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# Krueger et al.

## (54) METHOD AND APPARATUS FOR COMPRESSING AND DECOMPRESSINGA HIGHER ORDER AMIBISONICS REPRESENTATION FOR A SOUND FIELD

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Primary Examiner — Andrew L Sniezek

# (57) ABSTRACT

The invention improves HOA sound field representation compression. The HOA representation is analyzed for the presence of dominant sound sources and their directions are estimated. Then the HOA representation is decomposed into a number of dominant directional signals and a residual component. This residual component is transformed into the discrete spatial domain in order to obtain general plane wave<br>functions at uniform sampling directions, which are predicted from the dominant directional signals. Finally, the prediction error is transformed back to the HOA domain and represents the residual ambient HOA component for which an order reduction is performed, followed by perceptual encoding of the dominant directional signals and the residual component.

#### 15 Claims, 5 Drawing Sheets



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Fig. 1a



Fig. 1b



Fig. 2a



Fig.2b











Fig. 6

# METHOD AND APPARATUS FOR COMPRESSING AND DECOMPRESSINGA HIGHER ORDER AMBISONICS REPRESENTATION FOR A SOUND FIELD

This application claims the benefit, under 35 U.S.C. §365 of International Application PCT/EP2013/075559, filed Dec. 4, 2013, which was published in accordance with PCT Article 21(2) on Jun. 19, 2014 in English and which claims the benefit of European patent application No. 12306569.0, 10 filed Dec. 12, 2012.

The invention relates to a method and to an apparatus for compressing and decompressing a Higher Order Ambisonics representation for a sound field.

# **BACKGROUND**

Higher Order Ambisonics denoted HOA offers one way of representing three-dimensional Sound. Other techniques are wave field synthesis (WFS) or channel based methods like 20 22.2. In contrast to channel based methods, the HOA representation offers the advantage of being independent of a specific loudspeaker set-up. This flexibility, however, is at the expense of a decoding process which is required for the playback of the HOA representation on a particular loud- 25 speaker set-up. Compared to the WFS approach where the number of required loudspeakers is usually very large, HOA may also be rendered to set-ups consisting of only few loudspeakers. A further advantage of HOA is that the same representation can also be employed without any modifica- 30 tion for binaural rendering to head-phones.

HOA is based on a representation of the spatial density of complex harmonic plane wave amplitudes by a truncated Spherical Harmonics (SH) expansion. Each expansion coef ficient is a function of angular frequency, which can be 35 equivalently represented by a time domain function. Hence, without loss of generality, the complete HOA sound field representation actually can be assumed to consist of O time domain functions, where O denotes the number of expansion domain functions, where O denotes the number of expansion<br>coefficients. These time domain functions will be equiva- 40 lently referred to as HOA coefficient sequences in the following.

The spatial resolution of the HOA representation<br>improves with a growing maximum order N of the expanimproves with a growing maximum order N of the expan sion. Unfortunately, the number of expansion coefficients O 45 grows quadratically with the order N, in particular  $O = (N+1)^2$ . For example, typical HOA representations using order N=4 require O=25 HOA (expansion) coefficients. According to the above considerations, the total bit rate for the trans mission of HOA representation, given a desired single 50 channel sampling rate  $f_s$  and the number of bits  $N_b$  per sample, is determined by  $O(f_s \cdot N_b)$ . Transmitting an HOA representation of order N=4 with a sampling rate of  $f_s$ =48 kHz employing  $N_b=16$  bits per sample will result in a bit rate applications, e.g. streaming. Therefore compression of HOA representations is highly desirable. of 19.2 MBits/s, which is very high for many practical 55

#### INVENTION

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The existing methods addressing the compression of HOA representations (with N>1) are quite rare. The most straight forward approach pursued by E. Hellerud, I. Bur nett, A Solyang and U.P. Svensson, "Encoding Higher Order Ambisonics with AAC", 124th AES Convention, Amster- 65 dam, 2008, is to perform direct encoding of individual HOA coefficient sequences employing Advanced Audio Coding

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15 coefficient sequences are cancelled at Superposition. A fur (AAC), which is a perceptual coding algorithm. However, the inherent problem with this approach is the perceptual coding of signals which are never listened to. The recon structed playback signals are usually obtained by a weighted sum of the HOA coefficient sequences, and there is a high probability for unmasking of perceptual coding noise when the decompressed HOA representation is rendered on a particular loudspeaker set-up. The major problem for per ceptual coding noise unmasking is high cross correlations between the individual HOA coefficient sequences. Since the coding noise signals in the individual HOA coefficient sequences are usually uncorrelated with each other, there may occur a constructive superposition of the perceptual coding noise while at the same time the noise-free HOA ther problem is that these cross correlations lead to a reduced efficiency of the perceptual coders.

In order to minimise the extent of both effects, it is proposed in EP 2469742 A2 to transform the HOA repre sentation to an equivalent representation in the discrete spatial domain before perceptual coding. Formally, that discrete spatial domain is the time domain equivalent of the spatial density of complex harmonic plane wave amplitudes, sampled at some discrete directions. The discrete spatial domain is thus represented by O conventional time domain signals, which can be interpreted as general plane waves impinging from the sampling directions and would corre spond to the loudspeaker signals, if the loudspeakers were positioned in exactly the same directions as those assumed for the spatial domain transform.

The transform to discrete spatial domain reduces the cross correlations between the individual spatial domain signals, but these cross correlations are not completely eliminated. An example for relatively high cross correlations is a directional signal whose direction falls in-between the adja cent directions covered by the spatial domain signals.

A main disadvantage of both approaches is that the number of perceptually coded signals is  $(N+1)^2$ , and the data rate for the compressed HOA representation grows quadrati cally with the Ambisonics order N.

To reduce the number of perceptually coded signals, patent publication EP 2665208 A1 proposes decomposing of the HOA representation into a given maximum number of dominant directional signals and a residual ambient com ponent. The reduction of the number of the signals to be perceptually coded is achieved by reducing the order of the residual ambient component. The rationale behind this approach is to retain a high spatial resolution with respect to dominant directional signals while representing the residual with sufficient accuracy by a lower-order HOA representa tion.

This approach works quite well as long as the assump tions on the Sound field are satisfied, i.e. that it consists of a small number of dominant directional signals (representing general plane wave functions encoded with the full order N) and a residual ambient component without any directivity. However, if following decomposition the residual ambient component is still containing some dominant directional components, the order reduction causes errors which are distinctly perceptible at rendering following decompression. Typical examples of HOA representations where the assumptions are violated are general plane waves encoded in an order lower than N. Such general plane waves of order lower than N can result from artistic creation in order to make sound sources appearing wider, and can also occur with the recording of HOA sound field representations by spherical microphones. In both examples the sound field is

represented by a high number of highly correlated spatial domain signals (see also section Spatial resolution of Higher Order Ambisonics for an explanation).

A problem to be solved by the invention is to remove the disadvantages resulting from the processing described in 5 patent publication EP 2665208 A1, thereby also avoiding the above described disadvantages of the other cited prior art. This problem is solved by the methods disclosed in claims 1 and 3. Corresponding apparatuses which utilise these methods are disclosed in claims 2 and 4. 10

The invention improves the HOA sound field representa tion compression processing described in patent publication EP 2665208 A1. First, like in EP 2665208 A1, the HOA representation is analysed for the presence of dominant sound sources, of which the directions are estimated. With the knowledge of the dominant sound source directions, the HOA representation is decomposed into a number of domi nant directional signals, representing general plane waves, and a residual component. However, instead of immediately 20 reducing the order of this residual HOA component, it is transformed into the discrete spatial domain in order to directions representing the residual HOA component. Thereafter these plane wave functions are predicted from the 25 dominant directional signals. The reason for this operation is that parts of the residual HOA component may be highly correlated with the dominant directional signals. 15

That prediction can be a simple one so as to produce only a small amount of side information. In the simplest case the 30 prediction consists of an appropriate scaling and delay. Finally, the prediction error is transformed back to the HOA domain and is regarded as the residual ambient HOA component for which an order reduction is performed.

signals from the residual HOA component is to reduce its total power as well as the remaining amount of dominant directional signals and, in this way, to reduce the decompo sition error resulting from the order reduction.

