

(12) United States Patent

Zach

(54) OBJECT POSE RECOGNITION (56) References Cited

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(57) ABSTRACT

A method for use in estimating a pose of an imaged object comprises identifying candidate elements of an atlas that correspond to pixels in an image of the object, forming pairs of candidate elements , and comparing the distance between the members of each pair and with the distance between the corresponding pixels .

15 Claims, 8 Drawing Sheets

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Fig. 3

Fig. 6

 $Fig. 7$

a pose of an imaged object. In particular, but without representing a scene in three spatial dimensions. The image-
limitation, this disclosure relates to a method for use in acquiring device 101 is coupled, physically and limitation, this disclosure relates to a method for use in acquiring device 101 is coupled, physically and/or wire-
estimating a nose of an imaged object based on depth lessly, to a processing device 103 , which is arr estimating a pose of an imaged object based on depth

tifying objects in images or videos, while the task of pose instructions as may be provided to the processing device 103
estimation involves estimating the pose of objects which 15 via one or more of: a network interface 2 estimation involves estimating the pose of objects which ¹⁵ via one or more of: a network interface 228 arranged to have been recognised. Object recognition and nose estimation and the microprocessor 220 to communicate w have been recognised. Object recognition and pose estima enable the microprocessor 220 to communicate with a
tion are challenging problems for commuter vision algo-
communications network such as the internet; input/output tion are challenging problems for computer vision algo communications network such as the internet; input output
rithms especially when objects are partially occluded means 222 which may be arranged, without limitation, to rithms, especially when objects are partially occluded. means 222 which may be arranged, without limitation, to
Object recognition and nose estimation may be attempted interface with: floppy disks, compact discs, USB stick Object recognition and pose estimation may be attempted
using colour images or alternatively in situations where 20 or more keyboards, and/or one or more computer mice; and using colour images, or alternatively, in situations where 20 or more keyboards, and/or one or more computer mice; and colour cuse are not available or are unreliable may be a memory 224, for example a random access memory colour cues are not available or are unreliable, may be attempted using only depth information.

Aspects and features of the invention are set out in the appended claims.

FIG. 3 shows an illustration of potential correspondences between an image and an atlas;

FIG. 7 shows further exemplary results of a method described herein; and

Throughout the description and the drawings, like reference numerals refer to like parts.

FIG. 1 illustrates a system for use in acquiring an image identified in an atlas 315 of one or more candidate objects.

of an object 102 (henceforth 'an imaged object'). Examples The atlas 315 of one or more candidate obje of imaged objects include: in a gesture recognition applica- 55 a representation of each candidate object. The representation tion, a hand or a part thereof; in an infrastructure inspection of each candidate object may be tion, a hand or a part thereof; in an infrastructure inspection application, a building block or a part thereof, or a building

image representing, in three spatial dimensions, a scene absence of the object and/or the surface of the object), or a including the imaged object 102. The image-acquiring geometric model of the object (for example as may including the imaged object 102. The image-acquiring geometric model of the object (for example as may be device 101 may be any kind of device that is capable of mathematically defined or determined using Computeracquiring an image containing data about the depth of an Aided Design (CAD) software).

image point with respect to the image acquiring device 101. 65 Candidate locations are identified for each image element

Examples of time-of-flight camera, a structured-light 3D scanner (such as element, the descriptor representing the local geometry in

OBJECT POSE RECOGNITION a Microsoft Kinect device), an ultrasound distance measurer, a laser rangefinder, a LiDAR device, and a shape from X apparatus, such as a shape from (passive) stereo apparatus apparatus, such as a shape from (passive) stereo apparatus and/or a shape from shading apparatus. Further, the approaches described herein may be applied to any image This disclosure relates to a method for use in estimating 5 approaches described herein may be applied to any image
nose of an imaged object. In particular, but without representing a scene in three spatial dimensions. The examining a pose of an imaged object sased on depth process images acquired by the image acquiring device 101

10 in order to estimate a pose of the imaged object 102.
FIG. 2 shows an exemplary block diagram of a processing BACKGROUND FIG. 2 shows an exemplary block diagram of a processing
device 103. The processing device 103 comprises a micro-
recognition involves finding and iden-
processor 220 arranged to execute computer-readable The task of object recognition involves finding and iden-
ving objects in images or videos, while the task of nose instructions as may be provided to the processing device 103 is arranged to be able to retrieve, store, and provide to the microprocessor 220, instructions and data that have been SUMMARY stored in the memory 224. The microprocessor 220 may
25 further be coupled to a monitor 226 upon which a user further be coupled to a monitor 226 upon which a user interface may be displayed and further upon which the results of processing operations may be presented. The microprocessor 220 may also or alternatively communicate those results to another device via the network interface 228. BRIEF DESCRIPTION OF THE DRAWINGS
Examples of the present disclosure will now be explained
with reference to the accompanying drawings in which:
FIG. 1 shows a system for use in acquiring an image of also be used to execut

an object;

FIG. 2 shows an exemplary block diagram of a processing 35 A method for use in estimating a pose of the imaged

device for use in implementing the steps of the methods object 102 will now be explained with refe tween an image and an atlas; show, in first and second consecutive parts, a flowchart of FIGS. 4 and 5 show, in two consecutive parts, a flow chart 40 the steps of the method.

of the steps of a method described herein;
FIG. 6 shows exemplary results of a method described
herein:
 $\frac{1}{2}$ The image represents, in three spatial dimensions, a scene
herein:
 $\frac{1}{2}$ The image represents, in three including the imaged object 102 (which may be partially occluded due to another object, or objects, being in between $\frac{45 \text{ m}}{45 \text{ m}}$ and $\frac{45 \text{ m}}{45 \text{ m}}$ and the image acquiring device 101). The FIG. 8 shows performance results of a method described image 301 is made up of image elements, e.g., 305, 306, 307, herein.
Throughout the description and the drawings, like refer-
sities of which represent distances at the time of acquisition
Intensity of the respective intensity of the time of acquisition of the image 301 between the image acquiring device 101 50 and the various components of the scene .

