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(54) APPLYING DIMENSIONAL REDUCTION TO SPECTRAL DATA FROM POLISHING **SUBSTRATES**

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Related U.S. Application Data

- (63) Continuation of application No. 14/063,917, filed on Oct. 25, 2013, now Pat. No. 9,551,567. (57) **ABSTRACT**
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52) U.S. CI.
CPC $B24B\,37/013$ (2013.01); $B24B\,49/12$ dimensions. (2013.01); H01L 21/30625 (2013.01); H01L 22/26 (2013.01)

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USPC 702/127, 155, 170, 172; 451/5, 6, 285, USPC 702 / 127 , 155 , 170 , 172 ; 451 / 5 , 6 , 285 , 451 / 287 See application file for complete search history .

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A plurality of spectra reflected from one or more substrates at a plurality of different positions on the one or more substrates are represented in the form of a first matrix, and the first matrix is decomposed into products of at least two component matrixes of a first set of component matrixes. The dimensions of each of the at least two component matrixes is reduced to produce a second set of component matrixes containing the at least two matrixes with reduced dimensions.

15 Claims, 9 Drawing Sheets

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FIG. 6

No. 14/063,917, filed on Apr. 30, 2015, incorporated herein by reference.

The present disclosure relates to reducing noise in spectral trum corresponding to the spectrum represented by a respectively a respectively to the first matrix. data from polishing substrates, e.g., for controlling chemical 15 tive single row or single column of the first matrix.

In another aspect, a computer program product resides on

In another aspect, a computer program produ

insulative layers on a silicon wafer. A variety of fabrication one or more computers, the first matrix into products of at
processes require planarization of a layer on the substrate. least two component matrixes of a firs processes require planarization of a layer on the substrate. least two component matrixes of a first set of component
For example, for certain applications, e.g., polishing of a matrixes; reduce dimensions of each of the a For example, for certain applications, e.g., polishing of a matrixes; reduce dimensions of each of the at least two
metal layer to form vias, plugs, and lines in the trenches of 25 component matrixes to produce a second se metal layer to form vias, plugs, and lines in the trenches of 25 component matrixes to produce a second set of component a patterned layer, an overlying layer is planarized until the matrixes containing the at least two ma a patterned layer, an overlying layer is planarized until the top surface of a patterned layer is exposed. In other appli-

imensions, and generate, by the one or more computers, a

cations, e.g., planarization of a dielectric layer for photoli-

second matrix by taking a product of cations, e.g., planarization of a dielectric layer for photoli-
the matrix by taking a product of the matrixes of the
thography, an overlying layer is polished until a desired second set of component matrixes. Each spectru

method of planarization. This planarization method typically outer layer of the one or more substrates has substantially the requires that the substrate be mounted on a carrier head. The same thickness at the plurality of requires that the substrate be mounted on a carrier head. The same thickness at the plurality of positions. The second exposed surface of the substrate is typically placed against matrix has the same dimensions as the firs exposed surface of the substrate is typically placed against matrix has the same dimensions as the first matrix. Each a rotating polishing pad. The carrier head provides a con- 35 single row or each single column of the se a rotating polishing pad. The carrier head provides a con- 35 single row or each single column of the second matrix trollable load on the substrate to push it against the polishing comprises a modified dataset representing trollable load on the substrate to push it against the polishing comprises a modified dataset representing a modified spec-
pad. A polishing liquid, such as slurry with abrasive par-
ticles, is typically supplied to the su

ing process is complete, i.e., whether a substrate layer has for execution by the processor using the memory. The been planarized to a desired flatness or thickness, or when a program comprises instructions configured to c been planarized to a desired flatness or thickness, or when a program comprises instructions configured to cause the desired amount of material has been removed. Variations in processor to: represent a plurality of spectra desired amount of material has been removed. Variations in processor to: represent a plurality of spectra reflected from
the initial thickness of the substrate layer, the slurry com-
one or more substrates at a plurality o the initial thickness of the substrate layer, the slurry com-
position, the polishing pad condition, the relative speed 45 the one or more substrates in the form of a first matrix; position, the polishing pad condition, the relative speed 45 the one or more substrates in the form of a first matrix;
between the polishing pad and the substrate, and the load on decompose, by one or more computers, the f between the polishing pad and the substrate, and the load on decompose, by one or more computers, the first matrix into
the substrate can cause variations in the material removal products of at least two component matrixes the substrate can cause variations in the material removal rate. These variations cause variations in the time needed to rate. These variations cause variations in the time needed to component matrixes; reduce dimensions of each of the at reach the polishing endpoint. Therefore, it may not be least two component matrixes to produce a second possible to determine the polishing endpoint merely as a 50

stand-alone metrology station. However, such systems often have limited throughput. In some systems, a substrate is optically monitored in-situ during polishing, e.g., through a 55 or a single column of the first matrix. The spectra are window in the polishing pad. However, existing optical reflected when an outer layer of the one or mo window in the polishing pad. However, existing optical reflected when an outer layer of the one or more substrates monitoring techniques may not satisfy increasing demands has substantially the same thickness at the plural monitoring techniques may not satisfy increasing demands of semiconductor device manufacturers.

senting a plurality of spectra reflected from one or more
substrates at a plurality of different positions on the one or
more substrates in the form of a first matrix; decomposing, 65 and/or the computer program products m by one or more computers, the first matrix into products of more of the following features. A characterizing value is at least two component matrixes of a first set of component generated, by the one or more computers, bas

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APPLYING DIMENSIONAL REDUCTION TO

SPECTRAL DATA FROM POLISHING

component matrixes to produce a second set of component **DATA FROM POLISHING** component matrixes to produce a second set of component **SUBSTRATES** containing the at least two matrixes with reduced matrixes containing the at least two matrixes with reduced dimensions; and generating, by the one or more computers, dimensions in the original cross - REFERENCE TO RELATED 5 a second matrix by taking a product of the matrixes of the original second set of component matrixes. Each spectrum is represecond set of component matrixes. Each spectrum is represented by a dataset arranged in a single row or a single column of the first matrix. The spectra is reflected when an This application is a continuation of U.S. application Ser. Column of the first matrix. The spectra is reflected when an $\frac{14}{0.63}$. The spectra is reflected when an $\frac{14}{0.63}$. The spectra is reflected when an $\$ same thickness at the plurality of positions. The second matrix has the same dimensions as the first matrix. Each single row or each single column of the second matrix TECHNICAL FIELD single row or each single column of the second matrix
comprises a modified dataset representing a modified spec-
losure relates to reducing noise in spectral trum corresponding to the spectrum represented b

a computer readable medium, and the computer program BACKGROUND product comprises instructions for causing a processor to: represent a plurality of spectra reflected from one or more substrates at a plurality of different positions on the one or An integrated circuit is typically formed on a substrate by 20 substrates at a plurality of different positions on the one or the sequential deposition of conductive, semiconductive, or more substrates in the form of a fir thickness remains over the underlying layer.

