as inputs thereto the transcribed signals from said means to produce which were produced as a function of said proper value of dip angle; fourth and fifth sum ming means; a sawtooth generator; means connecting the  $10$ output of said third summing means and the output of said generator to the inputs of said fourth summing means; a signal inverter; means connecting the output of said third summing means to an input of said fifth summing means through said signal inverter; means con- 15 necting the output of said generator to an input of said fifth summing means; first and second pulse width modu lators; means connecting the outputs of said fourth and fifth summing means to the inputs of said first and second ing means; means to divide a seismic signal into positive and negative components; means connecting the positive components output of said means to divide and the out put of said first modulator to the respective inputs of said first multiplying means, means connecting the negative components output of said means to divide and the output of said second modulator to the respective inputs of said second multiplying means; and means to sum the outputs of said first and second multiplying means.

outputs or said first and second multiplying means.<br>
7. A method for correcting the normal moveout of a 30 rality of low signal-to-noise ratio seismic signals.<br>
plurality of seismic traces, produced by a plurality of 9. Me seismometers, comprising generating a mechanical analog of the seismic time triangle for each of said traces, said triangle comprising legs  $t<sub>h</sub>$ ,  $t<sub>r</sub>$ , and  $t<sub>n</sub>$ , where leg  $t<sub>h</sub>$  is the horizontal time from shotpoint to seismometer, leg  $t_r$ is the time from shot image to seismometer, and leg  $t_n$ is the normal time from shot point to shot image, one element of said analog being a stored record of the respective one of said traces capable of being dynamically transcribed by a respective one of a plurality of transcribing stations, said one element corresponding to said leg  $t_r$  of said seismic time triangle; manipulating said analogs so that the length of the leg  $t_n$  of each of said analogs increases uniformly with time, this time starting from a time corresponding to shot instant when the legs  $t_{r-45}$ and  $t<sub>h</sub>$  of said analog are coincident, the length of the leg  $t<sub>h</sub>$  of each of said analogs is proportional to the shotpoint to seismometer distance and inversely proportional to the average velocity between shot image and seismom eter, the angle between the leg  $t<sub>h</sub>$  and leg  $t<sub>n</sub>$  for each of 50 said analogs is 90° plus the angle of dip of the horizon, and so that the length of the leg  $t_r$  of each of said analogs is such as to maintain each of said analog triangles closed; locating said transcribing stations on said stored records external to the analog triangles during said manipulating so that the resulting non-uniform motion of said stored records across said transcribing stations will cause the time of transcription of seismic events to be equivalent to the normal time rather than the reflection time, summing the transcribed signals of said transcribing stations, comparing the resulting sum with each of said transcribed signals, establishing an output signal for each of said transcribed signals that is in phase with said resulting sum, summing the output signals to produce a coherence signal, the magnitude of the coherence signal being represignal, the magnitude of the coherence signal being repre-<br>sentative of the common information present in said tran-<br>scribed signals, repeating the above procedure for a plurality of values of said angle of dip, and comparing the coherence signals corresponding to said plurality of values of said angle of dip to determine the proper value of said 70 angle of dip for accurate time alignment of said plurality of seismic traces.

8. A method for increasing the information available from a plurality of low signal-to-noise ratio seismic sig-

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5 20 respective transcribed signal is in phase with the sum of said plurality of transcribed signals; summing the output rality of low signal-to-noise ratio seismic signals on a respective one of a plurality of magnetic tapes; passing said magnetic tapes through a transcription zone to produce a plurality of transcribed signals with each of said transcribed signals being responsive to the signal stored on a respective one of said magnetic tapes and to the rate of movement of such respective one of said magnetic tapes through said transcription zone; varying the rate of movement of each of said magnetic tapes through said transcription Zone as a function of time, a predetermined dip angle and the ratio of the distance between the shotpoint and the seis mometer station at which the respective seismic signal was detected to the average velocity of the seismic wave; sum ming said plurality of transcribed signals from said transi tion zone; comparing each of said plurality of transcribed signals and producing an output signal corresponding to each of said plurality of transcribed signals when the respective transcribed signal is in phase with the sum of signals to produce a coherence signal, the magnitude of the coherence signal being representative of the common information present in said transcribed signals; repeating the above procedure for a plurality of values of said pre-<br>determined dip angle, and comparing the coherence sig-<br>nals corresponding to said plurality of values of said predetermined dip angle to determine the proper value of