DETAILED DESCRIPTION At step S200, for each of at least a subset of the image elements, one or more corresponding candidate locations are identified in an atlas 315 of one or more candidate objects.

three-dimensional representation of the object (such as a or a part thereof; and in an obstacle avoidance application, depth map or laser scan), a volumetric 3D representation of a hazard or an obstacle. hazard or an obstacle.
An image-acquiring device 101 is arranged to acquire an 60 elements of which having values indicative of presence or An image-acquiring device 101 is arranged to acquire an 60 elements of which having values indicative of presence or image representing, in three spatial dimensions, a scene absence of the object and/or the surface of the

atlas. When matching a descriptor associated with the image At step S600, the distances between pairs of image element to a descriptor associated with a candidate location, 5 elements in image space and between the corresp element to a descriptor associated with a candidate location, \bar{s} elements in image space and between the corresponding a matching score may be assigned, said score quantifying the pairs of candidate locations in atlas

positions around an image element, a descriptor is formed by candidate locations 310 and 312, and the distance d_i is also listing those positions and creating a string (for example a 10 compared with the distance d_i b listing those positions and creating a string (for example a 10 binary occupancy string) wherein each element of the string didate locations 311 and 312.
corresponds to one of the listed positions and has a first If the distance between a pair of image elements and the value (i.e. a 1) if the image elements of the image indicate distance between a pair of corresponding candidate locations that that spatial position is behind the imaged scene or a are dissimilar, then the pair of candidate locations is not second value (i.e. a 0) if the image elements of the image 15 likely to actually correspond to the pair indicate that that spatial position is in front of the imaged and a low compatibility score may be assigned to the pair of scene. In practice, this may be achieved by working out a corresponding candidate locations. For ex surface normal at a given image element based on adjacent locations 311 and 312 are less likely to correspond to image image element values and then defining positions in relation elements 306 and 307 than candidate locati image element values and then defining positions in relation elements 306 and 307 than candidate locations 310 and 312, to the normal—for example at a set distance centred upon 20 as distance d_a is further from d_i tha

moments to describe local shape geometry could be used 25 the image space distance and/or descriptors designed for intensity images (e.g. SURF be derived therefrom. and shape context). These descriptors model local gradient Steps S300 to S600 of the above-described method are statistics. Generally, descriptors can be described as vectors performed for at least two different pairs of i statistics. Generally, descriptors can be described as vectors performed for at least two different pairs of image elements in Rⁿ. The matching of two descriptors is performed by and steps S300-S600 for any of those pair determining the Hamming distance between the two strings, 30 elements steps may be performed in parallel, sequentially, or and determining that the Hamming distance is below a a mixture thereof with steps S300-S600 of any other of the threshold. The Hamming distance may directly be used as a pairs of image elements. An effect of this is to eas threshold. The Hamming distance may directly be used as a pairs of image elements. An effect of this is to easily enable matching score. As other possibilities, (normalized) cross the approach to be performed in parallel a matching score. As other possibilities, (normalized) cross the approach to be performed in parallel and therefore correlation, and/or the squared or non-squared Euclidean quickly.

identified as corresponding to image element 306; for image scores of step S600.

element 307, two candidate locations 310, 312 on the At step S700, at least one triplet of candidate locations is candidate object 313 are identified as corresponding to 40 formed by selecting two pairs of candidate locations that image element 307; and for image element 308, candidate have a candidate location in common. For example, image element 307; and for image element 308, candidate have a candidate location in common. For example, a triplet location 311 on the candidate object 313 is identified as corresponding to image element 308. This first p

307) is formed/selected from the image elements for which 45 of candidate locations (310,311) corresponding to the pair of step S200 has been performed. As at least one corresponding image elements (306,308). Preferably, a candidate location will have been identified for each of the selected if the three candidate locations that constitute it lie image elements for which step S200 has been performed, for on a straight line (i.e. are collinea each pair of image elements, at least two (a pair of) not enable reliable pose determination.

corresponding candidate locations will have been identified 50 At step S800, a subset of triplets of candidate locations is

in $(306, 307)$, the pair of corresponding candidate locations $(310, 312)$ and also the pair of corresponding candidate (310, 312) and also the pair of corresponding candidate locations of each triplet, and optionally also based on the locations (311, 312) will have been identified. The matching scores of the individual candidate locations

determined. For example, a distance d_i between a first image in the could be added so as to give an overall compatibility element 306 and a second image element 307 is determined.
In the case where the image is a depth image space) between pairs of image elements are deter- 60 subset of the triplets is selected based on the ranking. As one mined by back-projecting the image elements using the example, a belief propagation approach is use mined by back-projecting the image elements using the depth information contained in the image 301.

At step S500, distances (in atlas space) between each of scores for the parts (matching scores and compatibility the pairs of candidate locations are calculated. For example, ones). as the pair of candidate locations (310,312) correspond to 65 At step S900, for each triplet in the subset of triplets, steps
the pair of image elements (306,307), a distance d_a between S900a to S900a are performed. As

the vicinity of that image element. The descriptor associated tion 312 is determined, and a distance d_a ¹ between the pair with the image element is matched to one or more descrip-
tors associated with potential candid

a matching score may be assigned, said score quantifying the pairs of candidate locations in atlas space are compared. For example, the distance d, between image elements 306 and milarity between the two descriptors.
As one possibility, for a number of predefined spatial 307 is compared with the distance d_a between corresponding

corresponding candidate locations. For example, candidate

for the atlas in a corresponding manner.
As other possibility, the corresponding candidate locations. As one possibility, the As other possibilities, descriptors that use higher-order pairwise compatibility score may be th pairwise compatibility score may be the difference between the image space distance and the atlas space distance or may

and steps S300-S600 for any of those pairs of image

distance may be used to compare descriptors.