So sented by a dataset arranged in a single row or a single

Chemical mechanical polishing (CMP) is one accepted column of the first matrix. The spectra are reflected when an Chemical mechanical polishing (CMP) is one accepted column of the first matrix. The spectra are reflected when an ethod of planarization. This planarization method typically outer layer of the one or more substrates has su

least two component matrixes to produce a second set of component matrixes containing the at least two matrixes function of polishing time.
In some systems, a substrate is optically measured in a computers, a second matrix by taking a product of the In some systems, a substrate is optically measured in a computers, a second matrix by taking a product of the independent matrixes. Each independent matrixes are not all the second set of component matrixes. Each independe spectrum is represented by a dataset arranged in a single row
or a single column of the first matrix. The spectra are positions. The second matrix has the same dimensions as the first matrix. Each single row or each single column of the SUMMARY 60 second matrix comprises a modified dataset representing a modified spectrum corresponding to the spectrum repre In one aspect, a machine based method comprises repre-
sented by a respective single row or single column of the
senting a plurality of spectra reflected from one or more
first matrix.

generated, by the one or more computers, based on the

property of the one or more substrates. The characterizing from the light reflections and interferences of FIG. 5E, and value is the thickness of the outermost laver on the one or of calculated spectra for each individual value is the thickness of the outermost layer on the one or of calculated spectra for each individual light reflection and more substrates. Spectra reflected from one or more sub-
interference. strates at locations where the outer layer of the one or more 5 FIG. 5G shows a variety of factors that affect reflection substrates has different thicknesses are grouped into differ-
spectra and in connection with laye substrates has different thicknesses are grouped into differ-
ent groups. Each different group of spectra is to be repre-
substrate. ent groups. Each different group of spectra is to be repre-
substrate.
Sented by a first matrix. Decomposing the first matrix
comprises applying singular value decomposition, CUR
matrix approximation, and/or principal comp predetermined criteria. The predetermined criteria comprise
truncating the one or more columns and/or rows of the
disconsistent in the compression of the disconsistent of light reflected
disconsistent and the compression o diagonal matrix that correspond to one or more nonzero
measure is to measure a spectrum of light reflected
from a substrate, either in-situ during polishing or at an matrix elements having a value smaller than a predetermined from a substrate, either in-situ during polishing or at an perceptage of values of all nonzero matrix elements of the 20 in-line metrology station, and fit a func percentage of values of all nonzero matrix elements of the 20° in-line metrology station, and fit a function, e.g., an optical
diagonal matrix. The predetermined percentage is $\%$ or model, to the measured spectra. diagonal matrix. The predetermined percentage is % or model, to the measured spectra. Another technique is to bigher The dimensions are reduced based on predetermined compare the measured spectrum to a plurality of referen higher. The dimensions are reduced based on predetermined compare the measured spectrum to a plurality of reference
criteria. The predetermined criteria comprise the difference spectra from a library, and identify a best-m criteria. The predetermined criteria comprise the difference between the first and second matrixes being smaller than a ence spectrum.

predetermined value. Reducing dimensions of each of the at 25 Either fitting of the optical model or identification of the

least two component mat least two component matrixes comprises replacing all nonzero values of one or more columns or rows of matrix characterizing value, e.g., the thickness of the outermost elements with zeros. One of the at least two component layer. For the fitting, the thickness can be treated as matrixes is a diagonal matrix and reducing dimensions of the parameter of the optical model, and the fitting process
diagonal matrix comprises replacing non-zero values of one 30 generates a value for the thickness. For fi or more diagonal matrix elements with zeros. The spectra thickness value are measured with an in-line monitoring system before be identified. polishing of the substrate. The spectra are measured with an Chemical mechanical polishing can be used to planarize in-situ monitoring system during polishing of the substrate. the substrate until a predetermined thickness in-situ monitoring system during polishing of the substrate. the substrate until a predetermined thickness of the first layer
A polishing endpoint is determined for the substrate based 35 is removed, a predetermined thickn A polishing endpoint is determined for the substrate based 35 is removed, a predetermined thickness of the first on the characterizing value.

on the characterizing value.

Certain implementations may include one or more of the Generally, the measured spectrum contains noise data that

following advantages. Noise in a spectrum can be reduced. May affect the preci following advantages. Noise in a spectrum can be reduced. In may affect the precision of the characterizing value or the
Wafer thicknesses can be measured relatively precisely so included the measurement. The methods and s Wafer thicknesses can be measured relatively precisely so thickness measurement. The methods and systems of this that endpoints of polishing can be determined at a high 40 disclosure reduce the noise in the spectrum to imp that endpoints of polishing can be determined at a high 40 precision. Wafer-to-wafer thickness non-uniformity precision. Wafer-to-wafer thickness non-uniformity precision of thickness measurement, although precision of (WTWNU) may be reduced, and reliability of measurement of other properties can also be improved. The the endpoint system to detect a desired polishing endpoint may be improved.

FIG. 2 illustrates a schematic top view of a substrate so having multiple zones.

FIG. 4 illustrates a top view of a polishing pad and shows The polishing apparatus 100 can include a port 130 to locations where in-situ measurements are taken on a sub- 55 dispense polishing liquid 132, such as a slurry, onto the polishing pad 110. The polishing apparatus can also include

FIG. **5B** illustrates spectrum evolution as the thickness of state.

a substrate changes during polishing.

FIG. **5C** illustrates a schematic cross-sectional view of heads **140**. Each carrier head **140** is operable to hold

of light reflections and interferences in optical monitoring.

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second matrix. The characterizing value is associated with a FIG. 5F shows plots of an overall spectrum measured property of the one or more substrates. The characterizing from the light reflections and interferences of FI

substrate.

measurement of other properties can also be improved. The precisely determined thickness can be used to determine the endpoint of the chemical mechanical polishing and improve
45 the uniformity of the wafer thickness. the uniformity of the wafer thickness.

BRIEF DESCRIPTION OF THE DRAWINGS FIG. 1 illustrates an example of a polishing apparatus 100.
FIG. 1 illustrates a schematic cross-sectional view of an shaped platen 120 on which a polishing pad 110 is situated. example of a polishing station.
FIG. 2 illustrates a schematic top view of a substrate 50 example, a motor 121 can turn a drive shaft 124 to rotate the wing multiple zones.
FIG. 3 illustrates a schematic cross-sectional view of an polishing pad with an outer polishing layer 112 and a softer FIG. 3 illustrates a schematic cross-sectional view of an polishing pad with an outer polishing layer 112 and a softer example of an in-line monitoring station.

strate.
FIG. 5A illustrates a measured spectrum from the optical a polishing pad conditioner to abrade the polishing pad 110 FIG. 5A illustrates a measured spectrum from the optical a polishing pad conditioner to abrade the polishing pad 110 in a consistent abrasive to maintain the polishing pad 110 in a consistent abrasive onitoring system.
FIG. 5B illustrates spectrum evolution as the thickness of state.
She illustrates spectrum evolution as the thickness of state.