In principle, the inventive compression method is Suited 40 for compressing a Higher Order Ambisonics representation denoted HOA for a sound field, said method including the steps:

from a current time frame of HOA coefficients, estimating dominant sound source directions; 45

- depending on said HOA coefficients and on said dominant sound source directions, decomposing said HOA representation into dominant directional signals in time domain and a residual HOA component, wherein said residual HOA component is transformed into the dis- 50 crete spatial domain in order to obtain plane wave functions at uniform sampling directions representing said residual HOA component, and wherein said plane wave functions are predicted from said dominant direc tional signals, thereby providing parameters describing 55 said prediction, and the corresponding prediction error is transformed back into the HOA domain;
- reducing the current order of said residual HOA compo nent to a lower order, resulting in a reduced-order 60
- de-correlating said reduced-order residual HOA component to obtain corresponding residual HOA component time domain signals;
- perceptually encoding said dominant directional signals and said residual HOA component time domain signals so as to provide compressed dominant directional signals and compressed residual component signals. 65

In principle the inventive compression apparatus is suited for compressing a Higher Order Ambisonics representation denoted HOA for a sound field, said apparatus including:<br>means being adapted for estimating dominant sound

- source directions from a current time frame of HOA coefficients;
- means being adapted for decomposing, depending on said HOA coefficients and on said dominant sound source directions, said HOA representation into dominant directional signals in time domain and a residual HOA component, wherein said residual HOA component is transformed into the discrete spatial domain in order to obtain plane wave functions at uniform sampling direc tions representing said residual HOA component, and wherein said plane wave functions are predicted from said dominant directional signals, thereby providing parameters describing said prediction, and the corre sponding prediction error is transformed back into the HOA domain;
- means being adapted for reducing the current order of said residual HOA component to a lower order, resulting in a reduced-order residual HOA component;
- means being adapted for de-correlating said reduced order residual HOA component to obtain correspond ing residual HOA component time domain signals;
- means being adapted for perceptually encoding said dominant directional signals and said residual HOA component time domain signals so as to provide com pressed dominant directional signals and compressed residual component signals.

component for which an order reduction is performed. Advantageously, the effect of subtracting the predictable 35 method, said decompressing method including the steps: In principle, the inventive decompression method is suited for decompressing a Higher Order Ambisonics representation compressed according to the above compression

- perceptually decoding said compressed dominant direc signals so as to provide decompressed dominant directional signals and decompressed time domain signals representing the residual HOA component in the spatial domain;
- re-correlating said decompressed time domain signals to obtain a corresponding reduced-order residual HOA component;
- extending the order of said reduced-order residual HOA component to the original order so as to provide a corresponding decompressed residual HOA compo nent;
- using said decompressed dominant directional signals, said original order decompressed residual HOA com ponent, said estimated dominant sound source directions, and said parameters describing said prediction, composing a corresponding decompressed and recomposed frame of HOA coefficients.

In principle the inventive decompression apparatus is suited for decompressing a Higher Order Ambisonics representation compressed according to the above compressing method, said decompression apparatus including:

- means being adapted for perceptually decoding said com pressed dominant directional signals and said com pressed residual component signals so as to provide decompressed dominant directional signals and decom pressed time domain signals representing the residual HOA component in the spatial domain;
- means being adapted for re-correlating said decompressed time domain signals to obtain a corresponding reduced order residual HOA component;

- means being adapted for extending the order of said<br>reduced-order residual HOA component to the original order so as to provide a corresponding decompressed residual HOA component;
- means being adapted for composing a corresponding decompressed and recomposed frame of HOA coeffi cients by using said decompressed dominant direc tional signals, said original order decompressed residual HOA component, said estimated dominant sound source directions, and said parameters describing 10<br>said prediction.

Advantageous additional embodiments of the invention are disclosed in the respective dependent claims.

#### DRAWINGS

Exemplary embodiments of the invention are described with reference to the accompanying drawings, which show<br>in:

FIG. 1a compression step 1: decomposition of HOA  $_{20}$ signal into a number of dominant directional signals, a residual ambient HOA component and side information;

FIG. 1b compression step 2: order reduction and decor relation for ambient HOA component and perceptual encod ing of both components;

FIG. 2a decompression step 1: perceptual decoding of time domain signals, re-correlation of signals representing the residual ambient HOA component and order extension;

FIG.2b decompression step 2: composition of total HOA representation;

FIG. 3 HOA decomposition;

FIG. 4 HOA composition:

FIG. 5 spherical coordinate system.

# EXEMPLARY EMBODIMENTS

Compression Processing

The compression processing according to the invention includes two successive steps illustrated in FIG. 1a and FIG.  $1b$ , respectively. The exact definitions of the individual  $_{40}$ signals are described in section Detailed description of HOA decomposition and recomposition. A frame-wise processing for the compression with non-overlapping input frames  $D(k)$ of HOA coefficient sequences of length B is used, where k denotes the frame index. The frames are defined with respect  $_{45}$ to the HOA coefficient sequences specified in equation (42) as

$$
D(k) := [d((kB+1)T_S)d((kB+2)T_S) \dots d((kB+B)T_S)],
$$
\n(1)

where  $T<sub>S</sub>$  denotes the sampling period.

In FIG.  $1a$ , a frame  $D(k)$  of HOA coefficient sequences is input to a dominant sound source directions estimation step or stage 11, which analyses the HOA representation for the presence of dominant directional signals, of which the directions are estimated. The direction estimation can be 55 performed e.g. by the processing described in patent publi cation EP 2665208A1. The estimated directions are denoted by  $\Omega_{DOM,1}(k), \ldots, \Omega_{DOM,2}(k)$ , where D denotes the maximum number of direction estimates. They are assumed to be arranged in a matrix  $A_{\hat{\Omega}}(k)$  as 60

$$
A_{\hat{\Omega}}(k) := [\hat{\Omega}_{DOM,1}(k) \dots \hat{\Omega}_{DOM,1}(k)]. \tag{2}
$$

It is implicitly assumed that the direction estimates are appropriately ordered by assigning them to the direction estimates from previous frames. Hence, the temporal 65 sequence of an individual direction estimate is assumed to describe the directional trajectory of a dominant sound

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source. In particular, if the d-th dominant sound source is supposed not to be active, it is possible to indicate this by assigning a non-valid value to  $\Omega_{DOM,d}(k)$ . Then, exploiting the estimated directions in  $A_{\hat{\Omega}}(k)$ , the HOA representation is decomposed in a decomposing step or stage 12 into a number of maximum  $\mathcal D$  dominant directional signals  $X_{DR}$  $(k-1)$ , some parameters  $\zeta(k-1)$  describing the prediction of the spatial domain signals of the residual HOA component from the dominant directional signals, and an ambient HOA component  $\hat{D}_4(k-2)$  representing the prediction error. A detailed description of this decomposition is provided in section HOA decomposition.