In the example of FIG. 3, for image element 306, two S700 of FIG. 5. The optional steps outlined in FIG. 5 enable

candidate locations 310, 311 on a candidate object 313 are a

rresponding to image element 308. first pair of candidate locations (310,312) corresponding to
At step S300, at least one pair of image elements (306, the pair of image elements (306,307) and from a second pair image elements (306,308). Preferably, a triplet will not be on a straight line (i.e. are collinear) as such a triplet would

selected from the at least one triplet of candidate locations based on the compatibility scores of the pairs of candidate matching scores of the individual candidate locations forming of each triplet. For example, the compatibility scores of At step S400, for each of the pairs of image elements, a 55 ing of each triplet. For example, the compatibility scores of distance between the image elements forming that pair is the two pairs of candidate locations that m to their compatibility scores and/or matching scores, and a subset of the triplets is selected based on the ranking. As one pth information contained in the image 301. Whole configuration of predicted matches based on the At step S500, distances (in atlas space) between each of scores for the parts (matching scores and compatibility

points is sufficient to uniquely define the spatial pose of a

example a rigid transformation matrix) for the imaged object 102 is computed based on the triplet. At step S900*b*, the approaches disclosed herein.
candidate object 313 (as defined by the atlas 315) is trans-
formed by the initial pose estimate and the transformed 5 out using colou formed by the initial pose estimate and the transformed $\frac{5}{5}$ candidate object is used to create an estimated image representative of an image of the imaged object that would be $\frac{0 \text{mJy}}{1 \text{mJy}}$ and $\frac{0 \text{mJy}}{1 \text{mJy}}$ at also

At step S900d, a refined pose estimate for the triplet, obstacle/hazardous object avoidance (for example by rec-
based on the comparison of step S900c, is determined. As oppizing dangerous objects): 3D gesture recognition based on the comparison of step S900c, is determined. As ognizing dangerous objects); 3D gesture recognition (for one example, a searching approach is employed by repeat-
example by recognizing hand templates in different one example, a searching approach is employed by repeat-
example by recognizing hand templates in different poses);
edly varying the initial pose estimate and determining $_{20}$ rapid 3D modelling (for example by recogniz edly varying the initial pose estimate and determining 20 rapid 3D modelling (for example by recognizing 3D build-
whether an evaluation of an estimated image that is created ing blocks (pipes, cubes, boxes) and storing ge according to the varied pose estimate is better or worse than relationships between them—which can be used to modify

selected, based on the scores of the refined pose estimates, 25 samples (i.e. image elements) that are contaminated by
as being representative of the true pose of the object. The qualitiers via message passing. The approac as being representative of the true pose of the object. The outliers via message passing. The approaches take into selected refined pose estimate can then be used in a variety account that objects projected into images con selected refined pose estimate can then be used in a variety of applications.

Examples of the described approaches are set out in the

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There is described herein a method for use in estimating 45 computation and is available in the next step.
a pose of an imaged object that comprises identifying All triplets of 3 nearby pixels in the depth image are
candid candidate elements of an atlas that correspond to pixels in an considered as sample set, and initially ranked and image of the object, forming pairs of candidate elements, discarded based on the computed messages. The topimage of the object, forming pairs of candidate elements, discarded based on the computed messages. The top-
and comparing the distance between the members of each ranked sample sets are evaluated using a more expenand comparing the distance between the members of each ranked sample sets are evaluated pair and with the distance between the corresponding pixels. 50 sive geometric fitting energy.

As one possibility, the approach described with reference The approaches described herein have been found to work to FIGS. 4 and 5 may perform steps S300 to S600 for only with objects that have a non-discriminative 3d shap to FIGS. 4 and 5 may perform steps S300 to S600 for only with objects that have a non-discriminative 3d shape. Fur-
a single pair of image elements so as to enable a determi-
thermore, the approaches do not need RGB images a single pair of image elements so as to enable a determi-
thermore, the approaches do not need RGB images in
nation of the suitability of candidate locations based on addition to depth data, and they can be easily impleme

ments and candidate locations are necessary in order to determine a pose estimate, the approaches described herein need not be limited to triplets of candidate locations for 60 example the triplets of candidate locations may be replaced with sets of candidate locations comprising more than two able medium carrying computer readable instructions pairs of candidate locations—preferably having one candi-
arranged for execution upon a processor so as to make the

Although the image 301 may have been The term computer readable medium as used herein refers obtained by downsampling an image obtained from an to any medium that stores data and/or instructions for obtained by downsampling an image obtained from an

6

candidate object, at step S900a, an initial pose estimate (for image-acquiring device 101 so as to reduce its resolution example a rigid transformation matrix) for the imaged object and thereby reduce the computational com

ing to the imaged object 102, and may be performed based only on an image 301 of an imaged object along with an

the virtual object later). acquired by the image-acquiring device 101 if the candidate atlas. Potential applications of the approaches described herein equivalent to the initial pose estimate. At step S900c, the estimated image is compared to the At step S900c, the estimated image is compared to the ¹⁰ include: robotic arms and autonomous robots (for example,
limage 301 representing the scene including the imaged
object 102 so as to produce a score for that estim measure such as: Sum of Squared Differences, Cross Cor- $\frac{15}{15}$ infrastructure inspection (for example by comparing a relation, Normalised Mutual Information, etc. lation, Normalised Mutual Information, etc.
At step S900d, a refined pose estimate for the triplet, abstacle/hazardous object avoidance (for example by rec-

a previous such evaluation for that triplet.

At step S1000, one of the refined pose estimates is The approaches described here quickly filter random

Selected based on the scores of the refined pose estimates 25 samples (contiguous region in the image, therefore using matches from spatially close pixels in the depth image is beneficial. below list of numbered clauses:

1. A method of recognizing and estimating the pose of an

³⁰ Due to the large number of outliers among the hypothesized

³⁰ Due to the large number of outliers among the hypothesized

 of the companies of the companies and community included to the companies of a scene depicting
the object given a single depth image of a scene depicting
2. A method that quickly discards incorrect detections of
the object

- predictions and depth data.

3. A method to rank object and pose predictions using

inference via local message passing (belief propaga-

tion).