FIG. 5C illustrates a schematic cross-sectional view of heads 140. Each carrier head 140 is operable to hold a light reflections and interferences in optical monitoring. substrate 10, such as a wafer, against the polishing FIG. 5D illustrates a schematic plot of a part of a
measured spectrum and a modified spectrum with reduced polishing parameters, for example pressure, associated with polishing parameters, for example pressure, associated with noise.

FIG. 5E illustrates another schematic cross-sectional view retaining ring 142 to hold the substrate 10 in position on the retaining ring 142 to hold the substrate 10 in position on the polishing pad 110 .

structure 150, e.g., a carousel or a track, and is connected by 10. Moreover, if the monitoring station includes an XY a drive shaft 152 to a carrier head rotation motor 154 so that actuator system, the measurement spot 18 the carrier head can rotate about an axis 155. Optionally path with a plurality of evenly spaced parallel line segments.
each carrier head 140 can oscillate laterally, e.g., on sliders 5 This permits the optical metrology on the carousel 150; by rotational oscillation of the carousel measurements that are spaced in a rectangular pattern over itself, or by motion of a carriage 108 that supports the carrier the substrate.

125, and each carrier head is rotated about its central axis 10 160 can include a light source 162, a light detector 164, and 155 and translated laterally across the top surface of the circuitry 166 for sending and receivi

heads can be provided to hold additional substrates so that used to transmit the light from the light source 162 to the the surface area of polishing pad 110 may be used efficiently. 15 optical access in the polishing pad, the surface area of polishing pad 110 may be used efficiently. 15 optical access in the polishing pad, and to transmit light
Thus, the number of carrier head assemblies adapted to hold reflected from the substrate 10 to th Thus, the number of carrier head assemblies adapted to hold reflected from the substrate 10 to the detector 164. For substrates for a simultaneous polishing process can be example, a bifurcated optical fiber 170 can be use substrates for a simultaneous polishing process can be example, a bifurcated optical fiber 170 can be used to based, at least in part, on the surface area of the polishing transmit the light from the light source 162 to th based, at least in part, on the surface area of the polishing transmit the light from the light source 162 to the substrate pad 110.
10 and back to the detector 164. The bifurcated optical fiber

spectrographic monitoring system, which can be used to source 162 and detector 164, respectively. The probe 180 measure a spectrum of reflected light from a substrate can include the trunk end of the bifurcated optical fib undergoing polishing. An optical access through the polish-
ing pad is provided by including an aperture (i.e., a hole that 25 In one implementation, the white light emitted includes light

optical monitoring system making spectra measurements at 30 of FIG . 1) can be positioned between the light source 162 a sampling frequency will cause the spectra measurements and the substrate 10. A suitable light source is a xenon lamp to be taken at locations 201 in an arc that traverses the or a xenon mercury lamp.

ing apparatus includes an in-sequence optical monitoring 35 over a portion of the electromagnetic spectrum. A suitable system 160 having a probe 180 positioned between two spectrometer is a grating spectrometer. Typical output for a polishing stations or between a polishing station and a spectrometer is the intensity of the light as a func polishing stations or between a polishing station and a transfer station. The probe 180 of the in-sequence monitortransfer station. The probe 180 of the in-sequence monitor-
ing system 160 can be supported on a platform 106, and can spectrum, the spectrometer outputs the intensities of the

vertical height relative to the top surface of the platform 106. applying a single flash of light from a light source to the In some implementations, the probe 180 is supported on an substrate. In particular, spectrum 602 In some implementations, the probe 180 is supported on an actuator system 182 that is configured to move the probe 180 reflected from a product substrate. Spectrum 604 is mea-
laterally in a plane parallel to the plane of the track. The 45 sured from light reflected from a base s laterally in a plane parallel to the plane of the track. The 45 setuator system 182 can be an XY actuator system that actuator system 182 can be an XY actuator system that (which is a wafer that has only a silicon layer). Spectrum 606
includes two independent linear actuators to move probe 180 is from light received by the probe 180 when includes two independent linear actuators to move probe 180 is from light received by the probe 180 when there is no
independently along two orthogonal axes. In some imple-
substrate situated over the probe 180. Under this mentations, there is no actuator system 182, and the probe referred to in the present specification as a dark condition, 180 remains stationary (relative to the platform 106) while 50 the received light is typically ambien 180 remains stationary (relative to the platform 106) while 50 the received light is typically ambient light.
the carrier head 140 moves to cause the spot measured by the The computing device can process the above describe

over the substrate while the monitoring system take a reflected from the substrate 10 evolve as polishing pro-
sequence of spectra measurements, so that a plurality of 55 gresses. FIG. 5B provides an example of the evoluti sequence of spectra measurements, so that a plurality of 55 gresses. FIG. 5B provides an example of the evolution as spectra are measured at different positions on the substrate. polishing of a film of interest progresses. spectra are measured at different positions on the substrate. polishing of a film of interest progresses. The different lines
By proper selection of the path and the rate of spectra of spectrum represent different times in

180, which causes the spot 184 measured by the probe 180 determination is based can to traverse a spiral path 184 on the substrate 10. However, 65 reference spectrum, or both. other combinations of motion can cause the probe to traverse
As noted above, the light source 162 and light detector
other paths, e.g., a series of concentric circles or a series of 164 can be connected to a computing dev

Each carrier head 140 is suspended from a support arcuate segments passing through the center of the substrate structure 150, e.g., a carousel or a track, and is connected by 10. Moreover, if the monitoring station include actuator system, the measurement spot 184 can traverse a

head 140 along the track.
In operation, the platen is rotated about its central axis in-sequence embodiments, the optical monitoring system in-sequence embodiments, the optical monitoring system polishing pad.
While only one carrier head 140 is shown, more carrier 166 and light detector 164. One or more optical fibers can be While only one carrier head 140 is shown, more carrier 162 and light detector 164. One or more optical fibers can be heads can be provided to hold additional substrates so that used to transmit the light from the light sou d 110.
In some implementations, the polishing apparatus 20 an include a trunk 172 positioned in proximity to the optical In some implementations, the polishing apparatus 20 an include a trunk 172 positioned in proximity to the optical includes an in-situ optical monitoring system 160, e.g., a access, and two branches 174 and 176 connected t

runs through the pad) or a solid window 118. having wavelengths of 200-800 nanometers. In some imple-
Referring to FIG. 2, if the window 118 is installed in the mentations, the light source 162 generates unpolarized light. trated in FIG. 3, although it can be used in the in-situ system

substrate 10.
In some implementation, illustrated in FIG. 3, the polish-
eter is an optical instrument for measuring intensity of light
ght ing system 160 can be supported on a platform 106, and can spectrum, the spectrometer outputs the intensities of the be positioned on the path of the carrier head. 40 light at 200-500, e.g., 301, different wavelengths. FIG positioned on the path of the carrier head. 40 light at 200-500, e.g., 301, different wavelengths. FIG. 5A
The probe 180 can include a mechanism to adjust its shows an example of spectra reflected from the substrate by

be 180 to traverse a path on the substrate.