 $X_{DIR}(k-1)$  and of the residual ambient HOA component  $D_A(k-2)$ , is shown. The directional signals  $X_{DIR}(k-1)$  are In FIG.  $1b$  the perceptual coding of the directional signals conventional time domain signals which can be individually compressed using any existing perceptual compression tech nique. The compression of the ambient HOA domain com ponent  $D_A(k-2)$  is carried out in two successive steps or stages. In an order reduction step or stage 13 the reduction to Ambisonics order  $N_{RED}$  is carried out, where e.g.  $N_{RED}=1$ , resulting in the ambient HOA component  $D_{A,RED}(k-2)$ . Such order reduction is accomplished by keeping in  $D_A(k-2)$  only  $(N_{RED}+1)^2$  HOA coefficients and dropping the other ones. At decoder side, as explained below, for the ommitted values corresponding Zero values are appended.

30 the remaining amount of directivity of the residual ambient It is noted that, compared to the approach in patent publication EP 2665208 A1, the reduced order  $N_{RED}$  may in general be chosen smaller, since the total power as well as HOA component is smaller. Therefore the order reduction causes smaller errors as compared to EP 2665208 A1.

35 ent HOA component  $D_{A,RED}$ (k-2) are decorrelated to obtain In a following decorrelation step or stage 14, the HOA coefficient sequences representing the order reduced ambibank of) parallel perceptual encoders or compressors 15 operating by any known perceptual compression technique. The decorrelation is performed in order to avoid perceptual coding noise unmasking when rendering the HOA represen tation following its decompression (see patent publication EP 12305860.4 for explanation). An approximate decorre lation can be achieved by transforming  $D_{A,RED}$ (k-2) to  $O_{RED}$  equivalent signals in the spatial domain by applying a Spherical Harmonic Transform as described in EP 2469742 A2.

50 achieve the best possible decorrelation effect. A further Alternatively, an adaptive Spherical Harmonic Transform as proposed in patent publication EP 12305861.2 can be used, where the grid of sampling directions is rotated to alternative decorrelation technique is the Karhunen-Loeve transform (KLT) described in patent application EP 12305860.4. It is noted that for the last two types of de-correlation some kind of side information, denoted by  $\alpha(k-2)$ , is to be provided in order to enable reversion of the decorrelation at a HOA decompression stage.

In one embodiment, the perceptual compression of all<br>time domain signals  $X_{DIR}(k-1)$  and  $W_{A,RED}(k-2)$  is performed jointly in order to improve the coding efficiency.

Output of the perceptual coding is the compressed direc tional signals  $X_{\text{DIR}}(k-1)$  and the compressed ambient time domain signals W<sub>A,RED</sub>(k-2).<br>Decompression Processing

The decompression processing is shown in FIG. 2a and FIG.2b. Like the compression, it consists of two successive steps. In FIG. 2a a perceptual decompression of the directional signals  $X_{DIR}(k-1)$  and the time domain signals

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 $\check{W}_{A,RED}$ (k-2) representing the residual ambient HOA component is performed in a perceptual decoding or decom pressing step or stage 21. The resulting perceptually decom pressed time domain signals  $W_{A,RED}(k-2)$  are re-correlated in a recorrelation step or stage  $22$  in order to provide the  $\overline{5}$ residual component HOA representation  $\hat{D}_{A,RED}$ (k-2) of order  $N_{RED}$ . Optionally, the re-correlation can be carried out in a reverse manner as described for the two alternative processings described for step/stage 14, using the transmitted or stored parameters  $\alpha(k-2)$  depending on the decorrelation method that was used. Thereafter, from  $\hat{D}_{ARED}$ (k-2) an appropriate HOA representation  $\hat{D}_A(k-2)$  of order N is estimated in order extension step or stage 23 by order extension. The order extension is achieved by appending corresponding 'zero' value rows to  $D_{A,RED}$ (k-2), thereby assuming that the HOA coefficients with respect to the

higher orders have zero values.<br>In FIG.  $2b$ , the total HOA representation is re-composed in a composition step or stage 24 from the decompressed dominant directional signals  $\hat{X}_{DR}(k-1)$  together with the 20 corresponding directions  $A_{\hat{\Omega}}(k)$  and the prediction parameters  $\zeta(k-1)$ , as well as from the residual ambient HOA component  $\ddot{D}_4(k-2)$ , resulting in decompressed and recomposed frame  $\hat{D}(k-2)$  of HOA coefficients.

In case the perceptual compression of all time domain 25 signals  $X_{DIR}(k-1)$  and  $W_{A,RED}(k-2)$  was performed jointly in order to improve the coding efficiency, the perceptual decompression of the compressed directional signals  $X_{DIR}(k-1)$  and the compressed time domain signals  $W_{$  $(k-1)$  and the compressed time domain signals  $W_{A,RED}$ <br>(k-2) is also performed jointly in a corresponding manner. 30

A detailed description of the recomposition is provided in section HOA recomposition.

HOA Decomposition

A block diagram illustrating the operations performed for the HOA decomposition is given in FIG. 3. The operation is 35 summarised: First, the smoothed dominant directional signals  $X_{DIR}(k-1)$  are computed and output for perceptual compression. Next, the residual between the HOA represen tation  $D_{DIR}(k-1)$  of the dominant directional signals and the original HOA representation  $D(k-1)$  is represented by a 40 number of O directional signals  $\tilde{X}_{GRID,DIR}(k-1)$ , which can be thought of as general plane waves from uniformly distributed directions. These directional signals are pre-<br>dicted from the dominant directional signals  $X_{DR}(k-1)$ , dicted from the dominant directional signals  $X_{DIR}(k-1)$ , where the prediction parameters  $\zeta(k-1)$  are output. Finally, 45 the residual D<sub>A</sub>(k-2) between the original HOA representation D<sub>DIR</sub>(k-1) of the dominant directional signals together with the HOA repredominant directional signals together with the HOA representation  $\hat{D}_{GRID,DIR}(k-2)$  of the predicted directional signals from uniformly distributed directions is computed and out- 50 put.

Before going into detail, it is mentioned that the changes of the directions between successive frames can lead to a discontinuity of all computed signals during the composi nals for overlapping frames are computed first, which have a length of 2B. Second, the results of successive overlapping frames are smoothed using an appropriate window function. Each smoothing, however, introduces a latency of a single frame. tion. Hence, instantaneous estimates of the respective sig- 55

Computing Instantaneous Dominant Directional Signals

The computation of the instantaneous dominant direction signals in step or stage 30 from the estimated sound source directions in  $A_{\hat{\Omega}}(k)$  for a current frame  $D(k)$  of HOA coefficient sequences is based on mode matching as described in M. A. Poletti, "Three-Dimensional Surround Sound Systems Based on Spherical Harmonics". J. Audio 65 8

Eng. Soc., 53(11), pages 1004-1025, 2005. In particular, tation results in the best approximation of the given HOA signal.

Further, without loss of generality, it is assumed that each direction estimate  $\hat{\Omega}_{DOM,d}(\mathbf{k})$  of an active dominant sound source can be unambiguously specified by a vector containing an inclination angle  $\theta_{DOM,d}(k) \in [0,\pi]$  and an azimuth angle  $\phi_{DOM,d}(k) \in [0,2\pi]$  (see FIG. 5 for illustration) according to

$$
_{\mathcal{O}M\mathcal{A}}(k) := (\hat{\theta}_{DOM\mathcal{A}}(k), \hat{\phi}_{DOM\mathcal{A}}(k))^T. \tag{3}
$$

First, the mode matrix based on the direction estimates of active sound sources is computed according to

$$
\mathbb{E}_{ACT}(k) := [SDOM, d_{ACT,1}(k)^{(k)S}DOM, d_{ACT,2}(k)^{(k)} \dots
$$
\n
$$
\mathbf{S}_{DOM, d_{ACT,D_{ACT}(k)}(k)}(k) \otimes_{j \in \mathbb{R}} \mathcal{O} \times \mathcal{D}_{ACT}(k)
$$
\n
$$
\tag{4}
$$

with

 $\hat{\Omega}_{Di}$ 

$$
S_{DOM,d}(k) := [S_0^0(\hat{\Omega}_{DOM,d}(k)), S_1^{-1}(\hat{\Omega}_{DOM,d}(k)), S_1^0)
$$
  

$$
(\hat{\Omega}_{DOM,d}(k)), \dots, S_N^N(\hat{\Omega}_{DOM,d}(k))]^T \in \mathbb{R}^O.
$$
 (5)