4. A method to efficiently sample promising sets of

⁴⁰ propaga-

⁴⁰ pro
- A method to efficiently sample promising sets of pairwise compatibility between predictions is computative correspondences. puted. For any sample set that contains predictions 5. A method that estimates an object's pose by detecting from this edge the likelihood of this sample being parts of the object in order to handle occlusions.
	-

distance comparisons for the first and second image ele- 55 in data-parallel architectures (multi-core CPUs, GPUs),
ments of that pair of image elements.
Although only three correspondences between image ele-
ments and can including hardware, firmware, and/or software, for example
on a computer readable medium, which may be a nontransitory computer readable medium. The computer readdate location in common. processor carry out any or all of the methods described Although the image 301 may be received directly from an 65 herein.

causing a processor to operate in a specific manner. Such a (i) few salient regions in range images, (ii) unreliable depth storage medium may comprise non-volatile media and/or discontinuities, and (iii) uninformative feat volatile media. Non-volatile media may include, for tors.

example, optical or magnetic disks. Volatile media may Since depth cameras report 3D geometry, and approaches

include dynamic memory. Exemplary forms of storage 5 medium include, a floppy disk, a flexible disk, a hard disk, a solid state drive, a magnetic tape, any other magnetic data a solid state drive, a magnetic tape, any other magnetic data of putative object coordinates may be assessed by compar-
storage medium, a CD-ROM, any other optical data storage ing the distance between two observed 3D poin storage medium, a CD-ROM, any other optical data storage ing the distance between two observed 3D points (back-
medium, any physical medium with one or more patterns of projected from the depth map) and the one between pre medium, any physical medium with one or more patterns of projected from the depth map) and the one between pre-
holes or protrusions, a RAM, a PROM, an EPROM, a 10 dicted object coordinates. Grossly deviating distances holes or protrusions, a RAM, a PROM, an EPROM, a 10 dicted object coordinates. Grossly deviating distances FLASH-EPROM, NVRAM, and any other memory chip or indicate that at least one of the predicted object coordinates

set out below. mal sample sets by scoring this (pairwise) consistency
Object Pose Recognition
Joint object recognition and pose estimation solely from The inventor has arrived at the insight that if one inter-
range images range images is an important task e.g. in robotics applica-
tions and in automated manufacturing environments. The (or latent) states, then the pairwise consistency of predicted lack of colour information and limitations of current com-
modity depth sensors make this task a challenging computer 20 graphical model, and that, consequently, the methodology of modity depth sensors make this task a challenging computer 20 vision problem, and a standard random sampling based approach is time-consuming. This difficult problem may be
addressed by generating promising inlier sets for pose
estimation by early rejection of clear outliers with the help
uses of graphical models with respect to images estimation by early rejection of clear outliers with the help uses of graphical models with respect to images, where a of local belief propagation (or dynamic programming). By 25 random field is defined over the entire ima

In contrast to colour images, depth maps are usually far Robust geometric estimation is typically addressed by less discriminative in their appearance particularly for local 30 data - driven random sampling in computer vision . A standard depth image patches. A sensible and simple prior for depth top-down RANSAC-type approach for rigid object pose images is given by a piecewise smooth regularizer. Conse-
quently, interest point detection in depth images is not
hypotheses (not necessarily using a uniform distribution) quently, interest point detection in depth images is not hypotheses (not necessarily using a uniform distribution) necessary and features are evaluated densely (or quasi-
and evaluate the induced pose with respect to the g densely by subsampling) in the query image. Further, real 35 On a high level view RANSAC generates a large number of depth sensors exhibit several shortcomings at depth discon-
pose hypotheses and subsequently ranks these. tinuities, such as half-occlusions and foreground fattening described herein can be employed in a bottom-up manner, occurring with triangulation-based sensors (passive stereo or that is, by reversing the direction of compu flight sensors. Overall, many depth sensing technologies 40 report reliable and accurate depth values only in smooth utilizing the consistency criterion. Since the minimal sets are regions of the true scene geometry. Beside that, the piece- overlapping, applying the consistency cri wise smooth appearance of range images also implies that putative correspondences enables several minimal sample extracting a full 3D local coordinate frame is not repeatable, sets to be discarded at once. This is an elegant solution to but at least estimating surface normals is rather reliable. 45 generate promising sample sets for but at least estimating surface normals is rather reliable. 45 generate promising sample sets for robust (pose) estim
Thus, feature extraction can be easily made invariant with in images exhibiting very few inlier correspo Thus, feature extraction can be easily made invariant with in images exhibiting very few inlier correspondences.

respect to two degrees of freedom (i.e. the surface normal) FIG. 6 shows exemplary results of the steps of a but not reliably invariant with respect to the remaining 2D described herein. Image 601 is an input RGB image (for rotation in the local tangent plane. For the same reason, illustration purposes only); image 602 is an inpu predicting poses directly based on feature correspondences 50 may lead to large uncertainties in the estimates, and theremay lead to large uncertainties in the estimates, and there atlas) with grayscale-coded object coordinates; image 604 fore the approach described herein predicts "object coordi-
shows the best matching object coordinates f fore the approach described herein predicts "object coordi-
nates" (i.e. 3D vertices on the object of interest) and com-
llustrate the level of false positives; image 605 shows the nates" (i.e. 3D vertices on the object of interest) and com-
pulstrate the level of false positives; image 605 shows the
putes more certain and accurate poses from multiple corresponding minimal feature distances, which al

partially visible. A sensible principle to add robustness with shows the geometric pose scores (Eq. 11) after pose refine-
respect to occlusions is to employ a compositional method, ment; and image 608 shows points of t i.e. to detect the object and estimate its pose by detecting and posed according to the best pose estimate.
aligning smaller parts. Due to the locally ambiguous appear- 60 In the below it is shown that the approaches descr ance of depth images, a much higher false-positive rate may herein are capable of handling noisy sensor data while
be expected than with colour images when matching fea-
performing at several frames per second. Another cha be expected than with colour images when matching fea-
tures extracted in the query images with the ones in the ing aspect is handling objects with highly self-similar local tures extracted in the query images with the ones in the ing aspect is handling objects with highly self-similar local training database, and it will be useful to maintain several shape appearance (e.g. surfaces of revolut training database, and it will be useful to maintain several shape appearance (e.g. surfaces of revolution or objects with predictions of object coordinates per pixel to address the 65 multiple symmetries).