Referring to FIG. 4, the probe 180 can traverse a path 184 being limited to any particular theory, the spectra of light being limited to any particular theory, the spectra of light of spectrum represent different times in the polishing. As can measurement, the measurements can be made at a substan-
tially uniform density over the wafer. Alternatively, more
measurements can be made near the edge of the substrate. 60 spectrums are exhibited by particular thickness measurements can be made near the edge of the substrate. 60 spectrums are exhibited by particular thicknesses of the film.
In the specific implementation shown in FIG. 4, the The computing device can execute logic that det been reached. The one or more spectra on which an endpoint determination is based can include a target spectrum, a

164 can be connected to a computing device, e.g., the

controller 190, operable to control their operation and Referring again to FIG. 2, when multiple spectra are receive their signals. The computing device can include a measured at multiple locations 201 of the substrate dur microprocessor situated near the polishing apparatus, e.g., a one rotation of the polishing pad, each spectrum can be programmable computer. In operation, the controller 190 similarly presented by a matrix B. In some situa programmable computer. In operation, the controller 190 similarly presented by a matrix B. In some situations, the can receive, for example, a signal that carries information $\frac{1}{2}$ thicknesses measured at the multip can receive, for example, a signal that carries information $\frac{1}{5}$ thicknesses measured at the multiple locations 201 within describing a spectrum of the light received by the light the same rotation are substantially describing a spectrum of the light received by the light the same rotation are substantially the same. For example, detector for a particular flash of the light source or time detector for a particular flash of the light source or time frame of the detector.

information about a thickness 612 of an outer layer 650 of 10 the substrate 10. During polishing, the outer layer directly contacts the polishing pad 110 and its outer surface 614 is polished. The substrate 10 may have one or more additional layers 610 at the back of the outer layer 650 . When a flash of white light 620 is applied to the substrate 10, part of the 15 white light 620 reflects (622) at the outer surface 614 of the outer layer 650. Another part of the white light 620 penetrates the outer surface 614 and is at least partially reflected (624) by an inner surface 616 of the outer layer 650. Part of
the j_{jk} represents the light intensity at the kth wavelength
the light 620 may further penetrate the inner surface 624 and
be at least partially reflected by

Without wishing to be bound by any particular theory, it
is believed that the spectra data contains information about
the noise data contained in the spectra represented by the
the thickness(es) of one or more layers of t the thickness(es) of one or more layers of the substrate 10. 25 matrix A can be reduced using singular value decomposition
The values of the spectra, i.e., the light intensities may also (SVD), CUR matrix approximation, o coefficients of the substrate materials, and others. It is also thickness in this example, while filtering out noise compo-
believed that the light intensity in the spectrum 604 also 30 nents in the dataset, e.g., due to v believed that the light intensity in the spectrum 604 also 30 nents in the dataset, e.g., due to variations in the thickness contains information representing interferences between of an underlying layer. The techniques ca contains information representing interferences between of an underlying layer. The techniques can be used in the reflections, such as those between the reflections $624, 626$ or in-situ systems or the in-line systems. Th reflections, such as those between the reflections $624, 626$ or in-situ systems or the in-line systems. The techniques can
the reflections $622, 626$. The light intensity data may also also be used with other datasets, e the reflections 622 , 626 . The light intensity data may also also be used with o contain other noise data that originate from sources, such as $\frac{1}{2}$ library or data base. variation is the such a that originate from sources ϵ_{eq} , such as Singular Value Decomposition
dimensions of the device (e.g., critical 35 Singular Value Decomposition can be mathematically expressed as
dimensions a dimensions, sidewall angle, etc.), pad window variations The decomposition can be mathematically expressed as $\frac{1}{10}$ (e.g., changing absorption in the shorter wavelengths), other $A=U\Sigma V^T$ process influences (e.g., slurry pooling).
As an example, referring to FIG. 5E and 5F, an example

As an example, referring to FIG. 5E and 5F, an example where U and V are orthonormal matrixes, $U^T U = I$, and substrate 10 includes a stack of layers 902, 904, 906, 908, 40 $V^T V = I$, having m by p dimensions and n by p dim **910, 912, 914, 916**, with one or more layers containing one respectively, and Σ is diagonal and hasp by p dimensions.
or more structural features **918, 920, 922**, etc. When a flash Without wishing to be bound by theor of light is applied to an outer surface 924 of the substrate 10, each column of the U matrix and each row of the V^T matrix the light penetrates one or more layers 902, 904 and is represent a concept, such as differ reflected from multiple surfaces 924, 926, 928. The mea- 45 of interferences between different reflection light in the sured spectra 1000 shown in FIG. 5F can be a weighted thickness measurement. It is also believed that e sured spectra 1000 shown in FIG. 5F can be a weighted thickness measurement. It is also believed that each element combination of respective spectra 1002, 1004, 1006 associ-
of the U matrix represents location-to-concept s ated with the different reflections from the different surfaces.
 Δ the Σ matrix represents strength of each concept, and each
As shown in FIG. 5G, the factors that affect the measured
element of the V matrix repre spectra may include thickness variations of the layers in the 50 similarities.
substrate, the substrate material (which is Cu in this The U matrix can be written as:

example), diffractions due to Cu grating by patterning, light
scattering/interference at sidewalls, etc.
Reducing the noise of the spectrum 604 can allow the
thickness 612 of the outer layer 650 to be determined at a 55
w higher precision than the spectrum 604 that contains the noise data. As an example, FIG. 5D shows a spectrum 604 recording the output of the spectrometer. After the noise is reduced, the modified spectrum 642 shows a relatively smooth curve and retains the largest component of the 60 spectrum 604 representing the thickness of the outer layer

650.

Alternative to the plots shown in FIGS. 5A, 5B, and 5D,

a spectrum measured at one location of the substrate 10 can also be represented by a matrix: $B=(i_1, i_2, \ldots, i_n)$, where i_j 65 represents the light intensity at the jth wavelength of a total of n wavelengths. In an example, n can be 200-500, or 301.