In equation (4),  $D_{ACT}(k)$  denotes the number of active directions for the k-th frame and  $d_{ACT,j}(k)$ ,  $1 \le j \le D_{ACT}(k)$ indicates their indices.  $S_n^m(\cdot)$  denotes the real-valued Spherical Harmonics, which are defined in section Definition of real valued Spherical Harmonics.

tion of real valued Spherical Harmonics.<br>
Second, the matrix  $\tilde{X}_{DR}(\mathbf{k}) \in \mathbb{R}$   $\mathcal{D}^{\times 2B}$  containing the instantaneous estimates of all dominant directional signals for the (k-1)-th and k-th frames defined as

$$
\tilde{X}_{DIR}(k) := [\tilde{x}_{DIR}(k,1)\tilde{x}_{DIR}(k,2) \dots \tilde{x}_{DIR}(k,2B)] \tag{6}
$$

with

$$
\tilde{x}_{DR}(k,l):=[\tilde{x}_{DIR,1}(k,l)\tilde{x}_{DIR,2}(k,l),\ldots,\tilde{x}_{DIR,1} \mathcal{D}(k,l)]^T\in\mathbb{R} \mathcal{D}_{,1\leq l\leq 2B}
$$
\n
$$
(7)
$$

is computed. This is accomplished in two steps. In the first step, the directional signal samples in the rows correspond ing to inactive directions are set to Zero, i.e.

$$
\tilde{x}_{DR,d}(k,l)=0 \forall 1 \le l \le 2B, \text{ if } d \notin \mathcal{M}_{\Lambda CT}(k),\tag{8}
$$

where  $\mathcal{M}_{\text{ACT}}(k)$  indicates the set of active directions. In the second step, the directional signal samples corresponding to active directions are obtained by first arranging them in a matrix according to

$$
\tilde{X}_{DIR, ACT}(k) := \tag{9}
$$

$$
\begin{bmatrix} \tilde{x}_{DIRA_{ACT,I}(k)}(k, 1) & \dots & \tilde{x}_{DIRA_{ACT,I}(k)}(k, 2B) \\ \vdots & \ddots & \vdots \\ \tilde{x}_{DIRA_{ACT,IB_{ACT}(k)}(k)}(k, 1) & \dots & \tilde{x}_{DIRA_{ACT,ID_{ACT}(k)}(k)}(k, 2B) \end{bmatrix}.
$$

This matrix is then computed to minimise the Euclidean norm of the error

$$
\Xi_{\mathcal{A}\mathcal{C}\mathcal{I}}(k)\tilde{X}_{\mathcal{D}\mathcal{I}\mathcal{R},\mathcal{A}\mathcal{C}\mathcal{I}}(k)-[D(k-1)D(k)].\tag{10}
$$

The solution is given by

$$
\tilde{X}_{DR,ACT}(k) = [\Xi_{ACT}^T(k)\Xi_{ACT}(k)]^{-1}\Xi_{ACT}^T(k)[D(k-1)D
$$
\n
$$
(k)].
$$
\n
$$
(11)
$$

Temporal Smoothing

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For step or stage 31, the smoothing is explained only for the directional signals  $\tilde{X}_{DIR}(k)$ , because the smoothing of other types of signals can be accomplished in a completely analogous way. The estimates of the directional signals  $\tilde{X}_{DIR,d}(k,l)$ ,  $1 \leq d \leq \mathcal{D}$ , whose samples are contained in the

matrix  $\tilde{X}_{DIR}(k)$  according to equation (6), are windowed by an appropriate window function w(1):

 $\tilde{x}_{DIR,WIN,d}(k,l) := \tilde{x}_{DIR,d}(k,l) \cdot w(l), 1 \leq l \leq 2B. \eqno(12)$ 

This window function must satisfy the condition that it  $\frac{1}{5}$ sums up to '1' with its shifted version (assuming a shift of B samples) in the overlap area:

$$
w(l) + w(B+l) = 1 \forall 1 \le l \le B. \tag{13}
$$

An example for such window function is given by the  $_{10}$  residual  $[D(k-2) D(k-1)]-[D_{DIR}(k-2) D_{DIR}(k-1)].$ periodic Hann window defined by

$$
w(l) := 0.5 \left[ 1 - \cos \left( \frac{2\pi (l-1)}{2B} \right) \right] \text{ for } 1 \le l \le 2B.
$$
 (14)

The smoothed directional signals for the  $(k-1)$ -th frame are computed by the appropriate superposition of windowed instantaneous estimates according to

$$
x_{DIR,d}((k-1)B+l)=\tilde{x}_{DIR,WIN,d}(k-1,B+l)+\tilde{x}_{DIR,WIN,d}(k,l).\eqno(15)
$$

The samples of all smoothed directional signals for the  $(k-1)$ -th frame are arranged in the matrix

$$
X_{DR}(k-1):=[x_{DR}((k-1)B+1)x_{DR}((k-1)B+2)\dots x_{DR}
$$
  
 
$$
((k-1)B+B)| \in \mathbb{R} \mathcal{D} \times B
$$
 (16)

with

$$
\mathcal{D}_{DR}(l)=[x_{DIR,1}(l)), x_{DIR,2}(l), \ldots, x_{DIR,1} \mathcal{D}_{(l)}]^T \in \mathbb{R}
$$
\n
$$
\mathcal{D}.
$$
\n(17)

The smoothed dominant directional signals  $x_{DIR,d}(l)$  are supposed to be continuous signals, which are successively input to perceptual coders.

Computing HOA Representation of Smoothed Dominant 35 Directional Signals

From  $X_{DR}(k-1)$  and  $A_{\hat{\Omega}}(k)$ , the HOA representation of the Smoothed dominant directional signals is computed in step or stage 32 depending on the continuous signals  $X_{DIR}$  (1) in order to mimic the same operations like to be performed for the HOA composition. Because the changes of the direction estimates between successive frames can lead to a discontinuity, once again instantaneous HOA representations of overlapping frames of length  $2B$  are  $_{45}$ computed and the results of successive overlapping frames are smoothed by using an appropriate window function. Hence, the HOA representation  $D_{DR}(k-1)$  is obtained by

Representing Residual HOA Representation by Directional Signals on Uniform Grid

From  $D_{DIR}(k-1)$  and  $D(k-1)$  (i.e.  $D(k)$  delayed by frame delay 381), a residual HOA representation by directional signals on a uniform grid is calculated in step or stage 33.<br>The purpose of this operation is to obtain directional signals (i.e. general plane wave functions) impinging from some fixed, nearly uniformly distributed directions  $\hat{\Omega}_{GRID, \alpha}$ ,  $1\!\!\leq\!\!o\!\!\leq\!\!O$  (also referred to as grid directions), to represent the

First, with respect to the grid directions the mode matrix  $E_{GRID}$  is computed as

$$
\mathbb{E}_{GRID} = [S_{GRID,1} S_{GRID,2} \dots S_{GRID,0}] \in \mathbb{R}^{O \times O}
$$
\n(21)

with

30

20

$$
S_{GRID,\circ} := [S_0^0(\hat{\Omega}_{GRID,\circ}), S_1^{-1}(\hat{\Omega}_{GRID,\circ}), S_1^0)
$$
  

$$
(\hat{\Omega}_{GRID,\circ}), \dots, S_N^N(\hat{\Omega}_{GRID,\circ})]^T \in \mathbb{R}^O.
$$
 (22)

Because the grid directions are fixed during the whole compression procedure, the mode matrix  $\Xi_{GRID}$  needs to be computed only once.