FLASH-EPROM, NVRAM, and any other memory chip or indicate that at least one of the predicted object coordinates may be an outlier. Thus, one can easily avoid sampling and rtridge.

may be an outlier. Thus, one can easily avoid sampling and

Detailed examples of the approaches described herein are

evaluating pose hypotheses from outlier-contaminated minievaluating pose hypotheses from outlier-contaminated mini-

(or latent) states, then the pairwise consistency of predicted inference in graphical models may be employed in this exploiting data-parallelism the approach is fast, and a com-
putationally expensive training phase is not necessary. State-
of models whose underlying graph has exactly the size of
of-the art performance is demonstrated on

> consider a large number of overlapping minimal sample sets and remove the ones clearly contaminated with outliers by overlapping, applying the consistency criterion to a pair of

illustration purposes only); image 602 is an input depth image; image 603 is a view of a trained CAD model (an putes correspondences.
Finally, objects of interest can be occluded and only be shows the smallest min-marginals Eq. 6 per pixel; image 607 Finally, objects of interest can be occluded and only be shows the smallest min-marginals Eq. 6 per pixel; image 607 partially visible. A sensible principle to add robustness with shows the geometric pose scores (Eq. 11) a ment; and image 608 shows points of the model superim-

amount of false positive matches. In summary, object detec-

Before a method is described in detail, a high-level

tion solely from depth data faces the following challenges:

overview is provided: at test time the algorit overview is provided: at test time the algorithm maintains a

set of putative matching object coordinates (corresponding If the Euclidean distance between X_p and X_q deviates candidate locations) for each pixel (image element) in the substantially from the one between X_p and X_q , then X_p and test image (image 301). Instead of sampling minimal sets of X_q cannot be part of an inlier set. The exact quantification of correspondences required for (rigid) pose computation, the "sufficiently large" deviations depe correspondences required for (rigid) pose computation, the "sufficiently large" deviations depends on the depth sensor
utility of pairs of correspondences (pairs of candidate $log₂ - 5$ characteristics. Note that this utility of pairs of correspondences (pairs of candidate loca- 5 characteristics. Note that this criterion is invariant to any
tions) is assessed by using the consistency with the observed
depth data. Triplets of correspond depth data. Triplets of correspondences (triplets of candidate native) by adding the compatibility of normal estimates. In locations) are ranked and finally promising ones are evaluation of the not to introduce extra tunin locations) are ranked, and finally promising ones are evalu-
order not to introduce extra tuning parameters of how to
weight the distance and normal compatibility terms, meth-

detecting objects that occupy only a fraction of the image, a minimal impact on the results, since the final compatibility scores are based on triplets of correspondences (triplets of

occupancy grid is employed to compute descriptors. Other options include: a $($ truncated) signed distance function 20 (TSDF), and 3D-SURF. The descriptor in the method described herein is a bit string of occupancies in the vicinity

dexceribed herein is a surface point.
In order to obtain some degree of invariance with respect to viewpoint changes, the z-axis of the local coordinate 25 frame at a surface point is aligned with the (local) surface normal. Given the piecewise smooth characteristic of range images, normals can be estimated relatively reliably for with most pixels (after running a Wiener filter to reduce the quantization artifacts observed in triangulation-based depth $_{30}$ sensors). For the same reason computation of the second principal direction is highly unreliable and not repeatable.

Therefore several descriptors are computed at each surface

point by sampling the 2D rotation in the tangential plane (as
 α is the maximum poise or uncerta point by sampling the 2D rotation in the tangential plane (as σ is the maximum noise or uncertainty level expected from one example, samples are taken in 20° steps resulting in 18 σ is the depth sensor and matching

one example, samples are taken in 20 steps resulting in 16 35 the depth sensor and matching procedure. Since the training
descriptors per surface point).
Instead of storing a full local occupancy grid (centered at
a surfac tangent plane are selected. Thus, voxel positions were ran-
domly sampled in a box aligned with the tangent plane that correspondences, e.g. $\{\hat{X}_p \leftrightarrow X_p, \quad \hat{X}_q \leftrightarrow X_q, \quad \hat{X}_r \leftrightarrow X_r\}$, a domly sampled in a box aligned with the tangent plane that correspondences, e.g. $\{X_p \leftrightarrow X_p, X_q \leftrightarrow X_q, X_r \leftrightarrow X_r\}$, a has half the height of the width and depth (8 cm ×8 cm ×4 cm Euclidean transformation and therefore pose estim has half the height of the width and depth (8 cm×8 cm×4 cm Euclidean transformation and therefore pose estimate can be boxes were used). This means that building the descriptors computed via the Kabsch algorithm or Horn's boxes were used). This means that building the descriptors computed via the Kabsch algorithm or Horn's method. The from the given depth images or training meshes is very fast. 45 task at hand is to generate a promising set from the given depth images or training meshes is very fast. 45 Matching

valid depth and estimated surface normal in the (sub-

Randomly sampling three putative correspondences will

sampled) depth image, and the task is to efficiently deter-

be inefficient, since the inlier ratio is very smal sampled) depth image, and the task is to efficiently deter-
mine the set of object coordinates with similar local shape $\frac{1}{50}$ in the following example: if the object of interest (imaged mine the set of object coordinates with similar local shape 50 in the following example: if the object of interest (imaged appearance. To quantify similarity of binary strings, the object 102) is seen in about 5% of t

pose hypothesis it is possible to assess the quality of pairs of
putative correspondences (pairs of candidate locations) by
and too optimistic (by assuming pixels seeing the object
parallel in the range image instead of a exploiting the information contained in the range image and too optimistic (by assuming pixels seeing the object
(image 301) If n and a are two nixels (image elements) in 60 have always a true positive correspondence) a (image 301). If p and q are two pixels (image elements) in ⁶⁰ have always a true positive correspondence) at the same
the query range image and \hat{X} and \hat{X} are the respective time. Nevertheless, almost all rando the query range image, and \hat{X}_p and \hat{X}_q are the respective time. Nevertheless, almost all random minimal sample sets back-projected 3D points induced by the observed depth, X_p will contain at least one outlier, and \hat{X}_q are putative correspondences reported at p and \hat{q} , ibility criterion described below efficiently determines then a necessary condition for $\hat{X}_q \leftrightarrow \hat{X}_q$. $\hat{X}_q \leftrightarrow \hat{X}_q$ being promising sample sets.

10

ated using a standard geometric criterion to determine the
best-scoring object pose.
Descriptor Computation
Descriptor Computation
City of predicted object coordinates. The loss of discrimi-
computation
City of the start o Given the nature of depth maps and the problem of minimal impact on the results, since the final compatibility has $\frac{1}{2}$ dense (or quasi-dense) computation of descriptors may be
used in order not to rely on unstable salient feature points.
It contracts are based on a pass of compatibility score) to assess the compatibility.
The descriptor t

$$
\psi(X_p, X_q; \hat{X}_p, \hat{X}_q) \stackrel{def}{=} \tag{2}
$$

$$
\begin{cases} \Delta^2(X_p, X_q; \hat{X}_p, \hat{X}_q) & \text{if } |\Delta(X_p, X_q; \hat{X}_p, \hat{X}_q)| \le \sigma \\ \infty & \text{otherwise} \end{cases}
$$
 (3)

$$
\Delta(X_p, X_q; \hat{X}_p, \hat{X}_q) \stackrel{def}{=} ||\hat{X}_p - \hat{X}_q|| - ||X_p - X_q||.
$$

atching
At test time descriptors are computed for each pixel with mined for each pixel.

appearance. Io quantity similarity of binary strings, the

Hamming distance is used. An approximated nearest neigh-

bours implementation for binary data in FLANN was used.