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sured within the same rotation would be within 500 Ang-
stroms. Suppose that m locations are measured, the m Referring to FIGS. 5A and 5C, the spectra 602 contains stroms. Suppose that m locations are measured, the m
formation chart e this traces 512 of an outer layer 550 of the matrixes B can be combined to form the following m

element of the V matrix represents wavelength-to-concept similarities.

$$
u_i = \begin{pmatrix} u_{1i} \\ u_{2i} \\ \vdots \\ u_{mi} \end{pmatrix},
$$

i.e.,
$$
U = \begin{bmatrix} u_{11} & \cdots & u_{1p} \\ \vdots & \ddots & \vdots \\ u_{m1} & \cdots & u_{mp} \end{bmatrix}
$$

$$
V = (v_1, v_2, \dots, v_p),
$$

where

$$
v_i = \begin{pmatrix} v_{1i} \\ v_{2i} \\ \vdots \\ v_{ni} \end{pmatrix},
$$

i.e.,
$$
V^T = \begin{bmatrix} v_{11} & \dots & v_{n1} \\ \vdots & \ddots & \vdots \\ v_{1p} & \dots & v_{np} \end{bmatrix},
$$

and
the Σ matrix can be written as:

$$
\sum = (\sigma_1, \sigma_2, \dots, \sigma_n)
$$

where

$$
\sigma_i = \begin{pmatrix} 0 \\ \vdots \\ \sigma_{ii} \\ \vdots \\ 0 \end{pmatrix}.
$$

$$
4 = \sigma_1 u_1 v_1^T + \sigma_2 u_2 v_2^T + \ldots + \sigma_p u_p v_p^T
$$

$$
\Sigma_{i>t} |\sigma_{ii}|^2 \leq r^* \Sigma_i |\sigma_{ii}|^2,
$$

where t is an integer between 1 and p, and r is a predeter-

mined percentage, e.g., 60%, 70%, 80%, 90%, or higher. In

such implementations, those matrix element(s) σ_{ii} that are 45 (w_{k1} , w_{k2} , ..., w_{kp}) tha cance of the corresponding term $\Sigma_{i\geq t} \sigma_i u_i v_i^T$ in the matrix A,

In some implementations, for simplicity, a predetermined variance from the matrix $\frac{1}{10}$. A can be written as: number of non-zero diagonal elements of the Σ matrix is eliminated or selected to remain in the matrix. For example, 55 two diagonal elements having the smallest values are eliminated from the Σ matrix, or two diagonal elements having where W is the largest values are chosen to remain in the matrix while vectors of A^TA . To reduce the noise data in the matrix A, the all other diagonal elements are eliminated. Those rows and dimensions of the T and W matrixes all other diagonal elements are eliminated. Those rows and dimensions of the T and W matrixes can be reduced. In columns of the matrix that correspond to the eliminated ω_0 particular, instead of p principal components columns of the matrix that correspond to the eliminated 60 particular, instead of p principal components, a total of L diagonal elements can be eliminated to reduce the dimen-
principal components, with L being an integer diagonal elements can be eliminated to reduce the dimen-
sions of the L being an integer between 0 and
sions of the matrix. Alternatively, the values of the diagonal
p, can be kept such that the dimensions of the T matrix

dimensions, the V matrix is reduced to have n by t dimen-65 a matrix A can be reconstructed based on the \overline{T} and W sions, and the Σ matrix is reduced to have t by t dimensions. matrixes with reduced dimensions. The sions, and the Σ matrix is reduced to have t by t dimensions. matrixes with reduced dimensions. The constructed matrix This reduction in dimension could be accomplished by A can have all the major components that repre

the V matrix can be written as: $\frac{1}{2}$ actually removing rows and column from the matrices U and V, respectively, or by simply setting the appropriate diagonal values in the Σ matrix to zero. The matrix A is reconstructed by the matrixes with reduced dimensions to be approxi-
5 mately:

 $A \propto \sigma_1 u_1 v_1^T + \sigma_2 u_2 v_2^T + \dots + \sigma_i u_i v_i^T$,
where the large components of the matrix A remains in the
reconstructed matrix A. Each row of the reconstructed
 10 matrix A rangents a modified spectrum that corresponds to matrix A represents a modified spectrum that corresponds to a measured spectrum in the original matrix A . Relative to the measured spectrum, the modified spectrum contains a reduced amount of noise and can be used to calculate the thickness of the outermost layer of the substrate. Such thickness of the outermost layer of the substrate . Such | vip . . . Vap] calculated thicknesses are more precise than thicknesses calculated based on the original matrix A, because of the noise reduction.

Alternative or in addition to the criteria for dimension reduction discussed above, the difference between the origi-20 nal and the reconstructed matrixes can also be used. For example, the difference, $||\text{original A-reconstructed A }||^2$ is $= (\sigma_1, \sigma_2, \dots, \sigma_p),$ example, the difference, ||original A-reconstructed A ||⁻ is chosen to be smaller than a predetermined value so that the dimension reduction does not reduce the data in addition to the noise data, e.g., the data needed for calculating the thickness. 25 thickness.
CUR Matrix Approximation

In some implementations, alternative to the singular value decomposition, CUR matrix approximation can be used to decompose the original A matrix. The method can be selected based the properties of the A matrix, for example, For every matrix A, the decomposition is unique Also, the Σ how sparse the A matrix is, etc. Sometimes the CUR matrix is relatively matrix is arranged such that $\sigma_{11} \ge \sigma_{22} \ge \dots \ge \sigma_{pp}$. Accordingly, the matrix A ca

³⁵ Principal Component Analysis
Another alternative decomposition method is principal Following the decomposition, to reduce the noise data in
the A matrix, the dimensions of the U, Σ , and V^T matrixes are
effectively reduced. In some implementations, the values of
o_{if} decreases as i increases, such to lie on the first coordinate (called the first principal component), the second greatest variance on the second

correspond to the undesirable noise in the spectra. Accord-
ingly, these terms $\sum_{i> i} \sigma_i u_i v_i^T$ can be discarded.
In some implementations for simplicity a predetermined
late individual variables of t_i inherits the max

where W is a n-by-p matrix whose columns are the eigensions of the matrix. Alternatively, the values of the diagonal p, can be kept such that the dimensions of the T matrix is elements to be eliminated can be replaced with zero. reduced to mxL, and the dimensions of the W mat elements to be eliminated can be replaced with zero. reduced to mxL, and the dimensions of the W matrix is educed to have m by t reduced to nxL. Similar to the singular value decomposition, A can have all the major components that represent the

sis by I. T. Jolliffe (Springer; 2nd edition (Oct. 2, 2002)), the entire content of which is incorporated herein by reference.