The directional signals on the respective grid are obtained aS

$$
\begin{aligned} \tilde{X}_{GRID,DR}(k-1) &= \mathbb{E}_{GRID}^{-1}([D(k-2)D(k-1)] - [D_{DIR}(k-1)] \\ & \quad 2)D_{DIR}(k-1)]). \end{aligned} \tag{23}
$$

Predicting Directional Signals on Uniform Grid from Domi nant Directional Signals

From  $\tilde{X}_{GRID,DIR}(k-1)$  and  $X_{DIR}(k-1)$ , directional signals on the uniform grid are predicted in step or stage 34. The prediction of the directional signals on the uniform grid composed of the grid directions  $\Omega_{GRID, o}$ , 1sosO from the directional signals is based on two successive frames for smoothing purposes, i.e. the extended frame of grid signals  $\tilde{X}_{GRID,DIR}(k-1)$  (of length 2B) is predicted from the extended frame of smoothed dominant directional signals

$$
\tilde{X}_{\text{DIR,EXT}}(k-1) := [X_{\text{DIR}}(k-3)X_{\text{DIR}}(k-2)X_{\text{DIR}}(k-1)].\tag{24}
$$

FIRST, each grid signal  $X_{GRID,DR,0}(K-1,1)$  1sosO, contrained in  $\tilde{X}_{GRID,DR}(K-1)$  is assigned to a dominant directained in  $X_{GRID,DIR}(k-1)$  is assigned to a dominant directional signal  $\tilde{X}_{DR,EXT,d}(k-1,l)$ ,  $1 \le d \le \mathcal{D}$ , contained in  $\tilde{X}_{DIR,EXT}(k-1)$ . The assignment can be based on the computation of the normalised cross-correlation function between the grid signal and all dominant directional signals. In particular, that dominant directional signal is assigned to the grid signal, which provides the highest value of the normalised cross-correlation function. The result of the assignment can be formulated by an assignment

(20)

$$
D_{DIR}(k-1) = \Xi_{ACT}(k)X_{DIR,ACT,WIN1}(k-1) + \Xi_{ACT}(k-1)X_{DIR, ACT,WIN2}(k-1),
$$
\n(18)



and  $X_{DIR, ACT, WIN2}(k-1)$ :=

xpirac (-1)(k-1)B+1): w(B+1) xpirack-)(k-1)B+1): w(B+1) \*DIRdAct perce-1)(k-1)(k - 1) B + 1). w(B+ 1) ... XDIRdacid-1)(k-1)(KB) w(2B)

 $\sum_{A \in \mathcal{A}} \sum_{A \in \mathcal{A}} (k)^{(k)(k)(k+1)}$  ...  $\sum_{A \in \mathcal{A}} \sum_{A \in \mathcal{A}} (k)^{(k)(k)(k+1)}$ 

function  $\{a_{k-1} : \{1, \ldots, 0\} \rightarrow \{1, \ldots, D\}$  assigning the o-th grid signal to the  $I_{A,k-1}(0)$ -th dominant directional signal.

Second, each grid signal  $\tilde{\mathbf{x}}_{GRID,DIR}$  (k-1,l) is predicted from the assigned dominant directional signal  $\tilde{\mathbf{x}}_{GRID,DIR, o}$ (k-1,l)  $5$  is computed by a delay and a scaling from the assigned is dominant directional signal  $\tilde{x}_{\text{DIR,EXT},f_{\mathcal{A},k-1}}(k-1,l)$  as

$$
\hat{\tilde{\mathbf{x}}}_{GRID,DIR,o}(k-1,l)=K_{o}(k-1)\cdot\tilde{\mathbf{x}}_{DR,EXT}\mathbf{f}_{\mathcal{A},k-1(o)}(k-1,l-\Delta_{o}(k-1)),
$$
\n(25)

where K<sub>o</sub>(k-1) denotes the scaling factor and  $\Delta_0(k-1)$ indicates the sample delay. These parameters are chosen for minimising the prediction error.

If the power of the prediction error is greater than that of the grid signal itself, the prediction is assumed to have  $_{15}$ failed. Then, the respective prediction parameters can be set to any non-valid value.

It is noted that also other types of prediction are possible. For example, instead of computing a full-band scaling factor, it is also reasonable to determine scaling factors for  $_{20}$   $D_A(k-2)$ . perceptually oriented frequency bands. However, this opera tion improves the prediction at the cost of an increased amount of side information.

All prediction parameters can be arranged in the param eter matrix as

$$
\zeta(k-1) := \begin{bmatrix} f_{\mathcal{A},k-1}(1) & K_1(k-1) & \Delta_1(k-1) \\ f_{\mathcal{A},k-1}(2) & K_2(k-1) & \Delta_2(k-1) \\ \vdots & \vdots & \vdots \\ f_{\mathcal{A},k-1}(O) & K_O(k-1) & \Delta_O(k-1) \end{bmatrix}.
$$
 (26)

12

version (delay 382) of  $D_{DIR}(k-1)$ , the HOA representation of the residual ambient sound field component is computed in step or stage 37 by

$$
D_A(k-2)=D(k-2)-\hat{D}_{GRID,DIR}(k-2)-D_{DIR}(k-2). \tag{28}
$$

# HOA Recomposition

Before describing in detail the processing of the indi vidual steps or stages in FIG. 4 in detail, a Summary is provided. The directional signals  $\tilde{X}_{GRID,DR}(k-1)$  with respect to uniformly distributed directions are predicted from the decoded dominant directional signals  $\hat{X}_{DR}(k-1)$  using the prediction parameters  $\hat{\zeta}(k-1)$ . Next, the total HOA representation  $\hat{D}(k-2)$  is composed from the HOA representation  $\hat{D}_{DR}(k-2)$  of the dominant directional signals, the HOA representation  $\hat{D}_{GRID,DR}(k-2)$  of the predicted directional signals and the residual ambient HOA component

Computing HOA Representation of Dominant Directional Signals

25 determining an HOA representation of dominant directional 30  $A_{\hat{\Omega}}(k)$  and  $X_{DIR}(k-1)$  are input to a step or stage 41 for signals. After having computed the mode matrices  $\Xi_{AC}(\mathbf{k})$ and  $E_{ACZ}(k-1)$  from the direction estimates  $A_{\hat{O}}(k)$  and  $A_{\Omega}(k-1)$ , based on the direction estimates of active sound sources for the k-th and (k-1)-th frames, the HOA representation of the dominant directional signals  $D_{DIR}(k-1)$  is obtained by

 $\hat{D}_{DIR}(k-1) = \Xi_{ACT}(k)X_{DIR, ACT, WIN1}(k-1)+\Xi_{ACT}(k-1)X_{DIR, ACT, WIN2}(k-1),$ 

$$
\text{where } X_{DIR,ACT,WIN1}(k-1) := \begin{bmatrix} \hat{x}_{DIR,d_{ACT,1}(k)}((k-1)B+1)\cdot w(1) & \dots & \hat{x}_{DIR,d_{ACT,1}(k)}(kB)\cdot w(B) \\ \hat{x}_{DIR,d_{ACT,2}(k)}((k-1)B+1)\cdot w(1) & \hat{x}_{DIR,d_{ACT,2}(k)}(kB)\cdot w(B) \\ \vdots & \ddots & \vdots \\ \hat{x}_{DIR,d_{ACT,D_{ACT}(k)}(k)}((k-1)B+1)\cdot w(1) & \dots & \hat{x}_{DIR,d_{ACT,D_{ACT}(k)}(k)}(kB)\cdot w(B) \\ \hat{x}_{DIR,d_{ACT,D_{ACT}(k-1)}(k-1)B+1)\cdot w(1)} & \dots & \hat{x}_{DIR,d_{ACT,D_{ACT}(k-1)}(kB)\cdot w(2B)} \\ \hat{x}_{DIR,d_{ACT,2}(k-1)}((k-1)B+1)\cdot w(B+1) & \dots & \hat{x}_{DIR,d_{ACT,2}(k-1)}(kB)\cdot w(2B) \\ \vdots & \ddots & \vdots \\ \hat{x}_{DIR,d_{ACT,2}(k-1)}((k-1)B+1)\cdot w(B+1) & \hat{x}_{DIR,d_{ACT,2}(k-1)}(kB)\cdot w(2B) \\ \vdots & \ddots & \vdots \\ \hat{x}_{DIR,d_{ACT,D_{ACT}(k-1)}(k-1)(k+1)}((k-1)B+1)\cdot w(B+1) & \dots & \hat{x}_{DIR,d_{ACT,D_{ACT}(k-1)}(kB)\cdot w(2B)} \end{bmatrix} \tag{31}
$$