Pairwise Compatibility

The matching step retur

then a necessary condition for $\hat{X}_p \leftrightarrow \hat{X}_p$, $\hat{X}_q \leftrightarrow \hat{X}_q$ being
inter correspondences is that
inter correspondences is that
 $|\hat{X}_p \rightarrow \hat{X}_q|$.
 $\|\hat{X}_p - \hat{X}_q\|$.
 $\|\hat{X}_p - \hat{X}_q\|$.
(1) (1) sum BP since negative sum BP since negative logpotentials are used) to quickly

45

$$
E_{pqr}(X_p, X_q, X_r) \stackrel{def}{=} \tag{4}
$$

$$
\phi_p(X_p) + \phi_q(X_q) + \phi_r(X_r) + \psi(X_p, X_q; \hat{X}_p, \hat{X}_q) + \psi(X_p, X_r; \hat{X}_p, \hat{X}_r).
$$

$$
\mu_{pqr}(X_p) \stackrel{\text{def}}{=} \min_{X_q, X_r} E_{pqr}(X_p, X_q, X_r) \tag{5}
$$

$$
m_{q \to q}(X_p) = \min_{X_q} \{ \phi_q(X_q) + \psi(X_p, X_q; \hat{X}_p, \hat{X}_q) \}
$$
\n⁽⁵⁾

$$
\mu_{pqr}(X_p) = \min_{X_q, X_r} E_{pqr}(X_p, X_q, X_r)
$$
\n
$$
= \phi_p(X_p) + m_{q \to p}(X_p) + m_{r \to p}(X_p)
$$
\n(6)

ma - pet (ma - p (XD)) Xp tive :

certain pairwise potentials ψ the message vector computa η 2. and update R and T using a weighted extension of the tion is sub-quadratic in the number of states (i.e. putative η 55 Kabsch algorithm (also known as object coordinates in this setting), which would lead to The weights w_j are derived from the smooth approxi-
further computational benefits. Unfortunately the choice of mation of the robust truncated quadratic kernel further computational benefits. Unfortunately the choice of the pairwise potential given in Eq . 3 does not allow an obvious faster algorithm for message computation . Message computation does not only yield the value of the messages , 60 $m_{q \to q}(X_p)$, but also the minimizing state

$$
X_{q \to p}^*(X_p) \stackrel{def}{=} \arg\min_{X_q} \{ \phi_q(X_q) + \psi(X_p, X_q; \hat{X}_p, \hat{X}_q) \}
$$
\n⁽⁷⁾

discard outlier contaminated sample sets. Let {p, q, r} be a
set of (non-collinear) pixels in the query image, let X_s , se{p,
q, r} range over the putative object coordinates, and $\phi_s(X_s)$
de a unary potential (usually b

neighbour search for X_s is used as unary potential $\phi_s(X_s)$. 15 predictions and numerical stability of pose estimation). For two edges q \rightarrow P and r \rightarrow P the predictions $(X_p, X^*_{q\rightarrow p}(X_p))$, cubic in the number of states in such setting.]
The min-marginals are computed densely for each pixel in 10 the query image (i.e. every nivel is the root) and messages the query image (i.e. every pixel is the root), and messages $m_{p+\delta_k \to p}$ are computed from pixel located at an offset δ_k ,
Ke{1, ..., K} from p. The choice of the set { δ_k } contains The Hamming distance between the descriptor extracted the $\overline{16}$ offsets of axis aligned and diagonal offsets at 8 and at pixels and the ones returned by the (approximate) nearest $\overline{16}$ pixels distance (which aims 16 pixels distance (which aims to trade off locality of predictions and numerical stability of pose estimation). For Note that min-marginals, i.e. the quantities two edges $q \to P$ and $r \to P$ the predictions $(X_p, X^*_{q \to p}(X_p))$
 $X^*_{r \to p}(X_p)$ form a minimal sample set for estimating the rigid pose, and min-marginals are for all $K(K-1)/2$ such triplets used to rank these minimal sample sets. The method $_{20}$ proceeds with estimating and evaluating the pose for the top ranked ones (here, 2000 are used) as described below.

Finited ones (here, 2000 are used) as a escribed below.

Franked ones (here, 2000 are used) as a escribed below.

Propagation on a tree rooted p. In this case only 3 corre-

Assessing the quality of a pose hypothesis by a messages smoothing the input] and another is to maximize over the latent pose. In the below, the latter option is chosen. Since it is not expected or assumed that many pose hypotheses will $m_{q \to q}(X_p) = \min_{X_q} {\left\{\phi_q(X_q) + \psi(X_p, X_q, \hat{X}_p, \hat{X}_q)\right\}}$ be obtained near the true pose, no pose clustering or aver-35 aging approaches are used . A , " classical " geometric approach is used by determining an optimal alignment

sent from a leaf q to the root p. Note that the min-marginals
can be expressed as
latent variable in general) is to "explain" the data given the
data given the $_{40}$ assumptions on the sensor noise, i.e. to formulate a respective cost function that sums (integrates) over the image domain. Unfortunately, this more principled formulation is expensive to optimize. Thus, for computational reasons, the $\phi_p(X_p) + m_{q \to p}(X_p) + m_{r \to p}(X_p)$ reverse direction of "explaining" the model is used (recall
that up to 2000 pose hypotheses are considered at this stage). Further, observe that the vector of messages

⁴³ Several methods to robustly refine the pose of a point set

with respect to a depth map were implemented, including pose refinement via (robust) non-linear least squares. The following simple alternation algorithm is efficient and effective:

- ⁵⁰ 1. Perform "projective data association" (i.e. establish the correspondence between a model point X_i and the can be reused in all trees containing the (directed) edge back-projected depth \hat{X}_j with both \hat{X}_j and RX_j +T being $q \rightarrow p$, leading to substantial computational savings. For on the same line-of-sight),
	-

$$
\rho_{\tau}(e) \stackrel{\text{def}}{=} \begin{cases} \frac{e^2}{4} \left(2 - \frac{e^2}{\tau^2} \right) & \text{if } e^2 \le \tau^2 \\ \frac{\tau^2}{4} & \text{otherwise} \end{cases}
$$
\n⁽⁸⁾

 (9)

$$
\omega_{\tau}(e) \stackrel{def}{=} \rho'_{\tau}(e)/e = \max\{0, 1 - e^2/\tau^2\},\
$$

$$
w_i = w_{\mathcal{I}}((RX_i + T - \hat{X}_i)_3) \tag{10}
$$

The weights given in Eq. 10 are based on depth deviation
between the transformed model point and the corresponding ⁵ We show as baseline methods the following approaches:
value in the depth man. If a depth value is missi value in the depth map. If a depth value is missing for the
projected model point, that correspondence is considered an
projected model point that correspondence is considered an
projected model point cloud is superim-
pro outlier and has zero weight, is the inlier noise level and the sequences. The respective model point cloud is superim-
same value is used as for (which is 3 mm). It should be noted posed on the normal-map rendered input. C same value is used as for (which is 3 mm). It should be noted posed on the normal-map rendered input. Correct detections that this algorithm does not optimize a single energy $(a, 10)$ and poses can be seen despite large o that this algorithm does not optimize a single energy ($a¹⁰$ and poses can be seen despite large occ
nonerty shared with most ICP variants using projective data property shared with most ICP variants using projective data depth data, and strong viewpoint changes.
Sesociation) These two steps are repeated 10 times on a FIG. 8 shows results obtained on the Mian dataset. It can association). These two steps are repeated 10 times on a FIG. 8 shows results obtained on the Mian dataset. It can
Fig. be seen that the method described herein is able to handle (random) subset of 1000 model points. The final score of the beseen that the method described herein is able to handle
nose hypothesis is evaluated on a larger subset of 10000 occlusions of up to 81% and still give 100% de pose hypothesis is evaluated on a larger subset of 10000 occlusions of up to 81% and still give 100% detection rates.
model points by using a robust fitting cost,

$$
\sum_{i} \rho_{\rm r} \big(\big(RX_j + T - \hat{X}_j \big)_3 \big) \tag{11}
$$

The pose with the lowest cost is reported and visualized. With 4 models on which to perform detection.
Implementation Notes Ground truth pose is provided for all instances of all
Training phase: The core data used in the t

are depth images of the object(s) of interest (imaged object) 25 together with the respective pose data. These depth maps can approach described herein and all baselines do not include
be generated synthetically from e.g. CAD models or cap-
this object. Results are provided for two diff be generated synthetically from e.g. CAD models or cap-
this object. Results are provided for two different resolutions
tured by a depth sensor. If CAD models are rendered, the
for the prediction image, 320×240 (downsa camera poses are generated randomly looking towards the object's centre of gravity. In the implementation, the real 30 predicted object coordinate image means faster computadepth sensor characteristics (e.g. noise or quantization tion, but also a lower probability of finding an inlier sample effects) are not simulated, which in some cases led to missed

correspondences in parts of the object (e.g. the top of the Experimental results: As seen in FIG. 8, approaches

pipe in FIG. 6 has a substantially different a rendered and real depth maps). From these depth maps a 35 to 81% of occlusion, with higher levels of occlusion
target number of descriptors (typically 32 k in these experi-
approaches described herein perform similarly to target number of descriptors (typically 32 k in these experiments) are extracted by selecting a random subset of (valid) ments) are extracted by selecting a random subset of (valid) baselines. Learning techniques could likely be employed to pixels in the depth map. Random sampling is slightly biased boost the results of the approaches descri pixels in the depth map. Random sampling is slightly biased boost the results of the approaches described herein (in towards pixels in the depth map with close to fronto-parallel terms of recognition rate and possibly in r surface patches. Thus, about 600 k descriptors $(32 \text{ k} \times 18 \text{ for } 40 \text{ T}$ The results on the Mian dataset give a clear understanding the sampled tangent-plane rotations) are generated and of how the approaches described Consequently, the training phase is completed within sec-

extraction, matching against the database, message passing, such as the toy car and the bracket, or by approximate and pose evaluation). While no part of the algorithm was manual 3D modeling of pipe-like structures). When implemented on a GPU, OpenMP-based multi-processing the descriptors for the objects of interest, the depth sensor
was used whenever possible. The input depth maps (image 50 characteristics (such as boundary fattening and d was used whenever possible. The input depth maps (image 50 characteristics (such as boundary fattening and depth quan-
301) are 640×480 pixels, but predicted object coordinates ization) were not simulated. Thus, the 3D mod 301) are 640 \times 480 pixels, but predicted object coordinates are computed on either 320 \times 240 or 160 \times 120 images (the are computed on either 320×240 or 160×120 images (the and the actual range images may be significantly different in latter one for to achieve interactive frame rates). On a dual their depth appearance. FIG. 7 depi latter one for to achieve interactive frame rates). On a dual their depth appearance. FIG. 7 depicts sample frames with Xeon E5-2690 system, a frame rate between 2 frames per the model point cloud superimposed on the input Xeon E5-2690 system, a frame rate between 2 frames per the model point cloud superimposed on the input depth second (320×240 resolution) or up to 10 Hz (160×120) was 55 (rendered via its normal map). second a 320x240 resolution is the most time consuming part. A GPU implementation is the most time consuming part. A GPU implementation is an approach described herein are presented, although a GPU the most time consuming part. A GPU implementation is an approach described herein are presented, although a GPU anticipated to have real-time performance.