used in processing measured spectra before the data is used FIG. 7 shows an example process 700 of implementing in calculating substrate thicknesses in an in-situ system or an 15 the noise reduction discussed above in cont in calculating substrate thicknesses in an in-situ system or an 15 in-line system. The noise reduction processes can be per-

spectra, e.g., light intensity data which typically is set for 20 monitoring system or an in-situ optical monitoring system.

one thickness measurement, or other data, are collected, or

Noise reduction is performed (703) library, datasets that contain information for a similar, e.g., may be sorted using a clustering algorithm such as the the same, thickness are binned (802) together. The datasets k-means clustering algorithm. The noise red binned together can be data for one wafer, e.g., collected for 25 performed on each cluster of spectra. An example of the a given rotation of the platen, or data for multiple wafers, noise reduction process is the process e.g., from a data library, that is associated with the similar or
the same thickness. The binned data can be stored in the (704) from the spectra with reduced noise. The characterthe same thickness. The binned data can be stored in the (704) from the spectra with reduced noise. The character-
form of a matrix, like the matrix A shown above. Optionally, izing values could be generated by identifying the binned data is further clustered (804) based on different 30 reference spectrum from a library of reference spectra, or by types of spectra for a given rotation and/or a given thickness fitting an optical model to the ing, the details of which are discussed in U.S. Patent polishing of the product substrate. For example, when the Publication No. 2015/0120242, the entire content of which characterizing values are thicknesses, the calculat Publication No. 2015/0120242, the entire content of which characterizing values are thicknesses, the calculated thick-
is incorporated herein by reference. The clustering may 35 nesses can be compared with a predetermined is incorporated herein by reference. The clustering may 35 further refine the binned datasets to facilitate precise thick-
 α determine the endpoint of the polishing process. In another

ness calculations. The clustered data for a given thickness

example, thicknesses at differ value can also be stored in the form of a matrix, such as the process can be determined and a polishing rate can be matrix A above. The matrix is then decomposed (806), using derived from the thicknesses. The thicknesses c singular value decomposition, principal component analysis, 40 or CUR matrix approximation, into component matrixes or CUR matrix approximation, into component matrixes noise reduction process. For example, the determined thick-
(e.g., U, Σ , and T matrixes in SVD, or T and W matrixes in nesses can be compared with directly measured (e.g., U , Σ , and T matrixes in SVD, or T and W matrixes in nesses can be compared with directly measured thicknesses PCA). The dimensions of the component matrixes are then to determine the effectiveness of the noise PCA). The dimensions of the component matrixes are then to determine the effectiveness of the noise reduction process reduced (808). The reduction can be done automatically and/or adjust the criteria. based on predetermined criteria. For example, in the 45 As used in the instant specification, the term substrate can example of SVD, the predetermined criteria can be whether include, for example, a product substrate (e.g. example of SVD, the predetermined criteria can be whether include, for example, a product substrate (e.g., which a percentage of the values of the matrix elements, starting includes multiple memory or processor dies), a te a percentage of the values of the matrix elements, starting includes multiple memory or processor dies), a test sub-
with the one having the highest index, in the Σ matrix is strate, a bare substrate, and a gating subs with the one having the highest index, in the Σ matrix is strate, a bare substrate, and a gating substrate. The substrate lower than a threshold percentage. An algorithm can be can be at various stages of integrated ci implemented such that when the percentage of the values of 50 the substrate can be a bare wafer, or it can include one or
those elements is lower than the threshold percentage, which more deposited and/or patterned layers. those elements is lower than the threshold percentage, which more deposited and/or patterned layers. The term substrate can be predetermined, columns and rows corresponding to can include circular disks and rectangular she those matrix elements are truncated from the matrix. The The above described polishing apparatus and methods can dimensions of U and V matrixes are reduced according to be applied in a variety of polishing systems. Either the reduction in the Σ matrix. Other criteria for dimension 55 reduction can also be used. A user may be enabled to enter reduction can also be used. A user may be enabled to enter provide relative motion between the polishing surface and or adjust the predetermined criteria, e.g., through a user the substrate. For example, the platen may orb or adjust the predetermined criteria, e.g., through a user the substrate. For example, the platen may orbit rather than interface. In some implementations, the dimension reduction rotate. The polishing pad can be a circula interface. In some implementations, the dimension reduction rotate. The polishing pad can be a circular (or some other can be manually performed by a user. The datasets, or the shape) pad secured to the platen. Some aspect spectra, are reconstructed (810) using the matrixes with the 60 reduced dimensions. The reconstructed datasets or spectra reduced dimensions. The reconstructed datasets or spectra ishing systems, e.g., where the polishing pad is a continuous contain a reduced amount of noise as compared to the initial or a reel-to-reel belt that moves linearl contain a reduced amount of noise as compared to the initial or a reel-to-reel belt that moves linearly. The polishing layer datasets or spectra.

or spectrum, the controller 190 can calculate a characterizing 65 value. The characterizing value is typically the thickness of the substrate 10, e.g., the thickness 612 of FIG. 5C, but can

thickness of the substrate, while a large portion of the noise be a related characteristic such as thickness removed. In data is removed as compared to the original matrix A. addition, although not discussed in detail abov ta is removed as compared to the original matrix A. addition, although not discussed in detail above, the char-
The PCA transformation can be mathematically associ-
acterizing value can be a physical property other than The PCA transformation can be mathematically associant acterizing value can be a physical property other than ated with the previously discussed singular value decompo-
thickness, e.g., metal line resistance. In addition, ated with the previously discussed singular value decompo-
sitions e.g., metal line resistance. In addition, the char-
sition, and the T matrix can be expressed as:
 $\frac{1}{5}$ acterizing value can be a more generic represen acterizing value can be a more generic representation of the progress of the substrate through the polishing process, e.g., T=UΣ.

Progress of the substrate through the polising process, e.g.,

an index value representing the time or number of platen

Details of the PCA are also discussed in Functional Data

rotations at which the spectrum wou Analysis by James Ramsay and B. W. Silverman (Springer; observed in a polishing process that follows a predetermined 2nd edition (Jul 1, 2005)), and Principal Component Analy- 10 progress. Details of techniques for calcula 2nd edition (Jul 1, 2005)), and Principal Component Analy - 10 progress. Details of techniques for calculating the characisis by I. T. Jolliffe (Springer; 2nd edition (Oct. 2, 2002)), the terizing value are discussed in U. tire content of which is incorporated herein by reference. U.S. Patent Publication No. 2014/0242878, the entire con-
The noise reduction processes discussed above can be tent of which is incorporated here by reference.

in-line system. The noise reduction processes can be per-
formed in real time during the polishing or be applied to data
the product substrate are collected (702) at a plurality of formed in real time during the polishing or be applied to data the product substrate are collected (702) at a plurality of from a database or a data library that has collected the data. different positions during one rotat from a database or a data library that has collected the data. different positions during one rotation of the platen. The An example process 800 is shown in FIG. 6. After the spectra could be measured using an in-sequence k-means clustering algorithm. The noise reduction can be performed on each cluster of spectra. An example of the izing values could be generated by identifying a matching derived from the thicknesses. The thicknesses can also be used to determine the criteria for dimension reduction in the

be applied in a variety of polishing systems. Either the polishing pad, or the carrier heads, or both can move to shape) pad secured to the platen. Some aspects of the endpoint detection system may be applicable to linear poldatasets or spectra.