All predicted signals  $\ddot{x}_{GRID,DIR, o}(k-1, l)$ ,  $1 \le o \le O$ , are  $_{50}$ assumed to be arranged in the matrix  $\tilde{X}_{GRID,DR}(k-1)$ . Computing HOA Representation of Predicted Directional Signals on Uniform Grid

The HOA representation of the predicted grid signals is computed in step or stage 35 from  $\tilde{X}_{GRID,DIR}(k-1)$  according tO

$$
\hat{\tilde{D}}_{GRID,DIR}(k-1) = \Xi_{GRID}\hat{\tilde{X}}_{GRID,DIR}(k-1). \tag{27}
$$

Computing HOA Representation of Residual Ambient Sound Field Component

From  $\ddot{D}_{GRID,DIR}$ (k-2), which is a temporally smoothed

version (in step/stage 36) of  $D_{GRID,DIR}(K-1)$ , from  $D(K-2)$  <sub>65</sub> which is a two-frames delayed version (delays 381 and 383) of D(k), and from  $D_{DR}(k-2)$  which is a frame delayed

Predicting Directional Signals on Uniform Grid from Domi

 $\widehat{\zeta}$ (k-1) and  $\widehat{X}_{DIR}$ (k-1) are input to a step or stage 43 for predicting directional signals on uniform grid from domi nant directional signals. The extended frame of predicted directional signals on uniform grid consists of the elements  $\hat{\tilde{\mathbf{x}}}_{GRID,DIR, o}$ (k-1,1) according to

 $\hat{\hat{X}}_{GRID,DIR}(k-1) =$  (32)

 $55<sub>1</sub>$ 

60

 $\hat{\tilde{x}}_{GRID,DIR,1}(k-1, 1)$  ...  $\hat{\tilde{x}}_{GRID,DIR,1}(k-1, 2B)$  $\begin{array}{lll} \hat{\tilde{x}}_{GRID,DIR,2}(k-1,\,1) & \hat{\tilde{x}}_{GRID,DIR,2}(k-1,\,2B) \\ \vdots & \ddots & \vdots \end{array}$  $\hat{\tilde{x}}_{GRID,DIR,O}(k-1, 1)$  ...  $\hat{\tilde{x}}_{GRID,DIR,O}(k-1, 2B)$ 

(29)

15

 $20$ 

which are predicted from the dominant directional signals by

$$
\tilde{\mathbf{x}}_{GRID,DIR,o}(k-1,l)=K_{o}(k-1)\cdot\hat{\mathbf{x}}_{DIR},\mathbf{f}_{\mathcal{A},k-1}(\mathbf{f}_{\mathcal{O}})((k-1)B+1)\cdot\mathbf{f}_{\mathcal{O}}(k-1)).
$$
\n(33)

Computing HOA Representation of Predicted Directional Signals on Uniform Grid

In a step or stage 44 for computing the HOA representa tion of predicted directional signals on uniform grid, the HOA representation of the predicted grid directional signals is obtained by

$$
\hat{\tilde{D}}_{GRID,DIR}(k-1) = \mathbb{E}_{GRID}\hat{\tilde{X}}_{GRID,DIR}(k-1),\tag{24}
$$

where  $\Xi_{GRID}$  denotes the mode matrix with respect to the predefined grid directions (see equation (21) for definition).

Composing HOA Sound Field Representation<br>From  $\hat{D}_{DR}(k-2)$  (i.e.  $\hat{D}_{DR}(k-1)$  delayed by frame delay 42),  $\hat{D}_{GRID,DIR}(k-2)$  (which is a temporally smoothed ver-

sion of  $D_{GRID,DIR}(k-1)$  in step/stage **45**) and  $D_A(k-2)$ , the total HOA sound field representation is finally composed in a step or stage 46 as

$$
\hat{D}(k-2) = \hat{D}_{DIR}(k-2) + \hat{D}_{GRID,DIR}(k-2) + \hat{D}_{A}(k-2). \tag{35}
$$

Basics of Higher Order Ambisonics

Higher Order Ambisonics is based on the description of a sound field within a compact area of interest, which is 25 assumed to be free of Sound sources. In that case the spatiotemporal behaviour of the sound pressure  $p(t,x)$  at time t and position x within the area of interest is physically fully determined by the homogeneous wave equation. The following is based on a spherical coordinate system as shown in FIG. 5. The X axis points to the frontal position, the y axis points to the left, and the Z axis points to the top. A position in space  $x=(r,\theta,\phi)^T$  is represented by a radius r>0 (i.e. the distance to the coordinate origin), an inclination angle  $\theta \in [0,\pi]$  measured from the polar axis z and an <sup>35</sup> azimuth angle  $\phi \in [0, 2\pi]$  measured counter-clockwise in the x-y plane from the x axis.  $(\cdot)^T$  denotes the transposition. 30

It can be shown (see E. G. Williams, "Fourier Acoustics", volume 93 of Applied Mathematical Sciences, Academic with respect to time denoted by  $\mathcal F$  ( $\bullet$ ), i.e. Press, 1999) that the Fourier transform of the sound pressure 40

$$
P(\omega, x) = \mathcal{F}_{t}(p(t, x)) = \int_{-\infty}^{\infty} p(t, x)e^{-i\omega t}dt
$$
\n(36)

with  $\omega$  denoting the angular frequency and i denoting the imaginary unit, may be expanded into a series of Spherical  $_{45}$ Harmonics according to

$$
P(\omega = kc_s r, \theta, \phi) = \sum_{n=0}^{N} \sum_{m=-n}^{N} A_n^m(k) j_n(kr) S_n^m(\theta, \phi),\tag{37}
$$

where  $c_s$  denotes the speed of sound and k denotes the angular wave number, which is related to the angular frequency  $\omega$  by

$$
k = \frac{\omega}{c_s}, \, j_n(.)
$$

denotes the spherical Bessel functions of the first kind, and  $S_n^{\,m}(\theta,\phi)$  denotes the real valued Spherical Harmonics of order n and degree m which are defined in section Definition of real valued Spherical Harmonics. The expansion coeffi cients  $A_n^m(k)$  are depending only on the angular wave number k. Note that it has been implicitely assumed that sound pressure is spatially band-limited. Thus the series is truncated with respect to the order index n at an upper limit N, which is called the order of the HOA representation. 60 65