Results are shown on the Mian dataset, since it is the de 60 Hz). The individual time contributions of the various stages facto baseline benchmark dataset for 3D object detection of the method described herein are as follo ASUS Xtion camera are also shown in order to demonstrate Matching (Hamming dist
the ability of the algorithm described herein to cope with using FLANN): 45%; noisy inputs. Since the algorithm described above takes 65 Message passing (for min-marginal computation): 24%; noisy input, the given meshes were converted to Ranking (ranking/sorting according to Eq. 6): 6%; and depth maps as input, the given meshes were converted to Ranking (ranking/sorting according to $\frac{1}{2}$ range images by rendering into 640×480 depth maps using Pose Evaluation (including ICP): 16%. range images by rendering into 640×480 depth maps using

and given by approximate parameters for the camera intrinsics (since the camera intensity of the camer calibration parameters of the range scanner are not avail able). Consequently, the amount of occlusions in the depth maps may be slightly higher than in the provided meshes.

object compared to the only other approaches that obtain similar or better detection rates, is of up to 30 times less for approaches described herein when compared with the Tuzel $((RX_j + T - \hat{X}_j)_3)$ (11) approaches described herein when compared with the Tuzel approach and up to 170 times less compared to the Drost

20 approach.

Experimental setup: The Mian dataset contains 50 scenes

with 4 models on which to perform detection.

objects. Apart from those 4 models, another model exists that was excluded in Mian's experiments; hence the for the prediction image, 320×240 (downsampling factor $\theta = 2$), and 160×120 ($\theta = 4$). A smaller resolution of the

same time the data is much cleaner than depth maps obtained
by current commodity sensors. Consequently, the inventor onds.

recorded their own data using an ASUS Xtion depth sensor

Parallel implementation: Most steps in approaches 45 and ran a method described herein for objects with available Parallel implementation: Most steps in approaches 45 and ran a method described herein for objects with available described herein can be parallelized (including descriptor CAD models (either obtained from a 3D model datab

Experiments
Results are shown on the Mian dataset, since it is the de 60 Hz). The individual time contributions of the various stages

15
By far the most expensive step is the feature matching and the object of interest, but in general feature matching 5. The method of claim 3, further comprising performing (i.e. nearest neighbour search) consumes a dominant fraction step (g) for further pairs of the candidate faster for object with a highly distinctive local shape appear \overline{a} 6. The method of claim 5, further comprising .
ances than for object with redundant surface structures since determining compatibility scores for the ances than for object with redundant surface structures, since determining compatibility scores for the first and second in the former case the search trees tend to be more balanced pairs of the candidate locations of each in the former case the search trees tend to be more balanced.

1. A computer implemented method for use in estimating $\frac{10}{2}$ compatibility scores.
The method of claim 6, wherein the step of selecting a a pose of an imaged object, the method comprising the following steps:

- a) receiving an image made up of image elements, the to their corresponding compatibility scores image representing, in three spatial dimensions, a scene
- b) for each of a plurality of the image elements, identi-
fiing an arrow assumed compatibility and determined compatibility of the triplets based on the determined compatibility of the triplets based on the determined com fying one or more corresponding candidate locations in scores is performed using graph searching.

an atlas of one or more candidate objects;
 19. The method of claim 6, further comprising, for each triplet in the subset
- image elements, the pair comprising a first image 20° estimate for the imaged element and a second image element;
-
- e) determining a second distance between a first candidate creating an estimated image of the imaged $\frac{1}{10}$ based on the image of the imitial pose estimate of that triplet; location corresponding to the first image element and a 25 the initial pose estimate of that triplet;
comparing the estimated image with the image representsecond candidate location corresponding to the second ing the scene including the imaged object; and
image element; and imaged object; and
announcing the first and specific including the imaged object; and
announcing the first and specific including the comparison, determinin
-

2. The method of claim 1, further comprising performing
 $\frac{1}{2}$ refined pose estimate for the triplet.

11. The method of claim 10, further comprising selecting steps (c) to (f) for one or more further pairs of image $\frac{30}{20}$ 11. The method of claim 10, further comprising selecting of electing of the refined pose estimates based on the scores of the elements from the plurality of image elements. one of the refined pose $\frac{3}{\pi}$. The method of claim 2, further comprising the stap of the schedule pose estimates.

3. The method of claim 2, further comprising the step of

- i) selecting a first pair of candidate locations having first rist for each of the plurality of image elements.
and aggregate energy of the plurality of the plurality of image elements : and second candidate locations corresponding to the ³⁵ first and second image elements of a first of the pairs of
- ii) selecting a second pair of candidate locations having
first and second candidate locations corresponding to
the first and second image elements of a second of the $\frac{40}{40}$ map and each image element has an intensit
- comprising the first pair of candidate locations and the values.
 14. An apparatus or system arranged to perform the second candidate location of the second pair of candidate locations.

4. The method of claim 3, wherein at least one of step i) and ii) comprises:

determining a compatibility score for the respective pair by one or more processors , to cause the one or more by one or more processor of candidate locations based upon the comparison of processors to carry out the method of claim 1 . step (f) , and * * * *

By far the most expensive step is the feature matching making the respective selection based upon that determi-
step. The exact values vary depending on the input frame nation.

-
- The invention claimed is:

1. A computer implemented method for use in estimating $\frac{10}{10}$ compatibility scores.

subset of the triplets comprises ranking the triplets according
to their corresponding compatibility scores and selecting a

subset of the triplets based on the dimensions, a scene including the ranking the image representing the imaged object; $\frac{15}{15}$ 8. The method of claim 6, wherein the selection of a subset of the triplets based on the

c) forming a pair of image elements from the plurality of triplet in the subset of triplets, computing an initial pose image alements the pair comprising a first image 20 estimate for the imaged object based on the resp

determining a first distance between the first image
element;
element and the second image element;
element and the second image element;
element and the second distance between a first candidate
exacting an estimated imag

-
-
- f) comparing the first and second distances.
 Comparison in the comparison of claim 1 further comprising performing and second the comparison, determining and second in the comparison of claim 1 further comparison perfor

g): The method of claim 2, tuttlet comprising the step of $\frac{12}{2}$. The method of claim 1, wherein step (b) comprises, $\frac{1}{2}$. The method of claim 1, wherein step (b) comprises,

and

image elements; and matching that descriptor to one or more candidate loca-
ii) selecting a second pair of candidate locations having

pairs of image elements, represents a depth, and further wherein step (d) comprises Forming a triplet of candidate locations, the triplet determining the first distance using image element intensity
values

 45 method of preceding claim 1.
15. A non-transitory computer-readable medium compris-

ing machine-readable instructions arranged, upon execution
by one or more processors, to cause the one or more