Referring again to FIG. 1, for each reconstructed dataset fillers) polishing material, a soft material, or a fixed-abrasive fillers) polishing material, a soft material, or a fixed-abrasive material. Terms of relative positioning are used; it should be understood that the polishing surface and substrate can be held in a vertical orientation or some other orientation.

Although the description above has focused on control of circuit). For a system of one or more computers to be a chemical mechanical polishing system, the in-sequence "configured to" perform particular operations or action metrology station can be applicable to other types of sub-
strate processing systems, e.g., etching or deposition sys-
hardware, or a combination of them that in operation cause
tems.

tems.

Embodiments, such as noise reduction or controlling

substrate polishing, of the subject matter and the functional

operations described in this specification can be imple-

mented in digital electronic circuitry, i in this specification can be implemented as one or more general or special purpose microprocessors or both, or any
computer programs i.e. one or more modules of computer 15 other kind of central processing unit. Generally, computer programs, i.e., one or more modules of computer 15 other kind of central processing unit. Generally, a central
program instructions encoded on a tangible non transitory processing unit will receive instructions an program instructions encoded on a tangible non transitory processing unit will receive instructions and data from a read
storage medium for execution by or to control the operation only memory or a random access memory or storage medium for execution by, or to control the operation only memory or a random access memory or both. The
of data processing apparatus. Alternatively or in addition essential elements of a computer are a central proc of, data processing apparatus. Alternatively or in addition, essential elements of a computer are a central processing the program instructions can be encoded on an artificially unit for performing or executing instruction the program instructions can be encoded on an artificially unit for performing or executing instructions and one or
generated propagated signal, e.g., a machine-generated elec- 20 more memory devices for storing instructio generated propagated signal, e.g., a machine-generated elec- 20 more memory devices for storing instructions and data.
trical, optical, or electromagnetic signal, that is generated to Generally, a computer will also includ encode information for transmission to suitable receiver coupled to receive data from or transfer data to, or both, one apparatus for execution by a data processing apparatus. The or more mass storage devices for storing d apparatus for execution by a data processing apparatus. The or more mass storage devices for storing data, e.g., mag-
computer storage medium can be a machine-readable stor-netic, magneto optical disks, or optical disks. H age device, a machine-readable storage substrate, a random 25 computer need not have such devices. Moreover, a computer or serial access memory device, or a combination of one or can be embedded in another device, e.g., a

devices, and machines for processing data, including by way 30 bus (USB) flash drive, to name just a few.

of example a programmable digital processor, a digital Computer readable media suitable for storing computer

compu computer, or multiple digital processors or computers. The program instructions and data include all forms of non apparatus can also be or further include special purpose volatile memory, media and memory devices, includin apparatus can also be or further include special purpose volatile memory, media and memory devices, including by logic circuitry, e.g., an FPGA (field programmable gate vay of example semiconductor memory devices, e.g., array) or an ASIC (application specific integrated circuit). 35 EPROM, EEPROM, and flash memory devices; magnetic The apparatus can optionally include, in addition to hard disks, e.g., internal hard disks or removable disks; magneto ware, code that creates an execution environment for com-
optical disks; and CD ROM and DVD-ROM disks. ware, code that creates an execution environment for com-
puties and CD ROM and DVD-ROM disks. The
puter programs, e.g., code that constitutes processor firm-
processor and the memory can be supplemented by, or puter programs, e.g., code that constitutes processor firm-
ware, a protocol stack, a database management system, an incorporated in, special purpose logic circuitry. operating system, or a combination of one or more of them. 40 Control of the various systems and processes described in

module, a software module, a script, or code, can be written that are stored on one or more non-transitory machine-
in any form of programming language, including compiled readable storage media, and that are executable on or interpreted languages, or declarative or procedural lan-45 more processing devices. The systems described in this guages, and it can be deployed in any form, including as a specification, or portions of them, can be imp guages, and it can be deployed in any form, including as a stand alone program or as a module, component, subroutine, apparatus, method, or electronic system that may include or other unit suitable for use in a computing environment. A one or more processing devices and memory to computer program may, but need not, correspond to a file in able instruction a file system. A program can be stored in a portion of a file $\frac{1}{100}$ specification. that holds other programs or data, e.g., one or more scripts While this specification contains many specific implestored in a markup language document, in a single file mentation details, these should not be construed as l stored in a markup language document, in a single file mentation details, these should not be construed as limita-
dedicated to the program in question, or in multiple coor-
tions on the scope of any invention or on the sc dinated files, e.g., files that store one or more modules, sub may be claimed, but rather as descriptions of features that programs, or portions of code. A computer program can be 55 may be specific to particular embodimen programs, or portions of code. A computer program can be 55 may be specific to particular embodiments of particular deployed to be executed on one computer or on multiple inventions. Certain features that are described in deployed to be executed on one computer or on multiple computers that are located at one site or distributed across computers that are located at one site or distributed across fication in the context of separate embodiments can also be multiple sites and interconnected by a data communication in plemented in combination in a single emb

computers executing one or more computer programs to Moreover, although features may be described above as perform functions by operating on input data and generating acting in certain combinations and even initially claim perform functions by operating on input data and generating acting in certain combinations and even initially claimed as output. The processes and logic flows can also be performed such, one or more features from a claimed by, and apparatus can also be implemented as, special 65 purpose logic circuitry, e.g., an FPGA (field programmable gate array) or an ASIC (application specific integrated

"configured to" perform particular operations or actions

netic, magneto optical disks, or optical disks. However, a or serial access memory device, or a combination of one or can be embedded in another device, e.g., a mobile telephone,
a personal digital assistant (PDA), a mobile audio or video ore of them.
The term "data processing apparatus" refers to data pro-
player, a game console, a Global Positioning System (GPS) The term " data processing apparatus" refers to data pro-

cessing hardware and encompasses all kinds of apparatus, receiver, or a portable storage device, e.g., a universal serial receiver, or a portable storage device, e.g., a universal serial

A computer program, which may also be referred to or
this specification, or portions of them, can be implemented
described as a program, software, a software application, a
in a computer program product that includes instr readable storage media, and that are executable on one or more processing devices. The systems described in this one or more processing devices and memory to store executable instructions to perform the operations described in this

tions on the scope of any invention or on the scope of what implemented in combination in a single embodiment. Connetwork.
The processes and logic flows described in this specifi- ω a single embodiment can also be implemented in multiple The processes and logic flows described in this specifi- 60 a single embodiment can also be implemented in multiple cation can be performed by one or more programmable embodiments separately or in any suitable subcombinati such, one or more features from a claimed combination can in some cases be excised from the combination, and the claimed combination may be directed to a subcombination or variation of a subcombination.