If the sound field is represented by a superposition of an infinite number of harmonic plane waves of different angular frequencies  $\omega$  and is arriving from all possible directions specified by the angle tuple  $(\theta, \phi)$ , it can be shown (see B. Rafaely, "Plane-wave Decomposition of the Sound Field on a Sphere by Spherical Convolution". J. Acoust. Soc. Am... 4 (116), pages 2149-2157, 2004) that the respective plane wave complex amplitude function  $D(\omega,\theta,\phi)$  can be expressed by the Spherical Harmonics expansion

$$
D(\omega = kc_s, \theta, \phi) = \sum_{n=0}^{N} \sum_{m=-n}^{N} D_n^m(k) S_n^m(\theta, \phi),
$$
\n(38)

where the expansion coefficients  $D_n^m(k)$  are related to the expansion coefficients  $A_n^m(k)$  by

$$
A_n^{\ \ m}(k) = 4\pi i^n D_n^{\ \ m}(k). \tag{39}
$$

Assuming the individual coefficients  $D_m^m(k=\omega/c_s)$  to be functions of the angular frequency  $\omega$ , the application of the inverse Fourier transform (denoted by  $\mathcal{F}_t^{-1}(\cdot)$ ) provides time domain functions

$$
l_n^m(t) = \mathcal{F}_t^{-1} \Big( D_n^m \Big( \frac{\omega}{c_s} \Big) \Big) = \frac{1}{2\pi} \int_{-\infty}^{\infty} D_n^m \Big( \frac{\omega}{c_s} \Big) e^{i\omega t} \, d\omega \tag{40}
$$

for each order n and degree m, which can be collected in a single vector

 $d(t) =$ 

$$
\begin{bmatrix} d_0^0(t) & d_1^{-1}(t) & d_1^0(t) & d_1^1(t) & d_2^{-2}(t) & d_2^{-1}(t) & d_2^0(t) & d_2^1(t) & d_2^2(t) & \dots \\ d_N^{N-1}(t) & d_N^N(t) & & & \end{bmatrix}^T.
$$

The position index of a time domain function  $d_m^m(t)$ within the vector  $d(t)$  is given by  $n(n+1)+1+m$ .

The final Ambisonics format provides the sampled ver sion of  $d(t)$  using a sampling frequency  $f_s$  as

$$
[\boldsymbol{d}(l_{\rm S})\}_{l \in \mathbb{N}} = \{d(T_{\rm S}), d(2T_{\rm S}), d(3T_{\rm S}), d(4T_{\rm S}), \dots\},\tag{42}
$$

where  $T_s=1/f_s$  denotes the sampling period. The elements of  $d(T<sub>S</sub>)$  are referred to as Ambisonics coefficients. Note that the time domain signals  $d_n^m(t)$  and hence the Ambisonics coefficients are real-valued.

Definition of Real-Valued Spherical Harmonics

The real valued spherical harmonics  $S_{n}^{m}(\theta,\phi)$  are given by

$$
S_n^m(\theta, \phi) = \sqrt{\frac{(2n+1)}{4\pi} \frac{(n-|m|)!}{(n+|m|)!}} P_{n,|m|}(\cos\theta) tr g_m(\phi)
$$
\n(43)

with 
$$
trg_m(\phi) = \begin{cases} \sqrt{2} \cos(m\phi) & m > 0 \\ 1 & m = 0 \\ -\sqrt{2} \sin(m\phi) & m < 0 \end{cases}
$$
 (44)

The associated Legendre functions  $P_{n,m}(x)$  are defined as

$$
P_{n,m}(x) = (1 - x^2)^{m/2} \frac{d^m}{dx^m} P_n(x), \, m \ge 0
$$
\n<sup>(45)</sup>

with the Legendre polynomial  $P_n(x)$  and, unlike in the above mentioned E. G. Williams textbook, without the Condon Shortley phase term  $(-1)^m$ .

 $\Psi^H \approx \Psi^{-1}$ ,

15

65

Spatial Resolution of Higher Order Ambisonics A general plane wave function X(t) arriving from a

direction  $\Omega_0 = (\theta_0, \phi_0)^T$  is represented in HOA by  $d_n^{\ m}(t)=x(t)S_n^{\ m}(\Omega_0), 0\leq n\leq N, |m|\leq n.$  $(46)$ 

The corresponding spatial density of plane wave ampli tudes  $d(t,\Omega) := \mathcal{F}_t^{-1}(D(\omega,\Omega))$  is given by

$$
d(t, \Omega) = \sum_{n=0}^{n} \sum_{m=-n}^{n} d_n^m(t) S_n^m(\Omega)
$$
\n
$$
= x(t) \left[ \sum_{n=0}^{n} \sum_{n=0}^{n} S_n^m(\Omega_0) S_n^m(\Omega) \right].
$$
\n(48)

$$
= x(t) \left[ \sum_{n=0}^{N} \sum_{m=-n}^{n} S_n^m(\Omega_0) S_n^m(\Omega) \right].
$$
 (48)

It can be seen from equation (48) that it is a product of the general plane wave function X(t) and a spatial dispersion function  $v_{\lambda}(\Theta)$ , which can be shown to only depend on the angle  $\Theta$  between  $\Omega$  and  $\Omega_0$  having the property

$$
\cos \Theta = \cos \theta \cos \theta_0 + \cos(\phi - \phi_0) \sin \theta \sin \theta_0. \tag{49}
$$

As expected, in the limit of an infinite order, i.e.  $N \rightarrow \infty$ , the spatial dispersion function turns into a Dirac delta  $\delta(\cdot)$ , i.e.

$$
\lim_{N \to \infty} v_N(\Theta) = \frac{\delta(\Theta)}{2\pi}.
$$
\n(50)

However, in the case of a finite order  $N$ , the contribution  $30<sub>1</sub>$ of the general plane wave from direction  $\Omega_0$  is smeared to neighbouring directions, where the extent of the blurring decreases with an increasing order. A plot of the normalised function  $v_{\mathcal{N}}(\Theta)$  for different values of N is shown in FIG. 6. It is pointed out that any direction S2 of the time domain 35 behaviour of the spatial density of plane wave amplitudes is a multiple of its behaviour at any other direction. In par ticular, the functions  $d(t, \Omega_1)$  and  $d(t, \Omega_2)$  for some fixed directions  $\Omega_1$  and  $\Omega_2$  are highly correlated with each other with respect to time t. 40

Discrete Spatial Domain

If the spatial density of plane wave amplitudes is discre tised at a number of O spatial directions  $\Omega_o$ ,  $1 \leq o \leq O$ , which are nearly uniformly distributed on the unit sphere, O directional signals  $\mathbf{d}(t, \mathbf{s}_o)$  are obtained. Collecting these  $45$ signals into a vector

$$
d_{\text{SP4T}}(t) := [d(t, \Omega_1) \dots d(t, \Omega_O)]^T,
$$
\n(51)

it can be verified by using equation (47) that this vector can tion  $d(t)$  defined in equation (41) by a simple matrix multiplication as be computed from the continuous Ambisonics representa- $_{50}$ 

$$
d_{\text{SPAT}}(t) = \Psi^H d(t),\tag{52}
$$

where  $(\cdot)^H$  indicates the joint transposition and conjugation,  $\frac{55}{25}$ and  $\Psi$  denotes the mode-matrix defined by

$$
\Psi := [S_1 \dots S_O] \tag{53}
$$

with

$$
S_o := [S_0^0(\Omega_o)S_1^{-1}(\Omega hd \ o)S_1^0S_1^{-1}(\Omega_o) \ . \ . \ . \ S_N^{N-1}(\Omega_o)
$$
\n
$$
S_N^N(\Omega_o).
$$
\n(54)

Because the directions  $\Omega$ <sub>o</sub> are nearly uniformly distributed on the unit sphere, the mode matrix is invertible in general. Hence, the continuous Ambisonics representation can be computed from the directional signals  $d(t,\Omega_0)$  by

$$
d(t) = \Psi^{-H} d_{\text{SPAT}}(t). \tag{55}
$$

Both equations constitute a transform and an inverse transform between the Ambisonics representation and the spatial domain. In this application these transforms are called the Spherical Harmonic Transform and the inverse Spherical Harmonic Transform.