9. Method for increasing the information available from a plurality of low signal-to-noise ratio seismic signals comprising, in combination; storing each of said plurality of low signal-to-noise ratio seismic signals on a respective one of a plurality of magnetic tapes; passing 35 said magnetic tapes through a transcription zone to produce a plurality of transcribed signals with each of said transcribed signals being responsive to the signal stored on a respective one of said magnetic tapes and to the rate said transcription zone; varying the rate of movement of each of said magnetic tapes through said transcription Zone as a function of time, a predetermined dip angle, and the ratio of the distance between the shotpoint and the seismometer station at which the respective seismic signal was detected to the average velocity of the seismic wave; summing the plurality of transcribed signals from said transcription Zone; comparing each of said plurality of scribed signals and producing an output signal corresponding to each of said plurality of transcribed signals when the respective transcribed signal is in phase with the sum of said plurality of transcribed signals; summing the out-<br>put signals to produce a coherence signal, the magnitude of the coherence signal being repesentative of the com-55 mon information present in said transcribed signals; re peating the above procedure for a plurality of values of said predetermined dip angle; comparing the coherence signals corresponding to said plurality of values of said predetermined dip angle to determine the proper value of 60 of low signal-to-noise ratio seismic signals; summing the transcribed signals from said transcription zone corre sponding to said proper value of said dip angle to form a first signal; generating a sawtooth signal; summing the said first signal and said sawtooth signal to form a second signal; summing said sawtooth signal and the inverse of said first signal to form a third signal; generating a pulse of uniform amplitude when said second signal exceeds a first predetermined value to form a fourth signal; generating a pulse of uniform amplitude when said third signal exceeds a second predetermined value to form a fifth<br>signal; dividing an individual one of said transcribed signals from said transcription zone corresponding to said Ifom a plurality of low signal-to-noise ratio seismic sig-<br>nals comprising, in combination; storing each of said plu- 75 proper value of said dip angle into positive and negative

**17** components; multiplying said fourth signal by said positive components to form a sixth signal; multiplying said fifth<br>signal by said negative components to form a seventh<br>signal; and summing said sixth and seventh signals.<br>10. A process for effecting the proper time alignment of<br>a

rality of seismic signals for a plurality of values of dip angle, summing the aligned signals corresponding to each of said values of dip angle to form composite signals, comparing the individual aligned signals corresponding to each<br>of said values of dip angle with the respective composite<br>signal and producing an output signal whenever an indi-<br>vidual aligned signal is in phase with the respe 5  $\overline{10}$ to each of said values of dip angle to form correlation 15

signals, and comparing said correlation signals to thereby<br>determine the proper value of dip angle.<br>11. A process for improving the reflection seismology<br>technique by increasing the readability of a plurality of<br>low signal example said plurality of values of said plurality of values of dip angle, summing the aligned signals corresponding to each of said values of dip angle to form composite signals, extra of said values of dip angle signals corresponding to each of said values of dip angle with the respective comeach of said values of dip angle with the respective com-<br>posite signal and producing an output signal whenever an<br>individual aligned signal is in phase with the respective<br>composite signal, summing the output signals corr

of the same polarity of said first signal.<br>12. A method for correcting the normal moveout of a<br>plurality of seismic traces produced by a plurality of seis-<br>mometers, comprising generating mechanical analog of the seismic time triangle for each of said traces, said tri-<br>angle comprisings legs  $t_h$ ,  $t_r$ , and  $t_h$ , where leg  $t_h$  is the<br>horizontal time from shot point to seismometer, leg  $t_r$  is the time from shot image to seismometer, and leg  $t_n$  is the normal time from shotpoint to shot image, one element of 40 18

30 formation present in said transcribed signals, repeating the said analog being a magnetic tape of one of said seismic traces capable of being dynamically transcribed by a re-<br>spective one of a plurality of transcribing stations located on said magnetic tape external to the analog triangle, said<br>one element corresponding to said leg  $t<sub>r</sub>$  of said seismic time triangle, and manipulating said analogs by affixing the initial time ends of said magnetic tapes to a constant speed transporting means so that the length of the  $t_n$  of each of said analogs increases uniformly with time, this each of said analogs increases uniformly with this, time starting from a time corresponding to shot means when the legs  $t_r$  and  $t_h$  of said analog are coincident, there<br>is generated a plurality of dimensions proportional to each<br>shotpoint to seismometer distance and inversely propor-<br>tional to said average velocity and said analogs is  $90^\circ$  plus the angle of dip of the horizon, so that the length of the leg  $t_r$  of each of said analogs is such as to maintain each of said analog triangles closed, and so that the resulting non-uniform motion of said magnetic tapes across said transcribing stations will cause the time of transcription of seismic events to be equivalent to the normal time rather than the reflection time, summing the transcribed signals from said transcribing stations,<br>comparing the resulting sum with each of said transcribed<br>signals, establishing an output signal for each of said tran-<br>scribed signals that is in phase with said re summing the output signals, the magnitude of the sum of said output signals being representative of the common information present in same state signals, repeating the sums of said angle of dip, and comparing the sums of the output signals corresponding to each of said values of said angle of dip to determine the proper value of said angle of dip.

## References Cited by the Examiner

### UNITED STATES PATENTS

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SAMUEL FEINBERG, Primary Examiner.

![](_page_14_Picture_200.jpeg)