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Similarly, while operations are depicted in the drawings in and the different groups have spectra reflected from regions a particular order, this should not be understood as requiring of the outer layer of the substrate th a particular order, this should not be understood as requiring of the outer layer of the substrate that have different thick-
that such operations be performed in the particular order nesses. shown or in sequential order, or that all illustrated operations $\frac{5}{2}$. The method of claim 1, wherein decomposing the first be performed, to achieve desirable results. In certain cir- $\frac{5}{2}$ matrix comprises applyi cumstances, multitasking and parallel processing may be applying CUR matrix approximation, or applying principal
advantageous. Moreover, the separation of various system component analysis.
modules and components in the em above should not be understood as requiring such separation a rotatable support to hold a polishing pad;
in all embodiments, and it should be understood that the 10 a carrier head to hold a substrate in contact with the in all embodiments, and it should be understood that the described program components and systems can generally polishing pad; be integrated together in a single software product or pack-
a motor to rotate the support;
aged into multiple software products.
an in-situ spectrographic moni

described. Other embodiments are within the scope of the the substrate during political following claims. For example, the actions recited in the a controller configured to following claims. For example, the actions recited in the claims can be performed in a different order and still achieve receive the multiplicity of spectra of light from the desirable results. As one example, the processes depicted in $\frac{1}{2}$ in-situ spectrographic monitoring the accompanying figures do not necessarily require the $_{20}$ collect, from the multiplicity of spectra, a plurality of particular order shown, or sequential order, to achieve spectra collected during a single rotation o

- polishing a substrate with a rotating polishing pad in a first matrix,
polishing system;
measuring a multiplicity of spectra of light reflected from component matrixes of a first set of component
- measuring a multiplicity of spectra of light reflected from
the substrate with an in-situ spectrographic monitoring 30
system, the multiplicity of spectra including a plurality
of spectra collected during a single rotation on the substrate, the plurality of spectra represented in reduced dimensions,
the form of a first matrix, each spectrum of the plurality 35 generate a second matrix by taking a product of the
- decomposing the first matrix into products of at least two first matrix, and each single row or each single component matrixes of a first set of component component matrixes of a first set of component matrix second matrix component and the second matrix component and model of the second matrix component and matrix component and matrix component and matrix component and matr
- matrixes containing the at least two matrixes with control the polishing system based on the second reduced dimensions;
- the second matrix comprising a modified dataset rep-

resenting a modified spectrum corresponding to the 50 8. The system of claim 7, wherein the controller is

spectrum represented by a respective single row or

configure
-

acterizing value being associated with a property of the the polishing pad and represented by a first matrix.

substrate, and controlling the polishing operation based on the polishing pad and represented by a first matrix

from the multiplicity of spectra into different groups, each and the different groups have spectra reflected from regions different group of spectra including a plurality of spectra of the outer layer of the substrate that collected during a single rotation of the polishing pad and nesses.
 11. The system of claim 6, wherein the controller is
 4. The method of claim 3, wherein the plurality of spectra 65 configured to decompose the first

4. The method of claim 3, wherein the plurality of spectra 65 within a group are reflected from regions of an outer layer of the substrate that have substantially the same thickness,

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-
-

- an in-situ spectrographic monitoring system configured to Particular embodiments of the subject matter have been $_{15}$ measure a multiplicity of spectra of light reflected from scribed. Other embodiments are within the scope of the substrate during polishing; and
	- -
- particular order shown, or sequential order, to achieve spectra collected during a single rotation of the desirable results. In some cases, multitasking and parallel processing may be advantageous.

The plurality of spectr What is claimed is:

1. A method of polishing comprising:

1. A method of polishing comprising:

1. A method of polishing comprising: 1. A method of polishing comprising: a substrate with a rotating polishing pad in a single row or a single column of the polishing a substrate with a rotating polishing pad in a set of first matrix,
	-
	-
	- of spectra being represented by a dataset arranged in a matrixes of the second set of component matrixes, single row or a single column of the first matrix; the second matrix having the same dimensions as the secomposing t matrixes;
reducing dimensions of each of the at least two compo-
sponding to the spectrum represented by a respective ducing dimensions of each of the at least two compo-
neutral spectrum represented by a respective
neutral ratrixes to produce a second set of component
neutral single row or single column of the first matrix, and nent matrixes to produce a second set of component single row or single column of the first matrix, and matrixes containing the at least two matrixes with control the polishing system based on the second

generating a second matrix by taking a product of the 45 7. The system of claim 6, wherein the controller is matrixes of the second set of component matrixes, the configured to generate a characterizing value based on the matrixes of the second set of component matrixes, the configured to generate a characterizing value based on the second matrix having the same dimensions as the first second matrix, the characterizing value being associate second matrix having the same dimensions as the first second matrix, the characterizing value being associated matrix, and each single row or each single column of with a property of the substrate, and to control the polis with a property of the substrate, and to control the polishing

configured to determine a polishing endpoint for the substrate based on the characterizing value.

single column of the first matrix; and strate based on the characterizing value.

strate based on the second strate based on the controller is

configured to group spectra from the multiplicity of spectra
 $\frac{1}{2}$. The 2. The method of claim 1, comprising generating a 55 into different groups, each different group of spectra includ-
characterizing value based on the second matrix, the char-
ing a plurality of spectra collected during a s ing a plurality of spectra collected during a single rotation of

gular value decomposition, CUR matrix approximation, or principal component analysis.

12. The system of claim 6, wherein the controller is configured to reduce dimensions of each of the at least two component matrixes by to i) truncate one or more columns and/or one or more rows of each of the at least two component matrixes, or ii) replace all non-zero values of one 5
or more columns or rows of matrix elements with zeros.

13. The system of claim 12, wherein the controller is configured to truncate or replace non - zero values of one or more columns or rows in which nonzero matrix elements have a value smaller than a predetermined percentage of 10 values of all nonzero matrix elements of the diagonal matrix.

14. The system of claim 13, wherein the predetermined
percentage is 80% or higher.
15. The system of claim 12, wherein the controller is

configured to truncate or replace non-zero values of columns 15 or rows by eliminating or retaining a predetermined number

of columns or rows . * * * * *