Because the directions  $\Omega_o$  are nearly uniformly distributed on the unit sphere,

$$
(56)
$$

<sup>10</sup> which justifies the use of  $\Psi^{-1}$  instead of  $\Psi^H$  in equation (52). Advantageously, all mentioned relations are valid for the discrete-time domain, too.

At encoding side as well as at decoding side the inventive processing can be carried out by a single processor or electronic circuit, or by several processors or electronic circuits operating in parallel and/or operating on different parts of the inventive processing.

The invention can be applied for processing correspond ing sound signals which can be rendered or played on a <sup>20</sup> loudspeaker arrangement in a home environment or on a loudspeaker arrangement in a cinema.

#### The invention claimed is:

25 representation (denoted HOA) for a sound field, said method 1. A method for compressing a Higher Order Ambisonics comprising:

from a current time frame of HOA coefficients, estimating dominant sound source directions;

- decomposing said HOA representation into dominant directional signals in a time domain and a residual HOA component, wherein said residual HOA compo nent is transformed into a discrete spatial domain in order to obtain plane wave functions at uniform Sam pling directions representing said residual HOA com ponent, and wherein said plane wave functions are predicted from said dominant directional signals, thereby providing parameters describing said prediction, and a corresponding prediction error from said prediction is transformed back into an HOA domain;
- reducing the current order of said residual HOA compo nent to a lower order, resulting in a reduced-order residual HOA component;
- de-correlating said reduced-order residual HOA compo nent to obtain corresponding residual HOA component time domain signals;
- perceptually encoding said dominant directional signals and said residual HOA component time domain signals so as to provide compressed dominant directional signals and compressed residual component signals.

2. The method according to claim 1, wherein said decorrelating of said reduced-order residual HOA component is performed by transforming said reduced-order residual HOA component to a corresponding order number of equivalent signals in the spatial domain using a Spherical Harmonic Transform.

60 equivalent signals in the spatial domain using a Spherical 3. The method according to claim 1, wherein said decorrelating of said reduced-order residual HOA component is performed by transforming said reduced-order residual HOA component to a corresponding order number of Harmonic Transform, where a grid of the uniform sampling directions is rotated, and by providing side information enabling a reversion of said de-correlating.<br>4. The method according to claim 1, wherein said per-

ceptually encoding comprises joint compression of said dominant directional signals and said residual HOA com ponent time domain signals.

5. The method according to claim 1, wherein said decom posing includes:

- computing from the estimated sound source directions in for a current frame of HOA coefficients dominant directional signals, followed by temporal Smoothing 5 resulting in smoothed dominant directional signals;
- computing from said estimated sound source directions in and said Smoothed dominant directional signals an HOA representation of smoothed dominant directional signals:
- representing a corresponding residual HOA representa tion by directional signals on a uniform grid;
- from said smoothed dominant directional signals and said residual HOA representation by directional signals, predicting directional signals on uniform grid and com 15 puting therefrom an HOA representation of predicted directional signals on uniform grid, followed by tem poral smoothing;
- computing from said smoothed predicted directional signals on uniform grid, from a two-frames delayed ver sion of said current frame of HOA coefficients, and from a frame delayed version of said smoothed domi nant directional signals an HOA representation of a residual ambient sound field component.

6. The method according to claim 1 whereby the com- 25 pressing of Higher Order Ambisonics representation com prises compressing of a digital audio signal.

7. An apparatus for compressing a Higher Order American (denoted Hoa) for a said apparatus comprising:<br>
American estimator which estimates dominant sound source 30

- directions from a current time frame of HOA coeffi cients;
- a decomposer which decomposes said HOA representa tion into dominant directional signals in time domain 35 and a residual HOA component, wherein said residual HOA component is transformed into a discrete spatial domain in order to obtain plane wave functions at uniform sampling directions representing said residual HOA component, and wherein said plane wave func- 40 tions are predicted from said dominant directional signals, thereby providing parameters describing said prediction, and a corresponding prediction error from said prediction is transformed back into the HOA domain: 45
- an order reducer which reduces the current order of said residual HOA component to a lower order, resulting in
- a de-correlator which de-correlates said reduced-order residual HOA component to obtain corresponding 50 residual HOA component time domain signals;
- an encoder which perceptually encodes said dominant time domain signals so as to provide compressed dominant directional signals and compressed residual 55 component signals.

8. The apparatus according to claim 7, wherein said de-correlating of said reduced-order residual HOA compo nent is performed by transforming said reduced-order residual HOA component to a corresponding order number 60 Ambisonics (denoted HOA) representation, said apparatus comprising: of equivalent signals in the spatial domain using a Spherical Harmonic Transform.

9. The apparatus according to claim 7, wherein said de-correlating of said reduced-order residual HOA compo nent is performed by transforming said reduced-order 65 residual HOA component to a corresponding order number of equivalent signals in the spatial domain using a Spherical

Harmonic Transform, where a grid of the uniform sampling directions is rotated, and by providing side information enabling reversion of said de-correlating.

10. The apparatus according to claim 7, wherein said perceptual encoding of said dominant directional signals and said residual HOA component time domain signals is per formed jointly.

11. The apparatus according to claim 7, wherein said decomposing includes:

- computing from the estimated Sound source directions in for a current frame of HOA coefficients dominant directional signals, followed by temporal smoothing resulting in smoothed dominant directional signals;
- computing from said estimated Sound source directions in and said Smoothed dominant directional signals an HOA representation of smoothed dominant directional signals:
- representing a corresponding residual HOA representa tion by directional signals on a uniform grid;
- from said Smoothed dominant directional signals and said residual HOA representation by directional signals, predicting directional signals on uniform grid and com puting therefrom an HOA representation of predicted directional signals on uniform grid, followed by tem poral smoothing;
- computing from said smoothed predicted directional signals on uniform grid, from a two-frames delayed ver sion of said current frame of HOA coefficients, and from a frame delayed version of said smoothed domi nant directional signals an HOA representation of a residual ambient sound field component.

12. The apparatus according to claim 11, wherein said predicting of directional signals on the uniform grid is computed by a delay and a full-band scaling from the assigned dominant directional signal.

13. The apparatus according to claim 11, wherein in said predicting of directional signals on uniform grid scaling factors for perceptually oriented frequency bands are deter mined.

14. A method for decompressing a compressed Higher Order Ambisonics (denoted HOA) representation, said method comprising:

- perceptually decoding compressed dominant directional signals and compressed residual component signals so as to provide decompressed dominant directional sig nals and decompressed time domain signals represent ing a residual HOA component in a spatial domain;
- re-correlating said decompressed time domain signals to obtain a corresponding reduced-order residual HOA component;
- extending the order of said reduced-order residual HOA component to an original order so as to provide an original order decompressed residual HOA component;
- using said decompressed dominant directional signals, said original order decompressed residual HOA com ponent, and estimated dominant sound source directions to generate a decompressed and recomposed frame of HOA coefficients.

15. An apparatus for decompressing a Higher Order

a decoder which perceptually decodes compressed domi nant directional signals and compressed residual com ponent signals so as to provide decompressed dominant directional signals and decompressed time domain sig nals representing a residual HOA component in a spatial domain;

- 19<br>a re-correlator which re-correlates said decompressed time domain signals to obtain a corresponding reduced-<br>order residual HOA component;
- an order extender which extends the order of said reduced-order residual HOA component to an original 5 order so as to provide an original order decompressed residual HOA component;
- a composer which generates a decompressed and recom posed frame of HOA coefficients by using said decom pressed dominant directional signals, said original 10 order decompressed residual HOA component, and estimated dominant sound source directions.

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